Christoph Schiller

# MOTION MOUNTAIN

# THE ADVENTURE OF PHYSICS - VOL.V

# MOTION INSIDE MATTER -

PLEASURE, TECHNOLOGY AND STARS

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Christoph Schiller

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# MOTION MOUNTAIN

The Adventure of Physics Volume V

Motion Inside Matter – Pleasure, Technology and Stars

Edition 31, available as free pdf with films at www.motionmountain.net Editio trigesima prima.

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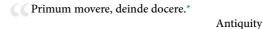
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τῷ ἐμοὶ δαὶμονι

Die Menschen stärken, die Sachen klären.



This book series is for anybody who is curious about motion in nature. How do hings, people, animals, images and empty space move? The answer leads o many adventures, and this volume presents those about motion inside everyday matter, inside people and animals, and inside stars and nuclei.

Motion *inside bodies* – dead or alive – is tiny: thus it is described by quantum theory. Quantum theory describes all motion with the quantum of action  $\hbar$ , the smallest change observed in nature. Building on this basic idea, the text first shows how to describe life, death and pleasure. Then, the text explains the observations of chemistry, materials science, astrophysics and particle physics. In the structure of physics, these topics correspond to the three 'quantum' points in Figure 1. The story of motion found inside living cells, inside the coldest gases and throughout the hottest stars is told here in a way that is simple, up to date and captivating.

In order to be *simple*, the text focuses on concepts, while keeping mathematics to the necessary minimum. Understanding the concepts of physics is given precedence over using formulae in calculations. The whole text is within the reach of an undergraduate.

In order to be *up to date*, the text is enriched by the many gems – both theoretical and empirical – that are scattered throughout the scientific literature.

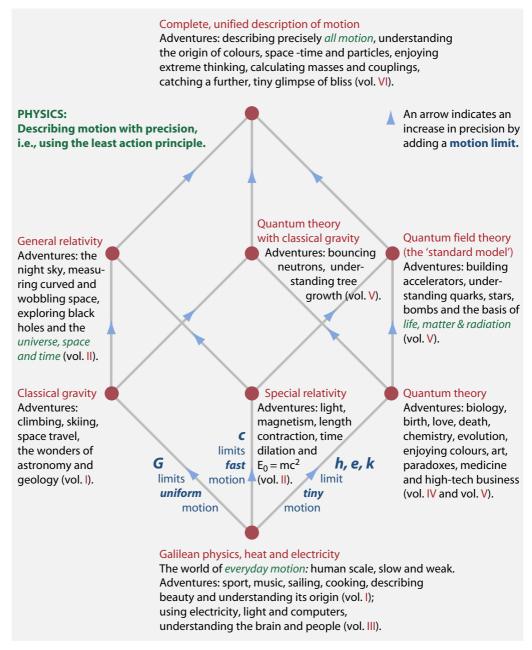
In order to be *captivating*, the text tries to startle the reader as much as possible. Reading a book on general physics should be like going to a magic show. We watch, we are astonished, we do not believe our eyes, we think, and finally we understand the trick. When we look at nature, we often have the same experience. Indeed, every page presents at least one surprise or provocation for the reader to think about. Numerous interesting challenges are proposed.

The motto of the text, *die Menschen stärken*, *die Sachen klären*, a famous statement on pedagogy, translates as: 'To fortify people, to clarify things.' Clarifying things – and adhering only to the truth – requires courage, as changing the habits of thought produces fear, often hidden by anger. But by overcoming our fears we grow in strength. And we experience intense and beautiful emotions. All great adventures in life allow this, and exploring motion is one of them. Enjoy it.

#### Christoph Schiller



<sup>\* &#</sup>x27;First move, then teach.' In modern languages, the mentioned type of *moving* (the heart) is called *motivating*; both terms go back to the same Latin root.



**FIGURE 1** A complete map of physics, the science of motion, as first proposed by Matvei Bronshtein (b. 1907 Vinnytsia, d. 1938 Leningrad). The Bronshtein cube starts at the bottom with everyday motion, and shows the connections to the fields of modern physics. Each connection increases the precision of the description and is due to a limit to motion that is taken into account. The limits are given for uniform motion by the gravitational constant G, for fast motion by the speed of light c, and for tiny motion by the Planck constant h, the elementary charge e and the Boltzmann constant k.

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#### PREFACE

#### Using this book

Marginal notes refer to bibliographic references, to other pages or to challenge solutions. In the colour edition, marginal notes, pointers to footnotes and links to websites are typeset in green. Over time, links on the internet tend to disappear. Most links can be recovered via www.archive.org, which keeps a copy of old internet pages. In the free pdf edition of this book, available at www.motionmountain.net, all green pointers and links are clickable. The pdf edition also contains all films; they can be watched directly in Adobe Reader.

Solutions and hints for *challenges* are given in the appendix. Challenges are classified as easy (e), standard student level (s), difficult (d) and research level (r). Challenges for which no solution has yet been included in the book are marked (ny).

#### Advice for learners

Learning allows us to discover what kind of person we can be. Learning widens knowledge, improves intelligence and provides a sense of achievement. Therefore, learning from a book, especially one about nature, should be efficient and enjoyable. Avoid bad learning methods like the plague! Do not use a marker, a pen or a pencil to highlight or underline text on paper. It is a waste of time, provides false comfort and makes the text unreadable. And do not learn from a screen. In particular, never, ever, learn from the internet, from videos, from games or from a smartphone. Most of the internet, almost all videos and all games are poisons and drugs for the brain. Smartphones are dispensers of drugs that make people addicted and prevent learning. Nobody putting marks on paper or looking at a screen is learning efficiently or is enjoying doing so.

In my experience as a pupil and teacher, one learning method never failed to transform unsuccessful pupils into successful ones: if you read a text for study, summarize every section you read, *in your own words and images, aloud*. If you are unable to do so, read the section again. Repeat this until you can clearly summarize what you read in your own words and images, aloud. And *enjoy* the telling aloud! You can do this alone or with friends, in a room or while walking. If you do this with everything you read, you will reduce your learning and reading time significantly; you will enjoy learning from good texts much more and hate bad texts much less. Masters of the method can use it even while listening to a lecture, in a low voice, thus avoiding to ever take notes.

#### Advice for teachers

A teacher likes pupils and likes to lead them into exploring the field he or she chose. His or her enthusiasm is the key to job satisfaction. If you are a teacher, before the start of a lesson, picture, feel and tell yourself how you enjoy the topic of the lesson; then picture, feel and tell yourself how you will lead each of your pupils into enjoying that topic as much as you do. Do this exercise consciously, every day. You will minimize trouble in your class and maximize your teaching success.

This book is not written with exams in mind; it is written to make teachers and students *understand* and *enjoy* physics, the science of motion.

#### Feedback

The latest pdf edition of this text is and will remain free to download from the internet. I would be delighted to receive an email from you at fb@motionmountain.net, especially on the following issues:

Challenge 1 s

— What was unclear and should be improved?

- What story, topic, riddle, picture or film did you miss?

Also help on the specific points listed on the www.motionmountain.net/help.html web page is welcome. All feedback will be used to improve the next edition. You are welcome to send feedback by mail or by sending in a pdf with added yellow notes, to provide illustrations or photographs, or to contribute to the errata wiki on the website. If you would like to translate a chapter of the book in your language, please let me know.

On behalf of all readers, thank you in advance for your input. For a particularly useful contribution you will be mentioned – if you want – in the acknowledgements, receive a reward, or both.

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The paper edition of this book is available, either in colour or in black and white, from www.amazon.com, in English and in certain other languages. And now, enjoy the reading.



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CONTENTS



# Motion Inside Matter – Pleasure, Technology and Stars

In our quest to understand how things move as a result of a smallest change value in nature, we discover how pleasure appears, why the floor does not fall but keeps on carrying us, that interactions are exchanges of radiation particles, that matter is not permanent, how quantum effects increase human wealth and health, why empty space pulls mirrors together, why the stars shine, where the atoms inside us come from, how quantum particles make up the world, and why swimming and flying is not so easy.

### CHAPTER 1 MOTION FOR ENJOYING LIFE

K Homo sum, humani nil a me alienum puto.\*\* Terence

Since we have explored quantum effects in the previous volume, let us now have ome serious fun with *applied* quantum physics. The quantum of action  $\hbar$  has ignificant consequences for medicine, biology, chemistry, materials science, engineering and the light emitted by stars. Also art, the colours and materials it uses, and the creative process in the artist, are based on the quantum of action. From a physics standpoint, all these domains study *motion inside matter*.

Inside matter, we observe, above all, tiny motions of quantum particles.\*\*\* Therefore the understanding and the precise description of matter requires *quantum physics*. In the following, we will only explore a cross-section, but it will be worth it. We start our exploration of motion inside matter with three special forms that are of special importance to us: life, reproduction and death. We mentioned at the start of quantum physics that none of these forms of motion can be described by classical physics. Indeed, life, reproduction and death are quantum effects. In addition, every perception, every sense, and thus every kind of pleasure is a quantum effect. The same is true for all our actions. Let us find out why.

# FROM QUANTUM PHYSICS TO BIOLOGICAL MACHINES AND MINIATURIZATION

We know that all of quantum theory can be resumed in one sentence:

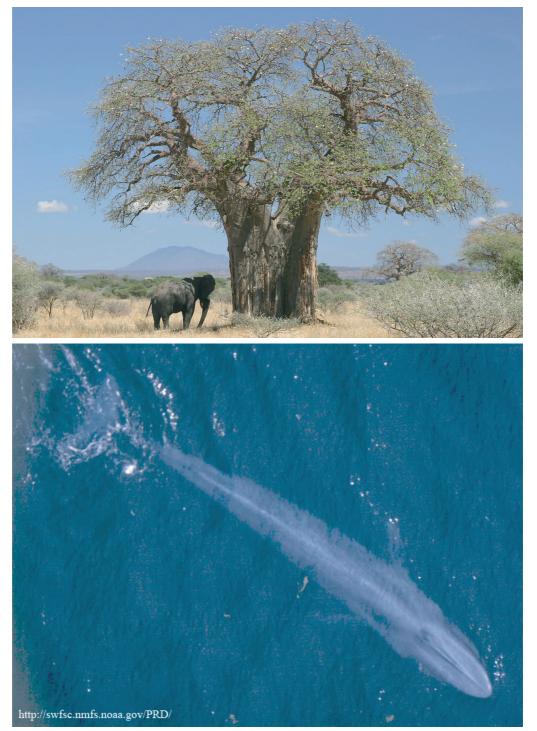
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 $\triangleright$  In nature, action or change below  $\hbar = 1.1 \cdot 10^{-34}$  Js is not observed.

In the following, we want to understand how this observation explains life, pleasure and death. An important consequence of the quantum of action is well-known.

▷ If it moves, it is made of quantons, or quantum particles.

<sup>\*\* &#</sup>x27;I am a man and nothing human is alien to me.' Terence is Publius Terentius Afer (b. *c.* 190 Carthago, d. 159 BCE Greece), the important roman poet. He writes this in his play *Heauton Timorumenos*, verse 77. \*\*\* The photograph on page 15 shows a soap bubble, the motion of the fluid in it, and the interference colours; it was taken and is copyright by Jason Tozer for Creative Review/Sony.



Starting size: the dot on the letter i – final size:

**FIGURE 2** Metabolic growth can lead from single cells, about 0.1 mm in diameter, to living beings of 25 m in size, such as the baobab or the blue whale (© Ferdinand Reus, NOAA).

Step by step we will discover how these statements are reflected in the behaviour of living beings. But what are living beings?

Living beings are physical systems that show metabolism, information processing, information exchange, reproduction and motion. All these properties can be condensed in a single statement:

▷ A *living being* is a collection of machines that is able to self-reproduce.

By *self*-reproduction, we mean that a system uses its own metabolism to reproduce. There are examples of objects which reproduce and which nobody would call living. Can you find some examples? To avoid misunderstandings, whenever we say 'reproduction' in the following, we always mean 'self-reproduction'.

Before we explore the definition of living beings in more detail, we stress that selfreproduction is simplified if the system is miniaturized. Therefore, most living beings are extremely small machines for the tasks they perform. This is especially clear when living beings are compared to human-made machines. The smallness of living beings is often astonishing, because the design and construction of human-made machines has considerably fewer requirements.

- 1. Human-made machines do not need to be able to reproduce; as a result, they can be made of many parts and can include rotating macroscopic parts. This is in contrast to living beings, who are all made of a single piece of matter, and cannot use wheels, propellers, gearwheels or even screws.
- 2. Human made machines can make use of metals, ceramics, poisonous compounds and many other materials that living beings cannot use.
- 3. Human machines do not need to self-assemble and grow; in contrast, living beings always need to carry a built-in chemical factory with them.
- 4. Human machines can be assembled and can operate at various temperatures, in strong contrast to living beings.

Despite these extreme engineering restrictions, living beings hold many miniaturization world records for machines:

- The brain has the highest processing power per volume of any calculating device so far. Just look at the size of chess champion Gary Kasparov and the size of the computer against which he played and lost. Or look at the size of any computer that attempts to speak.
- The brain has the densest and fastest memory of any device so far. The set of compact discs (CDs) or digital versatile discs (DVDs) that compare with the brain is many thousand times larger in volume.
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  - Motors in living beings are several orders of magnitude smaller than human-built ones. Just think about the muscles in the legs of an ant.
  - The motion of living beings beats the acceleration of any human-built machine by orders of magnitude. No machine achieves the movement changes of a grasshopper, a fly or a tadpole.
  - Living beings that fly, swim or crawl such as fruit flies, plankton or amoebas are still thousands of times smaller than anything comparable that is built by humans.

Challenge 2 s

In particular, already the navigation systems built by nature are far smaller than anything built by human technology.

- Living being's sensor performance, such as that of the eye or the ear, has been surpassed by human machines only recently. For the nose, this feat is still far in the future. Nevertheless, the sensor *sizes* developed by evolution think also about the ears or eyes of a common fly are still unbeaten.
- Challenge 3 s Can you spot more examples?

The superior miniaturization of living beings – compared to human-built machines – is due to their continuous strife for efficient construction. The efficiency has three main aspects. First of all, in the structure of living beings, *everything is connected to everything*. Each part influences many others. Indeed, the four basic processes in life, namely metabolic, mechanical, hormonal and electric, are intertwined in space and time. For example, in humans, breathing helps digestion; head movements pump liquid through the spine; a single hormone influences many chemical processes. Secondly, *all parts in living systems have more than one function*. For example, bones provide structure and produce blood; fingernails are tools and shed chemical waste. Living systems use many such optimizations. Last but not least, living machines are *well* miniaturized because they make efficient use of quantum effects. Indeed, every single function in living beings relies on the quantum of action. And every such function is extremely well miniaturized. We explore a few important cases.

#### Reproduction

Finding a mate is life's biggest prize. The view of biologists.

All the astonishing complexity of life is geared towards reproduction. *Reproduction*, more precisely, *self-reproduction*, is the ability of an object to build other objects similar to itself. Quantum theory told us that it is only possible to build a *similar* object, since an *exact* copy would contradict the quantum of action. But this limitation is not a disadvantage: an imperfect copy is required for life; indeed, a similar, thus imperfect copy is essential for biological evolution, and thus for change and specialization.

Reproduction is characterized by random changes, called *mutations*, that distinguish one generation from the next. The statistics of mutations, for example Mendel's 'laws' of heredity, and the lack of intermediate states, are direct consequences of quantum theory. In other words, reproduction and heredity are quantum effects.

Reproduction requires *growth*, and growth needs metabolism. *Metabolism* is a chemical process, and thus a quantum process, to harness energy, harness materials, realize growth, heal injuries and realize reproduction.

Since reproduction requires an increase in mass, as shown in Figure 2, all reproducing objects show both metabolism and growth. In order that growth can lead to an object similar to the original, a construction *plan* is necessary. This plan must be similar to the plan used by the previous generation. Organizing growth with a construction plan is only possible if nature is made of smallest entities which can be assembled following that plan.

We thus deduce that reproduction and growth implies that matter is made of smallest entities. If matter were not made of smallest entities, there would be no way to realize

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Challenge 4 e

Challenge 5 e

#### **1 MOTION FOR ENJOYING LIFE**



FIGURE 3 A quantum machine (© Elmar Bartel).

reproduction. The observation of reproduction thus implies the existence of atoms and the necessity of quantum theory! Indeed, without the quantum of action there would be no DNA molecules and there would be no way to inherit our own properties – our own construction plan – to children.

Passing on a plan from generation to generation requires that living beings have ways to store information. Living beings must have some built-in memory storage. We know already that a system with memory must be made of *many* particles: there is no other way to store information and secure its stability over time. The large number of particles is necessary to protect the information from the influences of the outside world.

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Our own construction plan is stored in DNA molecules in the nucleus and the mitochondria of each of the millions of cells inside our body. We will explore some details below. The plan is thus indeed stored and secured with the help of *many* particles. Therefore, reproduction is first of all a transfer of parent's DNA to the next generation. The transfer is an example of motion. It turns out that this and all other examples of motion in our bodies occur in the same way, namely with the help of molecular machines.

#### QUANTUM MACHINES

Living beings move. In order to reproduce, living beings must be able to move in selfdirected ways.

▷ A system able to perform self-directed motion is called a *machine*.

All self-reproducing beings, such as the one of Figure 3, are thus machines. Even machines that do not grow still need fuel, and thus need a metabolism. All machines, living or not, are based on quantum effects.

How do living machines work? From a fundamental physics point of view, we need only a few sections of our walk so far to describe them: we need QED and sometimes universal gravity. Simply stated, life is an electromagnetic process taking place in weak gravity.\* But the details of this statement are tricky and interesting.

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<sup>\*</sup> In fact, also the nuclear interactions play some role for life: cosmic radiation is one source for random

MOTION TYPE	EXAMPLES	INVOLVED MOTORS
Growth	collective molecular processes in cell growth, cell shape change, cell motility	linear molecular motors, ion pumps
	gene turn-on and turn-off	linear molecular motors
	ageing	linear molecular motors
Construction	material transport (polysaccharides, lipids, proteins, nucleic acids, others)	muscles, linear molecular motors
	forces and interactions between biomolecules and cells	pumps in cell membranes
Functioning	metabolism (respiration, digestion)	muscles, ATP synthase, ion pumps
	muscle working	linear molecular motors, ion pumps
	thermodynamics of whole living system and of its parts	muscles
	nerve signalling	ion motion, ion pumps
	brain working, thinking	ion motion, ion pumps
	memory: long-term potentiation	chemical pumps
	memory: synapse growth	linear molecular motors
	hormone production	chemical pumps
	illnesses	cell motility, chemical pumps
	viral infection of a cell	rotational molecular motors for RNA transport
Defence	the immune system	cell motility, linear molecular motors
	blood clotting	chemical pumps
	bronchial cleaning	cilial motors
Sensing	eye	chemical pumps, ion pumps
	ear	hair motion sensors, ion pumps, rotary molecular motors
	smell	ion pumps
	touch	ion pumps
Reproduction	information storage and retrieval	linear and rotational molecular motors inside nuclei
	cell division, organelle motion	linear molecular motors, polymerase
	sperm motion	linear molecular motors
	courting, using brain and muscles	linear molecular motors, ion pumps

 TABLE 1 Motion and molecular machines found in living beings.

We can say that *living beings are systems that move against their environment faster than molecules do.* Observation shows that living systems move faster the bigger they are. Observation also shows that living beings achieve this speed by making use of a huge number of tiny machines, often made of one or only a few molecules, that work together. These machines realize the numerous processes that are part of life.

An overview of processes taking place in living beings is given in Table 1. Above all, the table shows that the processes are due to *molecular machines*.

▷ A living being is a collection of a huge number of specialized molecular machines.

Molecular machines are among the most fascinating devices found in nature. Table 1 also shows that nature only needs a few such devices to realize all the motion types used by humans and by all other living beings: *molecular pumps* and *molecular motors*. Given the long time that living systems have been around, these devices are extremely efficient. They are found in every cell, including those of Figure 5. The specialized molecular machines in living beings are ion pumps, chemical pumps and rotational and linear molecular motors. Ion and chemical pumps are found *in* membranes and transport matter *across* membranes. Rotational and linear motors move structures *against* membranes.

Ref. 3 *across* membranes. Rotational and linear motors move structures *against* membranes. Even though there is still a lot to be learned about molecular machines, the little that is known is already spectacular enough.

#### How do we move? - Molecular motors

How do our muscles work? What is the underlying motor? One of the beautiful results of modern biology is the elucidation of this issue.

▷ *Muscles* work because they contain molecules which change shape when supplied with energy.

This shape change is *repeatable*. A clever combination and repetition of these molecular shape changes is then used to generate macroscopic motion.

▷ Each shape-changing molecule is a molecular motor.

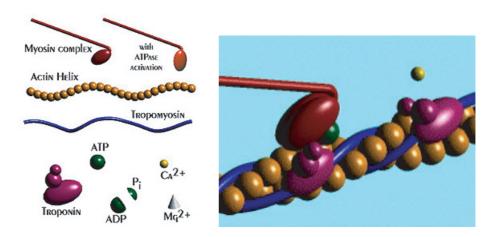
There are three basic classes of molecular motors in nature: linear motors, rotational motors and pumps.

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mutations, which are so important in evolution. Plant growers often use radioactive sources to increase Ref. 1 mutation rates. Radioactivity can also terminate life or be of use in medicine.

The nuclear interactions are also implicitly involved in life in several other ways. The nuclear interactions were necessary to form the atoms – carbon, oxygen, etc. – required for life. Nuclear interactions are behind the main mechanism for the burning of the Sun, which provides the energy for plants, for humans and for all other living beings (except a few bacteria in inaccessible places).

Summing up, the nuclear interactions occasionally play a role in the appearance and in the destruction of life; but they usually play no role for the actions or functioning of particular living beings.



**FIGURE 4** Left: myosin and actin are the two protein molecules that realize the most important linear molecular motor in living beings, including the motion in muscles. Right: the resulting motion step is 5.5 nm long; it has been slowed down by about a factor of ten (image and QuickTime film © San Diego State University, Jeff Sale and Roger Sabbadini).

1. *Linear molecular motors* are at the basis of muscle motion; an example is given in Figure 4. Other linear motors separate genes during cell division. Linear motors also move organelles inside cells and displace cells through the body during embryo growth, when wounds heal, and in all other cases of cell motility. Also assembler molecules, for example those that replicate DNA, can be seen as linear motors.

Challenge 6 s

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Ref. 5

Ref. 4

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A typical molecular motor consumes around 100 to 1000 ATP molecules per second, thus about 10 to 100 aW. The numbers are small; there are more astonishing if we take into account that the power due to the white noise of the surrounding water is 10 nW. In other words, in every molecular motor, the power of the environmental noise is eight to nine orders of magnitude higher than the power consumed by the motor! The ratio shows what a fantastic piece of machinery such a molecular motor is. At our scale, this would correspond to a car that drives, all the time, through an ongoing storm and earthquake.

2. We encountered *rotational motors* already earlier on; nature uses them to rotate the cilia of many bacteria as well as sperm tails. Researchers have also discovered that evolution produced molecular motors which turn around DNA helices like a motorized bolt would turn around a screw. Such motors are attached at the end of some viruses and insert the DNA into virus bodies when they are being built by infected cells, or extract the DNA from the virus after it has infected a cell. The most important rotational motor, and the smallest known so far – 10 nm across and 8 nm high – is ATP synthase, a protein that synthesizes most ATP in cells.

3. *Molecular pumps* are equally essential to life. They pump chemicals, such as ions or specific molecules, into every cell or out of it, using energy. They do so even if the concentration gradient tries to do the opposite. Molecular pumps are thus essential in ensuring that life is a process *far* from equilibrium. Malfunctioning molecular pumps are responsible for many health problems, for example for the water loss in cholera infection.

In the following, we explore a few specific molecular motors found in cells. How mo-Ref. 6 lecules produce movement in linear motors was uncovered during the 1980s. The results



FIGURE 5 A sea urchin egg surrounded by sperm, or molecular motors in action: molecular motors make sperm move, make fecundation happen, and make cell division occur (photo by Kristina Yu, © Exploratorium www.exploratorium.edu).

started a wave of research on all other molecular motors found in nature. The research showed that molecular motors differ from most everyday motors: molecular motors do *not* involve temperature gradients, as car engines do, they do *not* involve electrical currents, as electrical motors do, and they do *not* rely on concentration gradients, as chemically induced motion, such as the rising of a cake, does.

#### LINEAR MOLECULAR MOTORS

Ref. 6

The central element of the most important linear molecular motor is a combination of two protein molecules, namely myosin and actin. Myosin changes between two shapes and literally *walks* along actin. It moves in regular small steps, as shown in Figure 4. The motion step size has been measured, with the help of some beautiful experiments, to always be an integer multiple of 5.5 nm. A step, usually forward, but sometimes backwards, results whenever an ATP (adenosine triphosphate) molecule, the standard biological fuel, hydrolyses to ADP (adenosine diphosphate) and releases the energy contained in the chemical bond. The force generated is about 3 to 4 pN; the steps can be repeated several times a second. Muscle motion is the result of thousand of millions of such elementary steps taking place in concert.

Why does this molecular motor work? The molecular motor is so small that the noise due to the Brownian motion of the molecules of the liquid around it is extremely intense. Indeed, the transformation of disordered molecular motion into ordered macroscopic

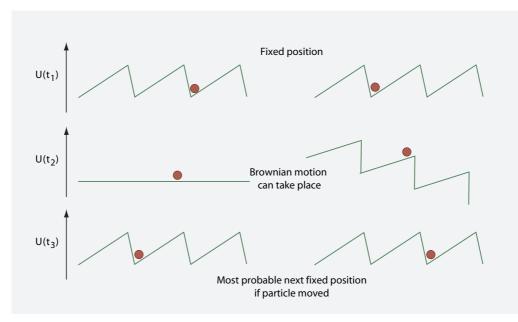


FIGURE 6 Two types of Brownian motors: switching potential (left) and tilting potential (right).

motion is one of the great wonders of nature.

Ref. 7

Challenge 7 e

Evolution is smart: with three tricks it takes advantage of Brownian motion and transforms it into macroscopic motion. (Molecular motors are therefore also called *Brownian motors*.) The first trick of evolution is the use of an asymmetric, but periodic potential, a so-called *ratchet*.\* The second trick of evolution is a temporal variation of the potential of the ratchet, together with an energy input to make it happen. The two most important realizations are shown in Figure 6. Molecular motors thus work away from thermal equilibrium. The third trick is to take a large number of these molecular motors and to add their effects.

The periodic potential variation in a molecular motor ensures that for a short, recurring time interval the free Brownian motion of the moving molecule – typically  $1 \mu m/s$  – affects its position. Subsequently, the molecule is fixed again. In most of the short time intervals of free Brownian motion, the position will not change. But if the position does change, the intrinsic asymmetry of the ratchet shape ensures that with high probability the molecule advances in the preferred direction. (The animation of Figure 4 lacks this irregularity.) Then the molecule is fixed again, waiting for the next potential change. On average, the myosin molecule will thus move in one direction. Nowadays the motion of single molecules can be followed in special experimental set-ups. These experiments confirm that muscles use such a ratchet mechanism. The ATP molecule adds energy to the system and triggers the potential variation through the shape change it induces in the myosin molecule. Nature then takes millions of these ratchets together: that is how our muscles work.

Engineering and evolution took different choices. A moped contains one motor. An expensive car contains about 100 motors. A human contains at least 10<sup>16</sup> motors.

<sup>\*</sup> It was named after Ratchet Gearloose, the famous inventor from Duckburg.



FIGURE 7 A classical ratchet, here of the piezoelectric kind, moves like a linear molecular motor (© PiezoMotor).

Another well-studied linear molecular motor is the kinesin–microtubule system that carries organelles from one place to the other within a cell. Like in the previous example, also in this case chemical energy is converted into unidirectional motion. Researchers were able to attach small silica beads to single molecules and to follow their motion. Using laser beams, they could even apply forces to these single molecules. Kinesin was found to move with around 800 nm/s, in steps lengths which are multiples of 8 nm, using one ATP molecule at a time, and exerting a force of about 6 pN.

Quantum ratchet motors do not exist only in living systems; they also exist as humanbuilt systems. Examples are electrical ratchets that move single electrons and optical ratchets that drive small particles. These applications are pursued in various experimental research programmes.

Also *classical* ratchets exist. One example is found in every mechanical clock; also many ballpoint pens contain one. Another example of ratchet with asymmetric of mechanical steps uses the Leidenfrost effect to rapidly move liquid droplets, as shown in the video www.thisiscolossal.com/2014/03/water-maze. A further example is shown in Figure 7; indeed, many piezoelectric actuators work as ratchets and the internet is full of videos that show how they work. Piezoelectric ratchets, also called *ultrasound motors*, are found in precision stages for probe motion and inside certain automatic zoom objectives in expensive photographic cameras. Also many atomic force microscopes and scanning electron microscopes use ratchet actuators.

Molecular motors are essential for the growth and the working of nerves and the **Ref. 8** brain. A nerve contains large numbers of dozens of molecular motors types from all three main families: dynein, myosin and kinesin. These motors transport chemicals, called 'cargos', along axons and all have loading and unloading mechanisms at their ends. They are necessary to realize the growth of nerves, for example from the spine to the tip of the toes. Other motors control the growth of synapses, and thus ensure that we have long-term memory. Malfunctioning molecular motors are responsible for Alzheimer disease, Huntington disease, multiple sclerosis, certain cancers and many other diseases due either to genetic defects or to environmental poisons.

In short, without molecular motors, we could neither move nor think.

#### A rotational molecular motor: ATP synthase

In cells, the usual fuel for most chemical reactions is adenosine triphosphate, or ATP. In plants, most ATP is produced on the membranes of cell organelles called *chloroplasts*, and in animal cells, in the so-called *mitochondria*. These are the power plants in most cells. ATP also powers most bacteria. It turns out that ATP is synthesized by a protein

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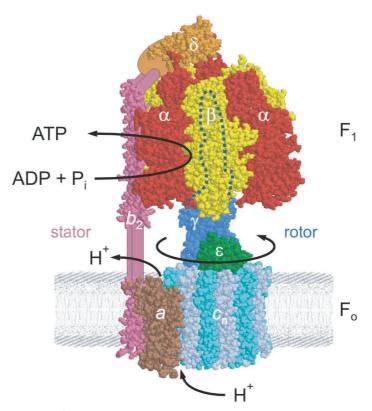


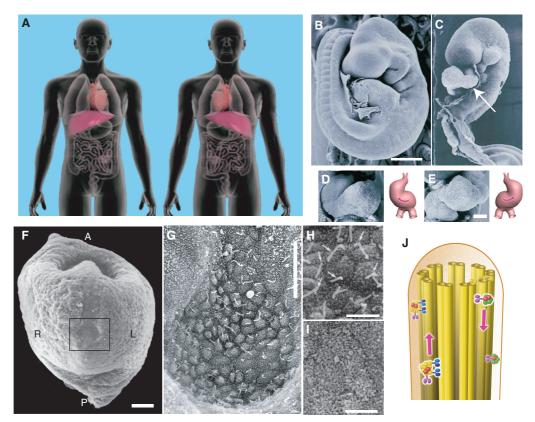
FIGURE 8 The structure of ATP synthase (© Joachim Weber).

Ref. 9

located in membranes. The protein is itself powered by protons,  $H^+$ , which form the basic fuel of the human body, whereas ATP is the high-level fuel. For example, most other molecular motors are powered by ATP. ATP releases its energy by being changed into to adenosine diphosphate, or ADP. The importance of ATP is simple to illustrate: every human synthesizes, during a typical day, an amount of ATP that is roughly equal to his or her body mass.

The protein that synthesizes ATP is simply called *ATP synthase*. In fact, ATP synthase differs slightly from organism to organism; however, the differences are so small that they can be neglected in most cases. (An important variation are those pumps where Na<sup>+</sup> ions replace protons.) Even though ATP synthase is a highly complex protein, its function it easy to describe: it works like a *paddle wheel* that is powered by a proton gradient across the membrane. Figure 8 gives an illustration of the structure and the process. The research that led to these discoveries was rewarded with the 1997 Nobel Prize in Chemistry.

In fact, ATP synthase also works in the reverse: if there is a large ATP gradient, it pumps protons out of the cell. In short, ATP synthase is a rotational motor and molecular pump at the same time. It resembles the electric starter motor, powered by the battery, found in the older cars; in those cars, during driving, the electric motor worked as a dynamo charging the battery. (The internet also contains animations of the rotation of ATP synthase.) ATP

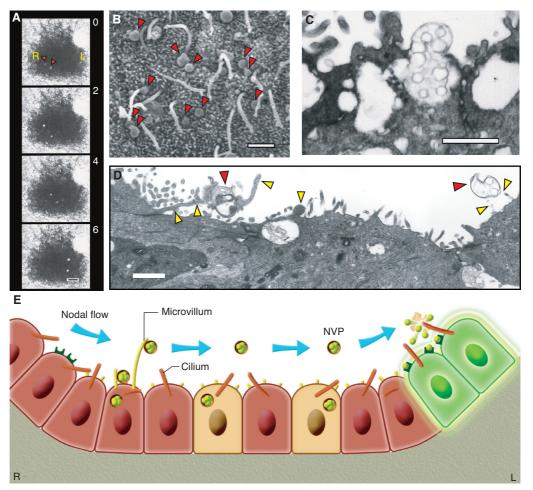


**FIGURE 9** A: The asymmetric arrangement of internal organs in the human body: Normal arrangement, situs solitus, as common in most humans, and the mirrored arrangement, situs inversus. Images B to E are scanning electron micrographs of mouse embryos. B: Healthy embryos at this stage already show a right-sided tail. C: In contrast, mutant embryos with defective cilial motors remain unturned, and the heart loop is inverted, as shown by the arrow. D: Higher-magnification images and schematic representations of a normal heart loop. E: Similar image showing an inverted loop in a mutant embryo. Images F to I are scanning electron micrographs of a mouse node. F: A low-magnification view of a 7.5 day-old mouse embryo observed from the ventral side, with the black rectangle indicating the node. The orientation is indicated with the letters A for anterior, P for posterior, L for left and R for right; the scale bar is 100 µm. G: A higher-magnification image of the mouse node; the scale bar is 20 µm. H: A still higher-magnification view of healthy nodal cilia, indicated by arrows, and of the nodal pit cells; the scale bar is 5 µm. I: The nodal pit cells of mutant embryos lacking cilia. J: Illustration of the molecular transport inside a healthy flagellum (© Hirokawa Nobutaka).

synthase has been studied in great detail. For example, it is known that it produces three ATP molecules per rotation, that it produces a torque of around  $20kT/2\pi$ , where kT is the kinetic energy of a molecule at temperature *T*. There are at least  $10^{16}$  such motors in an adult body. The ATP synthase paddle wheel is one of the central building blocks of life.

#### ROTATIONAL MOTORS AND PARITY BREAKING

Why is our heart on the left side and our liver on the right side? The answer of this old question is known only since a few years. The left-right asymmetry, or chirality, of human bodies must be connected to the chirality of the molecules that make up life. In all living



**FIGURE 10** A: Optical microscope images of flowing nodal vesicular parcels (NVPs). L and R indicate the orientation. The NVPs, indicated by arrowheads, are transported to the left side by the nodal flow. The scale bar is 10  $\mu$ m. B: A scanning electron micrograph of the ventral surface of nodal pit cells. The red arrowheads indicate NVP precursors. The scale bar is 2  $\mu$ m. C and D: Transmission electron micrographs of nodal pit cells. The scale bar is 1  $\mu$ m. E: A schematic illustration of NVP flow induced by the cilia. The NVPs are released from dynamic microvilli, are transported to the left side by the nodal flow due to the cilia, and finally are fragmented with the aid of cilia at the left periphery of the node. The green halos indicate high calcium concentration – a sign of cell activation that subsequently starts organ formation (© Hirokawa Nobutaka).

beings, sugars, proteins and DNS/DNA are chiral molecules, and in all living beings, only one of the two molecular mirror types is actually used. But how does nature translate the chirality of molecules into the chirality of a body? The answer was deduced only recently by Hirokawa Nobutaka and his team; and surprisingly, rotational molecular motors are the key to the puzzle.

Ref. 10

The position of the internal organs is fixed during the early development of the embryo. At an early stage, a central part of the embryo, the so-called *node*, is covered with rotational cilia, i.e., rotating little hairs. They are shown in Figure 9. In fact, all vertebrates have a node at some stage of embryo development. The nodal cilia are powered by a molecular motor; they all rotate in the *same* (clockwise) direction about ten times per second. The rotation direction is a consequence of the chirality of the molecules that are contained in the motors. However, since the cilia are inclined with respect to the surface – towards the tail end of the embryo – the rotating cilia effectively move the fluid above the node towards the left body side of the embryo. The fluid of this newly discovered *nodal flow* contains substances – nodal vesicular parcels – that accumulate on the left side of the node and subsequently trigger processes that determine the position of the heart. If the cilia do not rotate due to a genetic defect, or if the flow is reversed by external means, the heart and other organs get misplaced. This connection also explains all the other consequences of such genetic defects or interventions.

In other words, through the rotation of the cilia and the mentioned mechanism, the chirality of molecules is mapped to the chirality of the whole vertebrate organism. It might even be that similar processes occur also elsewhere in nature, for example in the development of the brain asymmetry. This is still a field of intense research. In summary, molecular motors are truly central to our well-being and life.

#### CURIOSITIES AND FUN CHALLENGES ABOUT BIOLOGY

Una pelliccia è una pelle che ha cambiato bestia.\* Girolamo Borgogelli Avveduti

With modern microscopic methods it is possible to film, in all three dimensions, the evolution of the eye of a fruit fly until it walks away as a larva. Such a film allows to follow every single cell that occurs during the 20 hours: the film shows how cells move around during development and show every single cell division. Watch this amazing film, taken at the EMBL in Heidelberg, at youtu.be/MefTPoeVQ3w.

\* \*

Biological evolution can be summarized in three principles:

- 1. All living beings are different also in a species.
- 2. All living beings have a tough life due to competition.
- 3. Living beings with an advantage will survive and reproduce.

The last principle is often called the 'survival of the fittest'. As a result of these three principles, with each generation, *species and living beings can change*. The result of accumulated generational change is called *biological evolution*. In particular, these three principles explain the change from unicellular to multicellular life, from fish to land animals, and from animals to people.

Quantum effects are fundamental in all three principles of evolution. Of course, life and metabolism are quantum effects. The differences mentioned in the first principle are due to quantum physics: perfect copies of macroscopic systems are impossible. The second principle mentions competition; that is a kind of measurement, which, as we saw, is only possible due to the existence of a quantum of action. The third principle mentions

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<sup>\* &#</sup>x27;A fur is a skin that has changed beast.'

reproduction: that is again a quantum effect, based on the copying of genes, which are quantum structures. In short, biological evolution is a process due to the quantum of Page 19 action. How would you determine which of two identical twins is the father of a baby? Challenge 8 d Can you give at least five arguments to show that a human clone, if there will ever be one, is a completely different person than the original? Challenge 9 s It is well known that the first ever cloned cat, *copycat*, born in 2002, looked completely different from the 'original' (in fact, its mother). The fur colour and its patch pattern were completely different from that of the mother. Analogously, identical human twins have different finger prints, iris scans, blood vessel networks and intrauterine experiences, among others. Many properties of a mammal are not determined by genes, but by the environment of the pregnancy, in particular by the womb and the birth experience. Womb influences include fur patches, skin fold shapes, but also character traits. The influence of the birth experience on the character is well-known and has been studied by many psychologists. Discuss the following argument: If nature were classical instead of quantum, there would not be just *two* sexes – nor any other *discrete* number of them, as in some lower animals - but there would be a *continuous range* of them. In a sense, there would be an infinite number of sexes. True? Challenge 10 s \* \* Here is a well-known unanswered question on evolution: how did the first kefir grains form? Kefir grains produce the kefir drink when covered with milk for about 8 to 12 hours. The grains consist of a balanced mixture of about 40 types of bacteria and yeasts. All kefir grains in the world are related. But how did the first ones form, about 1000 years Challenge 11 r ago? \* \* Molecular motors are quite capable. The molecular motors in the sooty shearwater (Puffinus griseus), a 45 cm long bird, allow it to fly 74 000 km in a year, with a measured record of 1094 km a day. \* \*

When the ciliary motors that clear the nose are overwhelmed and cannot work any more, they send a distress signal. When enough such signals are sent, the human body triggers the sneezing reaction. The sneeze is a reaction to blocked molecular motors.

The growth of human embryos is one of the wonders of the world. The website embryo. soad.umich.edu provides extensive data, photos, animations and magnetic resonance

images on the growth process.

Challenge 12 s	Do	birds	have	а	navel?	
challenge 12 S	$D_{0}$	Unus	nave	a	maycri	

Ref. 13

Ref. 15

All animals with the possibility of regenerating themselves from a small piece, such as *Planaria*, reproduce asexually, by dividing. All animals that reproduce sexually are unable to regenerating the whole animal from a small part.

\* \*

Challenge 13 s All animals that move with limbs are left-right symmetric. Why?

Many molecules found in living beings, such as sugar, have mirror molecules. However, in all living beings only one of the two sorts is found. Life is intrinsically asymmetric. Challenge 14 s How can this be?

\*

\* \*

\* \*

How is it possible that the genetic difference between man and chimpanzee is regularly given as about 1 %, whereas the difference between man and woman is one chromosome in 46, in other words, about 2.2 %?

What is the longest time a single bacterium has survived? It is more than the 5000 years of the bacteria found in Egyptian mummies. For many years, the survival time was estimated to lie at over 25 million years, a value claimed for the bacteria spores resurrected from the intestines in insects enclosed in amber. Then it was claimed to lie at over 250 million years, the time estimated that certain bacteria discovered in the 1960s by Heinz Dombrowski in (low-radioactivity) salt deposits in Fulda, in Germany, have hibernated there before being brought back to life in the laboratory. A similar result has been recently claimed by the discovery of another bacterium in a North-American salt deposit
Ref. 12

However, these values are now disputed, as DNA sequencing has shown that these bacteria were probably due to sample contamination in the laboratory, and were not part of the original sample. So the question of the longest survival time of bacteria is still open.

\*

In 1967, a TV camera was deposited on the Moon. Unknown to everybody, it contained a small patch of *Streptococcus mitis*. Three years later, the camera was brought back to Earth. The bacteria were still alive. They had survived for three years without food, water or air. Life can be resilient indeed. This widely quoted story is so unbelievable that it was checked again in 2011. The conclusion: the story is false; the bacteria were added by mistake in the laboratory after the return of the camera.

\* \*

ure of Dhusins - convrints @ Christoph Schiller lune 1990.-May 2020 - free ndf file available at www.motionmountain.net

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LIFE GROUP	DESCRIBED SPECIE	es Estimated	SPECIES
		MIN.	MAX.
Viruses	$4\cdot 10^3$	$50 \cdot 10^3$	$1 \cdot 10^6$
Prokaryotes ('bacteria')	$4\cdot 10^3$	$50 \cdot 10^3$	$3\cdot 10^6$
Fungi	$72 \cdot 10^3$	$200 \cdot 10^3$	$2.7\cdot 10^6$
Protozoa	$40\cdot 10^3$	$60 \cdot 10^3$	$200\cdot 10^3$
Algae	$40 \cdot 10^3$	$150 \cdot 10^3$	$1\cdot 10^6$
Plants	$270 \cdot 10^3$	$300 \cdot 10^3$	$500 \cdot 10^3$
Nematodes	$25 \cdot 10^3$	$100 \cdot 10^3$	$1\cdot 10^6$
Crustaceans	$40 \cdot 10^3$	$75 \cdot 10^3$	$200 \cdot 10^3$
Arachnids	$75 \cdot 10^3$	$300 \cdot 10^3$	$1\cdot 10^6$
Insects	$950\cdot 10^3$	$2\cdot 10^6$	$100\cdot 10^6$
Molluscs	$70 \cdot 10^3$	$100 \cdot 10^3$	$200\cdot 10^3$
Vertebrates	$45 \cdot 10^3$	$50 \cdot 10^3$	$55 \cdot 10^3$
Others	$115 \cdot 10^3$	$200 \cdot 10^3$	$800 \cdot 10^3$
Total	$1.75 \cdot 10^6$	$3.6 \cdot 10^{6}$	$112 \cdot 10^6$

 TABLE 2 Approximate numbers of living species.

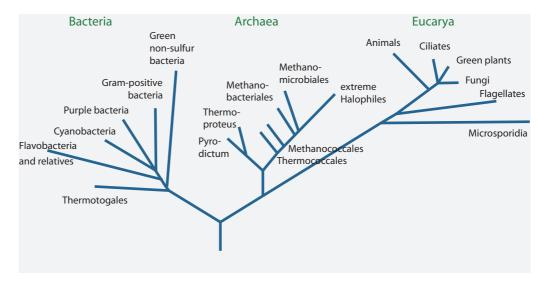


FIGURE 11 A modern version of the evolutionary tree.

Ref. 16

In biology, classifications are extremely useful. (This is similar to the situation in astrophysics, but in full contrast to the situation in physics.) Table 2 gives an overview of the magnitude of the task. This wealth of material can be summarized in one graph, shown in Figure 11. Newer research seems to suggest some slight changes to the picture. So far however, there still is only a single root to the tree.

\* \*

Muscles produce motion through electrical stimulation. Can technical systems do the same? Candidate are appearing: so-called *electroactive polymers* change shape when they are activated with electrical current or with chemicals. They are lightweight, quiet and simple to manufacture. However, the first arm wrestling contest between human and artificial muscles, held in 2005, was won by a teenage girl. The race to do better is ongoing.

Life is not a clearly defined concept. The definition used above, the ability to self-reproduce, has its limits. Can it be applied to old animals, to a hand cut off by mistake, to sperm, to ovules or to the first embryonal stages of a mammal? The definition of life also gives problems when trying to apply it to single cells. Can you find a better definition? Is the definition of living beings as 'what is made of cells' useful?

Challenge 16 e

Every example of growth is a type of motion. Some examples are extremely complex. Take the growth of acne. It requires a lack of zinc, a weak immune system, several bacteria, as well as the help of *Demodex brevis*, a mite (a small insect) that lives in skin pores. With a size of 0.3 mm, somewhat smaller than the full stop at the end of this sentence, this and other animals living on the human face can be observed with the help of a strong magnifying glass.

\*

Humans have many living beings on board. For example, humans need bacteria to live. It is estimated that 90 % of the bacteria in the human mouth alone are not known yet; only about 1000 species have been isolated so far.

\* \*

Ref 17

Bacteria are essential for our life: they help us to digest and they defend us against illnesses due to dangerous bacteria. In fact, the number of bacteria in a human body is estimated to be  $3.8(2.0) * 10^{13}$ , more than 99 % of which are in the gut. The number of cells in a adult, average human body is estimated to be  $3.0(0.3) * 10^{13}$  – of which 70 to 85 % are red blood cells. In short, a human body contains more bacteria than own cells! Nevertheless, the combined mass of all bacteria in a human body is estimated to be only around 0.2 kg, because gut bacteria are much smaller than human cells.

Of the around 100 groups of bacteria in nature, the human body mainly contains species from four of them: actinobacteria, bacteroidetes, firmicutes and proteobacteria. They play a role in obesity, malnutrition, heart disease, diabetes, multiple sclerosis, autism and many other conditions. These connections are an important domain of present research.

\* \*

How do trees grow? When a tree – biologically speaking, a *monopodal phanerophyte* – grows and produces leaves, between 40 % and 60 % of the mass it consists of, namely the water and the minerals, has to be lifted upwards from the ground. (The rest of the mass comes from the  $CO_2$  in the air.) How does this happen? The materials are pulled upwards by the water columns inside the tree; the pull is due to the negative pressure that is created when the top of the column evaporates. This is called the *transpiration-cohesion-tension* 

*model.* (This summary is the result of many experiments.) In other words, no energy is needed for the tree to pump its materials upwards.

Trees do not need energy to transport water. As a consequence, a tree grows purely by adding material to its surface. This implies that when a tree grows, a branch that is formed at a given height is also found at that *same* height during the rest of the life of that tree. Just check this observation with the trees in your garden.

Challenge 17 e

Challenge 18 d Mammals have a narrow operating temperature. In contrast to machines, humans function only if the internal temperature is within a narrow range. Why? And does this requirement also apply to extraterrestrials – provided they exist?

Challenge 19 r How did the first cell arise? This important question is still open. As a possible step towards the answer, researchers have found several substances that spontaneously form closed membranes in water. Such substances also form foams. It might well be that life formed in foam. Other options discussed are that life formed underwater, at the places where magma rises into the ocean. Elucidating the origins of cells is one of the great open riddles of biology – though the answer will not be of much use.

\* \*

\* \*

Challenge 20 s Could life have arrived to Earth from outer space?

Is there life elsewhere in the universe? The answer is clear. First of all, there *might* be life elsewhere, though the probability is extremely small, due to the long times involved and the requirements for a stable stellar system, a stable planetary system, and a stable geological system. In addition, so far, all statements that claim to have detected an example were *lies*. Not mistakes, but actual lies. The fantasy of extraterrestrial life poses an interesting challenge to everybody: Why would an extraterrestrial being be of interest to you? If you can answer, realize the motivation in some other way, *now*, without waiting. If you cannot answer, do something else.

Challenge 21 e

What could *holistic medicine* mean to a scientist, i.e., avoiding nonsense and false beliefs? Holistic medicine means treating illness with view on the whole person. That translates to four domains:

- *physical* support, to aid mechanical or thermal healing processes in the body;
- *chemical* support, with nutrients or vitamins;
- *signalling* support, with electrical or chemical means, to support the signalling system of the body;
- *psychological* support, to help all above processes.

When all theses aspects are taken care of, healing is as rapid and complete as possible. However, one main rule remains: *medicus curat, natura sanat.*\*

<sup>\* &#</sup>x27;The physician helps, but nature heals.'

Life is, above all, beautiful. For example, the book by CLAIRE NOUVIAN, *The Deep: The Extraordinary Creatures of the Abyss*, presented at www.press.uchicago.edu/books/nouvian/index.html allows one to savour the beauty of life deep in the ocean.

\* \*

What are the effects of *environmental pollution* on life? Answering this question is an intense field of modern research. Here are some famous stories.

- Herbicides and many genetically altered organisms kill bees. For this reason, bees are dying (since 2007) in the United States; as a result, many crops such as almonds and oranges are endangered there. In countries where the worst herbicides and genetically modified crops have been banned, bees have no problems. An example is France, where the lack of bees posed a threat to the wine industry.
- Chemical pollution leads to malformed babies. In mainland China, one out of 16 children is malformed for this reason (in 2007). In Japan, malformations have been much reduced though not completely since strict anti-pollution laws have been passed.
- Radioactive pollution kills. In Russia, the famous Lake Karachay had to be partly filled with concrete because its high radioactivity killed anybody that walked along it for an hour.
- Smoking kills though slowly. Countries that have lower smoking rates or that have curbed smoking have reduced rates for cancer and several other illnesses.
- Eating tuna is dangerous for your health, because of the heavy metals it contains.
- Cork trees are disappearing. The wine industry has started large research programs to cope with this problem.
- Even arctic and antarctic animals have livers full of human-produced chemical poisons.
- Burning fossil fuels raises the CO<sub>2</sub> level of the atmosphere. This leads to many effects for the Earth's climate, including a slow rise of average temperature and sea level.

Ecological research is uncovering many additional connections. Let us hope that the awareness for these issues increases across the world.

Some researchers prefer to define living beings as *self-reproducing* systems, others prefer to define them as *metabolic* systems. Among the latter, Mike Russell and Eric Smith propose the following definition of life: '*The purpose of life is to hydrogenate carbon dioxide.*' In other terms, the aim of life is to realize the reaction

$$CO_2 + 4H_2 \to CH_4 + 2H_2O$$
. (1)

This beautifully dry description is worth pondering – and numerous researchers are indeed exploring the consequences of this view.

\* \*

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Not only is death a quantum process, also aging is one. Research in the details of this vast field is ongoing. A beautiful example is the loss of leaves in autumn. The loss is triggered by ethene, a simple gas. You can trigger leave loss yourself, for example by putting cut apples – a strong source of ethene – together with a rose branch in a plastic bag: the roses will lose their leaves.

\* \*

The reanimation of somebody whose heart and breathing stopped is an useful movement sequence, called *cardiopulmonary resuscitation*. Do learn it.

New research has shown that motion is important to staying healthy. In particular, it is important to do sports, but it is even more important to reduce the time of being seated. People who sit many hours per day have increased risk to get diabetes, breast cancer, white mass reduction in the brain, dementia, and various other diseases. Research into the dangerous effects of sitting is still in its infancy. For example, research has shown that sitting in front of a tv, in front of a PC or in a car for many hours a day *cannot* be compensated by doing sport.

\* \*

To stay fit and to ensure that you feel fit, enjoy life and enjoy the books by Mark Verstegen.

\* \*

Which species of living being is the most successful, if we measure success as the species' biomass? This simple question has no known answer. Among animals, cattle (*Bos taurus*), humans (*Homo sapiens*) and Antarctic krill (*Euphasia superba*) have similar biomass values, but it is not clear whether these are the highest values. No good data seem to exist for plants – except for crops. It is almost sure that several species of bacteria, such as from the marine genus *Prochlorococcus* or some other bacteria species found in soil, and several species of fungi achieve much higher biomass values. But no reliable overview is available.

\*

Trees move in many interesting ways. For example, trees fight with their neighbours over space and access to light and nutrients. This occurs with most vehemence if the neighbour is of another species. Most trees do not like to be touched by other trees – but there are exceptions, such as beeches. For example, when beeches fight with oaks, after a few years, the oak is left with little space and light, and the beech has taken over most of it. But trees also help neighbours, for example in case of sickness, by providing nutrients and water. Many more fascinating stories about trees – including the way the communicate via aiborne chemical signals such as ethylene (ethene) – are told by PETER WOHLLEBEN, *Das geheime Leben der Bäume: Was sie fühlen, wie sie kommunizieren – die Entdeckung einer verborgenen Welt*, Ludwig Verlag, 2015.

\* \*

Trees sleep at night and get up in the morning. The observation is known since centur-

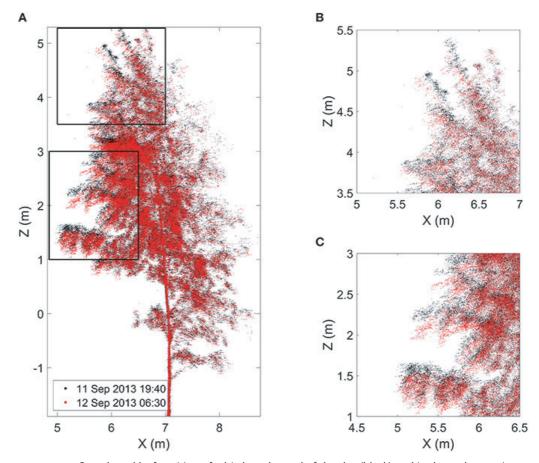


FIGURE 12 Branch and leaf position of a birch at the end of the day (black) and in the early morning (red), with magnified sections shown on the right (© Eetu Puttonen et al.).

ies; a beautiful measurement of the effect, using a laser scanner, was performed by Eetu
Puttonen and his group. Their results, shown in Figure 12, show that the height of a typical birch branch and its leaves in the early morning is up to 10 cm lower than during the day. The measurements also show that the trees move most in the early morning, when they wake up. The origin of these effects seems to be the difference of water intake during day and night.

# THE PHYSICS OF PLEASURE

What is mind but motion in the intellectual sphere? Oscar Wilde, *The Critic as Artist*.

Oscal Wilde, The Critic us Artisi.

Pleasure is a quantum effect. The reason is simple. Pleasure comes from the senses. All senses measure. And all measurements rely on quantum theory.

The human body, like an expensive car, is full of sensors. Evolution has built these

sensors in such a way that they trigger pleasure sensations whenever we do with our body what we are made for. Of course, no researcher will admit that he studies pleasure. Therefore the researcher will say that he or she studies the senses, and that he or she is doing *perception research*. But pleasure and all human sensors exist to let life continue. Pleasure is highest when life is made to continue. In the distant past, the appearance of new sensors in living systems has always had important effects of evolution, for example during the Cambrian explosion.

Research into pleasure and biological sensors is a fascinating field that is still evolving; here we can only have a quick tour of the present knowledge.

The *ear* is so sensitive and at the same time so robust against large signals that the experts are still studying how it works. No known sound sensor can cover an energy range of  $10^{13}$ ; indeed, the detected sound intensities range from  $1 \text{ pW/m}^2$  (some say  $50 \text{ pW/m}^2$ ) to  $10 \text{ W/m}^2$ , the corresponding air pressures vary from  $20 \mu$ Pa to 60 Pa. The lowest intensity that can be heard is that of a 20 W sound source heard at a distance of 10000 km, if no sound is lost in between. Audible sound wavelengths span from 17 m (for 20 Hz) to 17 mm (for 20 kHz). In this range, the ear, with its 16 000 to 20 000 hair cells and 30 000 cochlear neurons, is able to distinguish at least 1500 pitches. But the ear is also able to distinguish nearby frequencies, such as 400 and 401 Hz, using a special pitch sharpening mechanism.

The *eye* is a position dependent photon detector. Each eye contains around 126 million separate detectors on the retina. Their spatial density is the highest possible that makes sense, given the diameter of the lens of the eye. They give the eye a resolving power of 1', or 0.29 mrad, and the capacity to consciously detect down to 60 *incident* photons in 0.15 s, or 4 *absorbed* photons in the same time interval.

Each eye contains 120 million highly sensitive general light intensity detectors, the *rods*. They are responsible for the mentioned high sensitivity. Rods cannot distinguish colours. Before the late twentieth century, human built light sensors with the same sensitivity as rods had to be helium cooled, because technology was not able to build sensors at room temperature that were as sensitive as the human eye.

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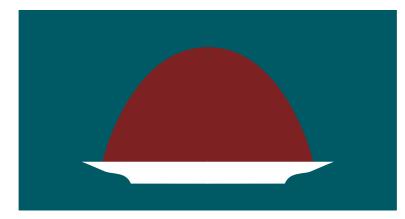
Ref. 19

The human eye contains about 6 million not so sensitive colour detectors, the *cones*, whose distribution we have seen earlier on. The different chemicals in the three cone types (red, green, blue) lead to different sensor speeds; this can be checked with the simple test shown in Figure 13. The sensitivity difference between the colour-detecting cones and the colour-blind rods is the reason that at night all cats are grey.

The images of the eye are only sharp if the eye constantly moves in small random motions. If this motion is stopped, for example with chemicals, the images produced by the eye become unsharp.

The eye also contains about 1 million retinal ganglion cells. All signals from the eye are transmitted through 1 million optical nerve fibres to a brain region, the virtual cortex, that contains over 500 million cells.

Human *touch sensors* are distributed over the skin, with a surface density which varies from one region to the other. The density is lowest on the back and highest in the face and on the tongue. The hand has about 17 000 tactile receptors, most of them at the finger tips. There are separate sensors for light touch (Meissner's corpuscles) and pressure (Merkel cells), for deformation (Ruffini corpuscles), for vibration (Pacinian corpuscles),



## FIGURE 13 The

different speed of the eye's colour sensors, the cones, lead to a strange effect when this picture (in colour version) is shaken right to left in *weak* light.

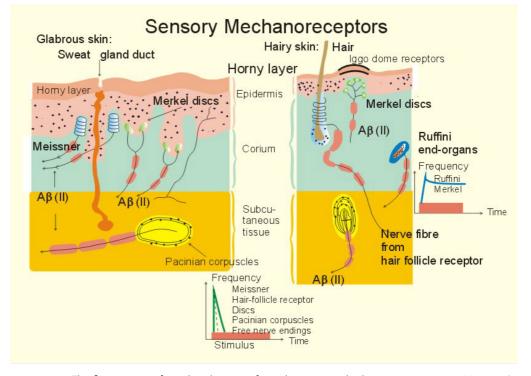


FIGURE 14 The five sensors of touch in humans, from the most to the least common ones: Meissner's corpuscles, Merkel cells, Ruffini corpuscles, Pacinian corpuscles and hair receptors.

and for tickling (unmyelinated fibers); there are additional separate sensors for heat, for coldness,\* and for pain. Some of the sensors, whose general appearance is shown in Figure 14, react proportionally to the stimulus intensity, some differentially, giving signals

<sup>\*</sup> There are *four* sensors for heat; one is triggered above 27°C, one above 31°C, one above 42°C, and one above 52°C. The sensor for temperatures above 42°C, TRPV1, is also triggered by capsaicin, the sharp chemical in chilli peppers.

There seems to be only *one* sensor for coldness, the ion channel TRPM8, triggered between 8 and 26°C. It is also triggered by menthol, a chemical contained in mojito and mint. Coldness neurons, i.e., neurons

only when the stimulus changes. Many of these sensors are also found inside the body – for example on the tongue. The sensors are triggered when external pressure deforms them; this leads to release of  $Na^+$  and  $K^+$  ions through their membranes, which then leads to an electric signal that is sent via nerves to the brain.

The human body also contains *orientation sensors* in the ear, *extension sensors* in each muscle, and *pain sensors* distributed with varying density over the skin and inside the body.

The *taste sensor* mechanisms of tongue are only partially known. The tongue is known to produce six taste signals<sup>\*</sup> – sweet, salty, bitter, sour, proteic and fatty – and the mechanisms are just being unravelled. The sense for proteic, also called *umami*, has been discovered in 1907, by Ikeda Kikunae; the sense for 'fat' has been discovered only in 2005. The tongue, palate and cheeks have about 10 000 taste buds, 90 % of which are on the tongue. Each taste bud has between 50 and 150 receptors; their diameter is around 10  $\mu$ m.

In ancient Greece, Democritus imagined that taste depends on the shape of atoms. Today it is known that sweet taste is connected with certain shape of molecules. Modern research is still unravelling the various taste receptors in the tongue. At least three different sweetness receptors, dozens of bitterness receptors, and one proteic and one fattiness receptor are known. In contrast, the sour and salty taste sensation are known to be due to ion channels. Despite all this knowledge, no sensor with a distinguishing ability of the same degree as the tongue has yet been built by humans. A good taste sensor would have great commercial value for the food industry. Research is also ongoing to find substances to block taste receptors; one aim is to reduce the bitterness of medicines or of food.

The *nose* has about 350 different smell receptors and a total of about 40 million receptor cells. (Dogs have 25 times more.) Through the possible combinations it is estimated that the nose can detect about 10 000 different smells.\*\* Together with the six signals that the sense of taste can produce, the nose also produces a vast range of taste sensations. It protects against chemical poisons, such as smoke, and against biological poisons, such as faecal matter. In contrast, artificial gas sensors exist only for a small range of gases. Good artificial taste and smell sensors would allow checking wine or cheese during their production, thus making their inventor extremely rich. At the moment, humans, with all their technology at their disposal, are not even capable of producing sensors as good as those of a bacterium; it is known that *Escherichia coli* can sense at least 30 substances in its environment.

Vol. III, page 32

Challenge 23 ny

Ref. 20

Other animals feature additional types of sensors. Sharks can *feel electrical fields*. Many snakes have *sensors for infrared light*, such as the pit viper or vampire bats. These sensors are used to locate prey or food sources. Some beetles, such as *Melanophila acuminata*, can also detect infrared; they use this sense to locate the wildfires they need to make

with TRPM8 at their tips, can be seen with special techniques using fluorescence and are known to arrive into the teeth; they provide the sensation you get at the dentist when he applies his compressed air test. \* Taste sensitivity is *not* separated on the tongue into distinct regions; this is an incorrect idea that has been copied from book to book for over a hundred years. You can perform a falsification by yourself, using sugar or salt grains.

Challenge 22 s

<sup>\*\*</sup> Linda Buck and Richard Axel received the 2004 Nobel Prize in Physiology or Medicine for their unravelling of the working of the sense of smell.

their eggs hatch. Also other insects have such organs. Pigeons, trout and sharks can feel magnetic fields, and use this sense for navigation. Many birds and certain insects can see UV light. Bats and dolphins are able to hear ultrasound up to 100 kHz and more. Whales and elephants can detect and localize infrasound signals.

In summary, the sensors with which nature provides us are state of the art; their sensitivity and ease of use is the highest possible. Since all sensors trigger pleasure or help to avoid pain, nature obviously wants us to enjoy life with the most intense pleasure possible. Studying physics is one way to do this.

> C There are two things that make life worth living: Mozart and quantum mechanics. Victor Weisskopf\*

#### THE NERVES AND THE BRAIN

There is no such thing as perpetual tranquillity of mind while we live here; because life itself is but motion, and can never be without desire, nor without fear, no more than without sense. Thomas Hobbes, Leviathan.

The main unit processing all the signals arriving from the sensors, the brain, is essential for all feelings of pleasure. The human brain has the highest complexity of all brains known.\*\* In addition, the processing power and speed of the human brain is still larger than any device build by man.

We saw already earlier on how electrical signals from the sensors are transported into the brain. In the brain itself, the arriving signals are *classified* and *stored*, sometimes for a short time, sometimes for a long time. Most storage mechanisms take place in the structure and the connection strength between brain cells, the *synapses*, as we have seen. The process remaining to understand is the classification, a process we usually call *thinking*. For certain low level classifications, such as geometrical shapes for the eye or sound harmonies for the ear, the mechanisms are known. But for high-level classifications, such as the ones used in conceptual thinking, the aim is not yet achieved. It is not yet known how to describe the processes of reading or understanding in terms of signal motions. Research is still in full swing and will probably remain so for a large part of the twentyfirst century.

In the following we look at a few abilities of our brain, of our body and of other bodies that are important for the types of pleasure that we experience when we study motion.

Vol. I, page 325

Ref. 21

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<sup>\*</sup> Victor Friedrich Weisskopf (b. 1908 Vienna, d. 2002 Cambridge), acclaimed theoretical physicist who worked with Einstein, Born, Bohr, Schrödinger and Pauli. He catalysed the development of quantum electrodynamics and nuclear physics. He worked on the Manhattan project but later in life intensely campaigned against the use of nuclear weapons. During the cold war he accepted the membership in the Soviet Academy of Sciences. He was professor at MIT and for many years director of CERN, in Geneva. He wrote several successful physics textbooks. The author heard him making the above statement in 1982, during one of his lectures.

<sup>\*\*</sup> This is not in contrast with the fact that a few whale species have brains with a larger mass. The larger mass is due to the protection these brains require against the high pressures which appear when whales dive (some dive to depths of 1 km). The number of neurons in whale brains is considerably smaller than in human brains.

#### LIVING CLOCKS

#### L'horologe fait de la réclame pour le temps.\* Georges Perros

Vol. I, page 44 We have given an overview of living clocks already at the beginning of our adventure. They are common in bacteria, plants and animals. And as Table 3 shows, without biological clocks, neither life nor pleasure would exist.

When we sing a musical note that we just heard we are able to reproduce the original frequency with high accuracy. We also know from everyday experience that humans are able to keep the beat to within a few per cent for a long time. When doing sport or when dancing, we are able to keep the timing to high accuracy. (For shorter or longer times, the internal clocks are not so precise.) All these clocks are located in the brain.

Brains process information. Also computers do this, and like computers, all brains need a clock to work well. Every clock is made up of the same components. It needs an *oscillator* determining the rhythm and a mechanism to feed the oscillator with energy. In addition, every clock needs an oscillation *counter*, i.e., a mechanism that reads out the clock signal, and a means of *signal distribution* throughout the system is required, synchronizing the processes attached to it. Finally, a clock needs a *reset mechanism*. If the clock has to cover many time scales, it needs several oscillators with different oscillation frequencies and a way to reset their relative phases. Even though physicists know fairly well how to build good clocks, we still do not know

Ref. 23

Ref. 24

many aspects of biological clocks. Most biological oscillators are chemical systems; some, like the heart muscle or the timers in the brain, are electrical systems. The general elucidation of chemical oscillators is due to Ilya Prigogine; it has earned him a Nobel Prize for chemistry in 1977. But not all the chemical oscillators in the human body are known yet, not to speak of the counter mechanisms. For example, a 24-minute cycle inside each human cell has been discovered only in 2003, and the oscillation mechanism is not yet fully clear. (It is known that a cell fed with heavy water ticks with 27-minute instead of 24 minute rhythm.) It might be that the deily rhythm.

24-minute rhythm.) It might be that the daily rhythm, the circadian clock, is made up of or reset by 60 of these 24-minute cycles, triggered by some master cells in the human body. The clock reset mechanism for the circadian clock is also known to be triggered by daylight; the cells in the eye who perform this resetting action have been pinpointed only in 2002. The light signal from these cells is processed by the superchiasmatic nuclei, two dedicated structures in the brain's hypothalamus. The various cells in the human body act differently depending on the phase of this clock.

The clocks with the longest cycle in the human body control *ageing*. One of the more famous ageing clock limits the number of divisions that a cell can undergo. Indeed, the number of cell divisions is finite for most cell types of the human body and typically lies between 50 and 200. (An exception are reproductory cells – we would not exist if they would not be able to divide endlessly.) The cell division counter has been identified; it is embodied in the *telomeres*, special structures of DNA and proteins found at both ends of each chromosome. These structures are reduced by a small amount during each cell division. When the structures are too short, cell division stops. The purely theoretical prediction of this mechanism by Alexei Olovnikov in 1971 was later proven by a number

<sup>\* &#</sup>x27;Clocks are ads for time.'

LIVING BEING	OSCILLATING SYSTEM	Period
Sand hopper (Talitrus saltator)	knows in which direction to flee from circadian the position of the Sun or Moon	
Human ( <i>Homo sapiens</i> )	gamma waves in the brain	0.023 to 0.03 s
	alpha waves in the brain	0.08 to 0.13 s
	heart beat	0.3 to 1.5 s
	delta waves in the brain	0.3 to 10 s
	blood circulation	30 s
	cellular circahoral rhythms	1 to 2 ks
	rapid-eye-movement sleep period	5.4 ks
	nasal cycle	4 to 14 ks
	growth hormone cycle	11 ks
	suprachiasmatic nucleus (SCN), circadian hormone concentration, temperature, etc.; leads to jet lag	90 ks
	skin clock	circadian
	monthly period	2.4(4) Ms
	built-in aging	3.2(3) Gs
Common fly (Musca domestica)	wing beat	30 ms
Fruit fly (Drosophila melanogaster)	wing beat for courting	34 ms
Most insects (e.g. wasps, fruit flies)	winter approach detection (diapause) by yearly length of day measurement; triggers metabolism changes	
Algae (Acetabularia)	Adenosinetriphosphate (ATP) concentration	
Moulds (e.g. Neurospora crassa)	conidia formation	circadian
Many flowering plants	flower opening and closing	circadian
Tobacco plant	flower opening clock (photoperiodism); triggered by length of days, discovered in 1920 by Garner and Allard	annual
Arabidopsis	circumnutation	circadian
	growth	a few hours
Telegraph plant ( <i>Desmodium</i> gyrans)	side leaf rotation	200 s
Forsythia europaea, F. suspensa, F. viridissima, F. spectabilis	Flower petal oscillation, discovered by Van Gooch in 2002	5.1 ks

TABLE 3 Examples of biological rhythms and clocks.

of researchers. (Only the latter received the Nobel Prize in medicine, in 2009, for this confirmation.) Research into the mechanisms and the exceptions to this process, such as cancer and sexual cells, is ongoing.

Not all clocks in human bodies have been identified, and not all mechanisms are

known. For example, basis of the monthly period in women is interesting, complex, and unclear.

Other fascinating clocks are those at the basis of *conscious* time. Of these, the brain's stopwatch or *interval timer* has been most intensely studied. Only recently was its mechanism uncovered by combining data on human illnesses, human lesions, magnetic resonance studies and effects of specific drugs. The basic interval timing mechanism takes place in the striatum in the basal ganglia of the brain. The striatum contains thousands of timer cells with different periods. They can be triggered by a 'start' signal. Due to their large number, for small times of the order of one second, every time interval has a different pattern across these cells. The brain can read these patterns and learn them. In this way we can time music or specific tasks to be performed, for example, one second after a signal.

Even though not all the clock mechanisms in humans are known, biological clocks share a property with all human-built and all non-living clocks: they are limited by quantum mechanics. Even the simple pendulum is limited by quantum theory. Let us explore the topic.

#### WHEN DO CLOCKS EXIST?

C Die Zukunft war früher auch besser.\* Karl Valentin.

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Challenge 24 ny

When we explored general relativity we found out that purely gravitational clocks do not exist, because there is no unit of time that can be formed using the constants c and G. Clocks, like any measurement standard, need matter and non-gravitational interactions to work. This is the domain of quantum theory. Let us see what the situation is in this case.

Ref. 26

First of all, in quantum theory, the time is *not* an observable. Indeed, the time operator is not Hermitean. In other words, quantum theory states that there is no physical observable whose value is proportional to time. On the other hand, clocks are quite common; for example, the Sun or Big Ben work to most people's satisfaction. Observations thus encourages us to look for an operator describing the position of the hands of a clock. However, if we look for such an operator we find a strange result. Any quantum system having a Hamiltonian bounded from below – having a lowest energy – lacks a Hermitean operator whose expectation value increases monotonically with time. This result can be proven rigorously, as a mathematical theorem.

Take a mechanical pendulum clock. In all such clocks the weight has to stop when the chain end is reached. More generally, all clocks have to stop when the battery or the energy source is empty. In other words, in all real clocks the Hamiltonian is bounded from below. And the above theorem from quantum theory then states that such a clock cannot really work.

In short, quantum theory shows that exact *clocks do not exist in nature*. Quantum theory states that any clock can only be *approximate*. Time cannot be measured exactly; time can only be measured approximately. Obviously, this result is of importance for high

<sup>\* &#</sup>x27;Also the future used to be better in the past.' Karl Valentin (b. 1882 Munich, d. 1948 Planegg), playwright, writer and comedian.

precision clocks. What happens if we try to increase the precision of a clock as much as possible?

High precision implies high sensitivity to fluctuations. Now, all clocks have an oscillator inside, e.g., a motor, that makes them work. A high precision clock thus needs a high precision oscillator. In all clocks, the position of this oscillator is read out and shown on the dial. Now, the quantum of action implies that even the most precise clock oscillator has a position indeterminacy. The precision of any clock is thus limited.

Worse, like any quantum system, any clock oscillator even has a small, but finite probability to stop or to run backwards for a while. You can check this conclusion yourself. Just have a look at a clock when its battery is almost empty, or when the weight driving the pendulum has almost reached the bottom position. The clock will start doing funny things, like going backwards a bit or jumping back and forward. When the clock works normally, this behaviour is strongly suppressed; however, it is still possible, though with low probability. This is true even for a sundial.

In summary, clocks necessarily have to be *macroscopic* in order to work properly. A clock must be as large as possible, in order to average out its fluctuations. Astronomical systems are good examples. A good clock must also be well-isolated from the environment, such as a freely flying object whose coordinate is used as time variable. For example, this is regularly done in atomic optical clocks.

# THE PRECISION OF CLOCKS

Given the limitations due to quantum theory, what is the ultimate accuracy  $\tau$  of a clock? To start with, the indeterminacy relation provides the limit on the mass of a clock. The clock mass M must obey

$$M > \frac{\hbar}{c^2 \tau} \tag{2}$$

which is obviously always fulfilled in everyday life. But we can do better. Like for a pen-Challenge 27 e dulum, we can relate the accuracy  $\tau$  of the clock to its maximum reading time T. The idea was first published by Salecker and Wigner. They argued that

$$M > \frac{\hbar}{c^2 \tau} \frac{T}{\tau} \tag{3}$$

where T is the time to be measured. You might check that this condition directly requires that any clock must be macroscopic.

Let us play with the formula by Salecker and Wigner. It can be rephrased in the following way. For a clock that can measure a time t, the size l is connected to the mass mby

$$l > \sqrt{\frac{\hbar t}{m}} \,. \tag{4}$$

How close can this limit be achieved? It turns out that the smallest clocks known, as well Ref. 28 as the clocks with most closely approach this limit, are bacteria. The smallest bacteria, the *mycoplasmas*, have a mass of about  $8 \cdot 10^{-17}$  kg, and reproduce every 100 min, with a

Challenge 25 e

Ref. 27

Challenge 28 e

precision of about 1 min. The size predicted from expression (4) is between  $0.09 \,\mu\text{m}$  and  $0.009 \,\mu\text{m}$ . The observed size of the smallest mycoplasmas is  $0.3 \,\mu\text{m}$ . The fact that bacteria can come so close to the clock limit shows us again what a good engineer evolution has been.

Note that the requirement by Salecker and Wigner is not in contrast with the possibility to make the *oscillator* of the clock very small; researchers have built oscillators made of a single atom. In fact, such oscillations promise to be the most precise human built clocks. But the oscillator is only one part of any clock, as explained above.

In the real world, the clock limit can be tightened even more. The whole mass M cannot be used in the above limit. For clocks made of atoms, only the binding energy between atoms can be used. This leads to the so-called *standard quantum limit for clocks*; it limits the accuracy of their frequency v by

$$\frac{\delta v}{v} = \sqrt{\frac{\Delta E}{E_{\text{tot}}}}$$
(5)

where  $\Delta E = \hbar/T$  is the energy indeterminacy stemming from the finite measuring time T and  $E_{tot} = NE_{bind}$  is the total binding energy of the atoms in the metre bar. So far, the quantum limit has not yet been achieved for any clock, even though experiments are getting close to it.

In summary, clocks exist only in the limit of  $\hbar$  being negligible. In practice, the errors made by using clocks and metre bars can be made as small as required; it suffices to make the clocks large enough. Clock built into human brains comply with this requirement. We can thus continue our investigation into the details of matter without much worry, at least for a while. Only in the last part of our mountain ascent, where the requirements for precision will be even higher and where general relativity will limit the size of physical systems, trouble will appear again: the impossibility to build precise clocks will then become a central issue.

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## WHY ARE PREDICTIONS SO DIFFICULT, ESPECIALLY OF THE FUTURE?

Future: that period of time in which our affairs prosper, our friends are true, and our happiness is assured.

Ambrose Bierce

Nature limits predictions in four ways:

- 1. We have seen that quantum theory, through the uncertainty relations, limits the precision of measurements, and of clocks and time measurements in particular. Thus, the quantum of action makes it hard to determine initial states to full precision – even for a single particle.
- Vol. I, page 239 2. We have seen that high numbers of particles make it difficult to predict the future due to the often statistical nature of their initial conditions.
  - 3. We have found in our adventure that predictions of the future are made difficult by non-linearities and by the divergence from nearby initial conditions.

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4. We have seen that a non-trivial space-time topology can limit predictability. For ex-

Ref. 29 Page 43 ample, we will discover that black hole and horizons can limit predictability due to their one-way inclusion of energy, mass and signals.

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5. We will find out in the last pat of our adventure that quantum gravity effects even make a precise definition of time and space impossible.

Measurements and practical predictability are thus limited. The central reason for this limitation is the quantum of action. But if the quantum of action makes perfect clocks impossible, is determinism still the correct description of nature? And does time exist after all? The answer is clear: yes and no. We learned that all the mentioned limitations of clocks can be overcome for limited time intervals; in practice, these time intervals can be made so large that the limitations do *not* play a role in everyday life. As a result,

▷ In practice, in all quantum systems both determinism and the concept of time remain applicable.

This conclusion is valid even though theory says otherwise. Our ability to enjoy the pleasures due to the flow of time remains intact.

However, when extremely large momentum flows or extremely large dimensions need to be taken into account, quantum theory cannot be applied alone; in those cases, general relativity needs to be taken into account. The fascinating effects that occur in those situations will be explored in detail later on.

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## DECAY AND THE GOLDEN RULE

I prefer most of all to remember the future. Salvador Dalì

All pleasure only makes sense in the face of death. And death is a form of decay. Decay is any spontaneous change. Like the wave aspect of matter, decay is a process with no classical counterpart. Of course, any decay – including the emission of light by a lamp, the triggering of a camera sensor, radioactivity or the ageing of humans – can be observed classically; however, the *origin* of decay is a pure quantum effect.

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In any decay of unstable systems or particles, the decoherence of superpositions of macroscopically distinct states plays an important role. Indeed, experiments confirm that the prediction of decay for a specific system, like a scattering of a particle, is only possible on *average*, for a large number of particles or systems, and never for a single one. These observations confirm the quantum origin of decay. In every decay process, the superposition of macroscopically distinct states – in this case those of a decayed and an undecayed particle – is made to decohere rapidly by the interaction with the environment. Usually the 'environment' vacuum, with its fluctuations of the electromagnetic, weak and strong fields, is sufficient to induce decoherence. As usual, the details of the involved environment states are unknown for a single system and make any prediction for a specific system impossible.

What is the *origin* of decay? Decay is always due to *tunnelling*. With the language of quantum electrodynamics, we can say that decay is motion induced by the vacuum fluctuations. Vacuum fluctuations are random. The experiment between the plates confirms the importance of the environment fluctuations for the decay process.

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Quantum theory gives a simple description of decay. For a system consisting of a large number N of decaying identical particles, any *decay* is described by

$$\dot{N} = -\frac{N}{\tau}$$
 where  $\frac{1}{\tau} = \frac{2\pi}{\hbar} \left| \langle \psi_{\text{initial}} | H_{\text{int}} | \psi_{\text{final}} \rangle \right|^2$ . (6)

This result for  $\dot{N} = dN/dt$  was named the *golden rule* by Fermi,\* because it works so well despite being an approximation whose domain of applicability is not easy to specify. The golden rule leads to

$$N(t) = N_0 e^{-t/\tau} . (7)$$

Decay is thus predicted to follow an exponential behaviour, independently of the details of the physical process. In addition, the decay time  $\tau$  depends on the interaction and on the square modulus of the transition matrix element. For almost a century, all experiments confirmed that quantum decay is *exponential*.

On the other hand, when quantum theory is used to derive the golden rule, it is found that decay is exponential only in certain special systems. A calculation that takes into account higher order terms predicts two deviations from exponential decay for completely isolated systems: for short times, the decay rate should *vanish*; for long times, the decay rate should follow an *algebraic* – not an exponential – dependence on time, in some

Ref. 31 cases even with superimposed oscillations. After an intense experimental search, deviations for short times have been observed. The observation of deviations at long times are rendered impossible by the ubiquity of thermal noise. In summary, it turns out that decay is exponential only when the environment is noisy, the system made of many weakly interacting particles, or both. Since this is usually the case, the mathematically exceptional exponential decrease becomes the (golden) rule in the description of decay.

Can you explain why human life, despite being a quantum effect, is not observed to Challenge 30 s follow an exponential decay?

# The present in quantum theory

Utere temporibus.\*\*

Ovidius

Ref. 32

Challenge 29 e

Many sages advise to enjoy the present. As shown by perception research, what humans call 'present' has a duration of between 20 and 70 milliseconds. This result on the biological present leads us to ask whether the *physical* present might have a duration as well.

In everyday life, we are used to imagine that shortening the time taken to measure the position of a point object as much as possible will approach the ideal of a particle fixed at a given point in space. When Zeno discussed the flight of an arrow, he assumed that this is possible. However, quantum theory changes the situation.

Can we really say that a moving system is at a given spot at a given time? In order to

<sup>\*</sup> Originally, the golden rule is a statement from the christian bible, (Matthew 7,12) namely the precept 'Do to others whatever you would like them to do to you.'

<sup>\*\* &#</sup>x27;Use the occasions.' Tristia 4, 3, 83

find an answer through experiment, we could use a photographic camera whose shutter time can be reduced at will. What would we find? When the shutter time approaches the oscillation period of light, the sharpness of the image would decrease; in addition, the colour of the light would be influenced by the shutter motion. We can increase the energy of the light used, but the smaller wavelengths only shift the problem, they do not solve it. Worse, at extremely small wavelengths, matter becomes transparent, and shutters cannot be realized any more. All such investigations confirm: Whenever we reduce shutter times as much as possible, observations become unsharp. The lack of sharpness is due to the quantum of action. Quantum theory thus does not confirm the naive expectation that shorter shutter times lead to sharper images. In contrast, the quantum aspects of nature show us that there is no way in principle to approach the limit that Zeno was discussing.

In summary, the indeterminacy relation and the smallest action value prevent that moving objects are at a fixed position at a given time. Zeno's discussion was based on an extrapolation of classical concepts into domains where it is not valid any more. Every observation, like every photograph, implies a *time average*:

Observations average interactions over a given time span.

For a photograph, the duration is given by the shutter time; for a measurement, the average is defined by the details of the set-up. Whatever this set-up might be, the averaging time is never zero. \* There is no 'point-like' instant of time that describes the present. The observed, physical *present* is always an average over a non-vanishing interval of time. In nature, the present has a finite duration. To give a rough value that guides our thought, in most situations the length of the present will be less than a yoctosecond, so that it can usually be neglected.

## Why can we observe motion?

Zeno of Elea was thus wrong in assuming that motion is a sequence of specific positions in space. Quantum theory implies that motion is *only approximately* the change of position with time.

Why then can we observe and describe motion in quantum theory? Quantum theory shows that motion is the *low energy approximation* of quantum evolution. Quantum evolution *assumes* that space and time measurements of sufficient precision can be performed. We know that for any given observation energy, we can build clocks and metre bars with much higher accuracy than required, so that in practice, quantum evolution is applicable in all cases. As long as energy and time have no limits, all problems are avoided, and *motion is a time sequence of quantum states*.

In summary, we can observe motion because for any known observation energy we can find a still higher energy and a still longer averaging time that can be used by the measurement instruments to define space and time with higher precision than for the system under observation. In the final part of our mountain ascent, we will discover that there is a maximum energy in nature, so that we will need to change our description in those situations. However, this energy value is so huge that it does not bother us at all at the present point of our exploration.

Vol. VI, page 46

Page 51 \* Also the discussion of the quantum Zeno effect, below, does not change the conclusions of this section.

## Rest and the quantum Zeno effect

The quantum of action implies that there is no rest in nature. Rest is thus always either an approximation or a time average. For example, if an electron is bound in an atom, not freely moving, the probability cloud, or density distribution, is stationary in time. But there is another apparent case of rest in quantum theory, the *quantum Zeno effect*. Usually, observation *changes* the state of a system. However, for certain systems, observation can have the opposite effect, and *fix* a system.

Quantum mechanics predicts that an unstable particle can be prevented from decaying if it is continuously observed. The reason is that an observation, i.e., the interaction with the observing device, yields a non-zero probability that the system does not evolve. If the frequency of observations is increased, the probability that the system does not decay at all approaches 1. Three research groups – Alan Turing by himself in 1954, the group of A. Degasperis, L. Fonda and G.C. Ghirardi in 1974, and George Sudarshan and Baidyanath Misra in 1977 – have independently predicted this effect, today called the *quantum Zeno effect*. In sloppy words, the quantum Zeno effect states: if you look at a system all the time, nothing happens.

The quantum Zeno effect is a natural consequence of quantum theory; nevertheless, its strange circumstances make it especially fascinating. After the prediction, the race for the first observation began. The effect was partially observed by David Wineland and his

Ref. 33

the first observation began. The effect was partially observed by David Wineland and his group in 1990, and definitively observed by Mark Raizen and his group in 2001. In the meantime, other groups have confirmed the measurements. Thus, quantum theory has been confirmed also in this surprising aspect.

The quantum Zeno effect is also connected to the deviations from exponential decay – due to the golden rule – that are predicted by quantum theory. Indeed, quantum theory predicts that every decay is exponential only for intermediate times, and quadratic for short times and polynomial for extremely long times. These issues are research topics to this day.

Ref. 34

Ref. 35

In a fascinating twist, in 2002, Saverio Pascazio and his team have predicted that the quantum Zeno effect can be used to realize X-ray tomography of objects with the lowest radiation levels imaginable.

In summary, the quantum Zeno effect does not contradict the statement that there is no rest in nature; in situations showing the effect, there is an non-negligible interaction between the system and its environment. The details of the interaction are important: in certain cases, frequent observation can actually accelerate the decay or evolution. Quantum physics still remains a rich source of fascinating effects.

# Consciousness - a result of the quantum of action

In the pleasures of life, consciousness plays an essential role.

Vol. III, page 339

▷ *Consciousness* is our ability to observe what is going on in our mind.

This activity, like any type of change, can itself be observed and studied. Though it is hard and probably impossible to do so by introspection, we can study consciousness in others. Obviously, consciousness takes place in the brain. If it were not, there would be no way to keep it connected with a given person. Simply said, we know that each brain located on Earth moves with over one million kilometres per hour through the cosmic background radiation; we also observe that consciousness moves along with it.

The brain is a quantum system: it is based on molecules and electrical currents. The changes in consciousness that appear when matter is taken away from the brain – in operations or accidents – or when currents are injected into the brain – in accidents, experiments or misguided treatments – have been described in great detail by the medical profession. Also the observed influence of chemicals on the brain – from alcohol to hard drugs – makes the same point. The brain is a quantum system.

Modern imaging machines can detect which parts of the brain work when sensing, remembering or thinking. Not only is sight, noise and thought processed in the brain; we can follow these processes with measurement apparatus. The best imaging machines are based on magnetic resonance, as described below. Another, more questionable imaging technique, positron tomography, works by letting people swallow radioactive sugar. Both techniques confirm the findings on the location of thought and on its dependence on chemical fuel. In addition, we already know that memory depends on the particle nature of matter. All these observations depend on the quantum of action.

Today, we are thus in the same situation as material scientists were a century ago: they knew that matter is made of charged particles, but they could not say *how* matter is built up. Similarly, we know today that consciousness is made from the signal propagation and signal processing in the brain; we know that consciousness is an electrochemical process. But we do not know yet the details of *how* the signals make up consciousness. Unravelling the workings of this fascinating quantum system is the aim of neurology. This is one of the great challenges of twenty-first century science.

Can you add a few arguments to the ones given here, showing that consciousness is a physical process? Can you show in particular that not only the consciousness of others, but also your own consciousness is a quantum process? Can you show, in addition, that despite being a quantum process, coherence plays no essential role in consciousness?

In short, our consciousness is a consequence of the matter that makes us up. Consciousness and pleasure depend on matter, its interactions and the quantum of action.

# Why can we observe motion? - Again

Studying nature can be one of the most intense pleasures of life. All pleasures are based on our ability to observe or detect motion. And our human condition is central to this ability. In particular, in our adventure so far we found the following connections: We

experience motion

- only because we are of finite size, and in particular, because we are large compared to our quantum mechanical wavelength (so that we do not experience wave effects in everyday life),
- only because we are large compared to a black hole of our same mass (so that we have useful interactions with our environment),
- only because we are made of a large but finite number of atoms (to produce memory and enable observations),
- only because we have a limited memory (so that we can clear it),
- only because we have a finite but moderate temperature (finite so that we have a lifetime, not zero so that we can be working machines),

tr ns f io ss dc io us f c es en e

Challenge 31 s

- only because we are a mixture of liquids and solids (enabling us to move and thus to experiment),
- only because we are approximately electrically neutral (thus avoiding that our sensors get swamped),
- only because our brain forces us to approximate space and time by continuous entities (otherwise we would not form these concepts),
- only because our brain cannot avoid describing nature as made of different parts (otherwise we would not be able to talk or think),
- only because our ancestors reproduced,
- only because we are animals (and thus have a brain),
- only because life evolved here on Earth,
- only because we live in a relatively quiet region of our galaxy (which allowed evolution), and
- only because the human species evolved long after the big bang (when the conditions were more friendly to life).

If any of these conditions – and many others – were not fulfilled, we would not observe motion; we would have no fun studying physics. In fact, we can also say: if any of these conditions were not fulfilled, motion would not exist. In many ways motion is thus an illusion, as Zeno of Elea had claimed a long time ago. Of course, motion is a *inevitable* illusion, one that is shared by many other animals and machines. To say the least, the observation and the concept of motion is a result of the properties and limitations of the human condition. A complete description of motion and nature must take this connection into account. Before we attempt that in the last volume of this adventure, we explore a few additional details.

# Curiosities and fun challenges about quantum experience

Most clocks used in everyday life, those built inside the human body and those made by humans, are electromagnetic. Any clock on the wall, be it mechanical, quartz controlled, radio or solar controlled, is based on electromagnetic effects. Do you know an exception?

\* \*

Challenge 32 s

Vol. I, page 15

The sense of smell is quite complex. For example, the substance that smells most badly to humans is *skatole*, also called, with his other name, *3-methylindole*. This is the molecule to which the human nose is most sensitive. Skatole makes faeces smell bad; it is a result of haemoglobin entering the digestive tract through the bile. Skatole does not smell bad to all animals; in contrast to humans, flies are attracted by its smell. Skatole is also produced by some plants for this reason.

On the other hand, *small* levels of skatole do not smell bad to humans. Skatole is also used by the food industry in small quantities to give smell and taste to vanilla ice cream – though under the other name.

\* \*

It is worth noting that human senses detect energies of quite different magnitudes. The eyes can detect light energies of about 1 aJ, whereas the sense of touch can detect only

## Challenge 33 s energies as small as about 10 µJ. Is one of the two systems relativistic?

\* \*

The human construction plan is stored in the DNA. The DNA is structured into 20 000 genes, which make up about 2 % of the DNA, and 98 % non-coding DNA, once called 'junk DNA'. Humans have as many genes as worms; plants have many more. Only around 2010 it became definitely clear, through the international 'Encode' project, what the additional 98 % of the DNA do: they switch genes on and off. They form the *administration* of the genes and work mostly by binding to specific proteins.

Research suggests that most genetic defects, and thus of genetic diseases, are not due to errors in genes, but in errors of the control switches. All this is an ongoing research field.

\* \*

Even at perfect darkness, the eye does not yield a black impression, but a slightly brighter one, called *eigengrau*. This is a result of noise created inside the eye, probably triggered by spontaneous decay of rhodopsin, or alternatively, by spontaneous release of neuro-transmitters.

\* \*

The high sensitivity of the ear can be used to *hear* light. To do this, take an empty 750 ml jam glass. Keeping its axis horizontal, blacken the upper half of the inside with a candle. The lower half should remain transparent. After doing this, close the jam glass with its lid, and drill a 2 to 3 mm hole into it. If you now hold the closed jam glass with the hole to your ear, keeping the black side up, and shining into it from below with a 50 W light bulb, something strange happens: you hear a 100 Hz sound. Why?

Challenge 34 s bulb, some

Ref. 37

Ref. 38

Most senses work already before birth. It is well-known since many centuries that playing the violin to a pregnant mother every day during the pregnancy has an interesting effect. Even if nothing is told about it to the child, it will become a violin player later on. In fact, most musicians are 'made' in this way.

\* \*

There is ample evidence that not using the senses is damaging. People have studied what happens when in the first years of life the vestibular sense – the one used for motion detection and balance restoration – is not used enough. Lack of rocking is extremely hard to compensate later in life. Equally dangerous is the lack of use of the sense of touch. Babies, like all small mammals, that are generally and systematically deprived of these experiences tend to violent behaviour during the rest of their life.

\* \*

The importance of ion channels in the human body can not be overstressed. Ion channels malfunctions are responsible for many infections, for certain types of diabetes and for many effects of poisons. But above all, ion channels, and electricity in general, are essential for life.

#### THE PHYSICS OF PLEASURE

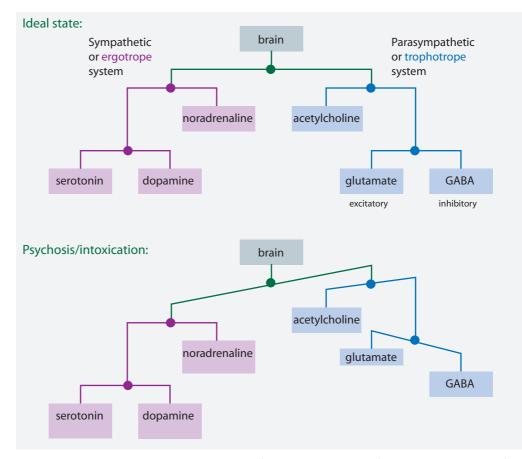


FIGURE 15 The 'neurochemical mobile' model of well-being, with one of the way it can get out of balance.

\* \*

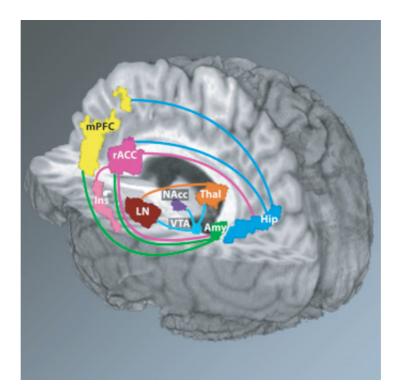
Our body contains many systems that avoid unpleasant outcomes. For example, it was discovered in 2006 that saliva contains a strong pain killer, much stronger than morphine; it is now called *opiorphin*. It prevents that small bruises inside the mouth disturb us too much. Opiorphine also acts as an antidepressant. Future research has to show whether food addiction is related to this chemical.

\* \*

It is still unknown why people – and other mammals – *yawn*. This is still a topic of research.

\* \*

Nature has invented the senses to increase pleasure and avoid pain. But neurologists have found out that nature has gone even further; there is a dedicated *pleasure system* in the brain, shown in Figure 16, whose function is to decide which experiences are pleasurable and which not. The main parts of the pleasure system are the *ventral tegmental area* in



**FIGURE 16** The location of the ventral tegmental area (VTA) and of the nucleus accumbens (NAcc) in the brain. The other regions involved in pleasure and addiction are Amy, the amygdala, Hip, the hippocampus, Thal, the thalamus, rACC, the rostral anterior cingulate cortex, mPFC, the medial prefrontal cortex, lns, the insula, and LN, the lentiform nucleus (courtesy NIH).

the midbrain and the *nucleus accumbens* in the forebrain. The two parts regulate each other mainly through *dopamine* and *GABA*, two important neurotransmitters. Research has shown that dopamine is produced whenever pleasure exceeds expectations. Nature has thus developed a special signal for this situation.

In fact, well-being and pleasure are controlled by a large number of neurotransmitters and by many additional regulation circuits. Researchers are trying to model the pleasure system with hundreds of coupled differential equations, with the distant aim being to understand addiction and depression, for example. On the other side, also simple models of the pleasure system are possible. One, shown in Figure 15, is the 'neurochemical mobile' model of the brain. In this model, well-being is achieved whenever the six most important neurotransmitters\* are in relative equilibrium. The different possible departures from equilibrium, at each joint of the mobile, can be used to describe depression, schizophrenia, psychosis, the effect of nicotine or alcohol intake, alcohol dependency, delirium, drug addiction, detoxication, epilepsy and more.

<sup>\*</sup> Neurotransmitters come in many types. They can be grouped into *mono- and diamines* – such as dopamine, serotonin, histamine, adrenaline – *acetylcholine, amino acids* – such as glycine, GABA and glutamate – *polypeptides* – such as oxytocin, vasopressin, gastrin, the opiods, the neuropetides etc. – *gases* – such as NO and CO – and a number of molecules that do not fit into the previous classes – such as anandamide or NAAG.

Challenge 35 s

\* \*

The pleasure system in the brain is not only responsible for addiction. It is also respons ible, as Helen Fisher showed through MRI brain scans, for romantic love. Romantic love, directed to one single other person, is a state that is created in the ventral tegmental area and in the nucleus accumbens. Romantic love is thus a part of the reptilian brain; indeed, romantic love is found in many animal species. Romantic love is a kind of positive addiction, and works like cocaine. In short, in life, we can all choose between addiction and love.

An important aspect of life is death. When we die, conserved quantities like our energy, momentum, angular momentum and several other quantum numbers are redistributed. They are redistributed because conservation means that nothing is lost. What does all this imply for what happens after death?

\*

We all know the smell that appears in the open field at the start of a summer rainfall, or the smell of fresh earth. It is due to a substance called *geosmin*, a bicyclic alcohol that is produced by bacteria in the soil. The bacteria produce it when it rains. For reasons not fully understood, the human nose is especially sensitive to the smell of geosmin: we are able to smell it at concentrations below  $10^{-10}$ .

\* \*

Also plants have sensors. Plants can sense light, touch, gravity, chemicals, as well as electric fields and currents. Many plants grow differently when touched; roots sense and conduct electric signals and then grow accordingly; obviously, plants grow against gravity and towards light. Above all, plants are known to be able to distinguish many different chemicals in the air, above all, ethene (ethylene), which is also an important plant hormone.

\*

Many plants have built-in sensors and clocks that measure the length of the day. For example, *spinach* does not grow in the tropics, because in order to flower, spinach must sense for at least fourteen days in a row that the day is at least 14 hours long – and this never happens in the tropics. This property of plants, called *photoperiodism*, was discovered in 1920 by Wightman Garner and Harry Allard while walking across tobacco fields. They discovered – and proved experimentally – that tobacco plants and soya plants only flower when the length of the day gets sufficiently short, thus around September. Garner and Allard found that plants could be divided into species that flower when days are short – such as chrysanthemum or coffee – others that flower when days are long – such as cross or tomatoes. The measurement precision for the length of the day is around 10 min. The day length sensor itself was discovered only much later; it is located in the leaves of the plant, is called the *phytochrome system* and is based on specialised proteins. The proteins are able to measure the ratio between bright red and dark red light and control the moment of flower opening in such plants.

#### SUMMARY ON BIOLOGY AND PLEASURE

To ensure the successful reproduction of living beings, evolution has pursued miniaturization as much as possible. Molecular motors, including molecular pumps, are the smallest motors known so far; they work as quantum ratchets. Molecular motors are found in huge numbers in every living cell. In short:

▷ Every human consists of trillions of machines.

To increase pleasure and avoid pain, evolution has also supplied the human body also with numerous sensors, sensor mechanisms, and a pleasure system deep inside the brain. In short, nature has invented *pleasure* as a guide for behaviour. Neurologists have thus proven what Epicurus said 23 centuries ago and Sigmund Freud repeated one century ago:

▷ Pleasure controls human life.\*

All biological pleasure sensors and pleasure systems are based on quantum motion, in particular on chemistry and materials science. We therefore explore both fields in the following.

V A

<sup>\*</sup> But Epicurus also said: 'It is impossible to live a pleasant life without living wisely and honourably and justly, and it is impossible to live wisely and honourably and justly without living pleasantly.' This is one of his *Principal Doctrines*.

# Chapter 2 Changing the world with Quantum effects

The discovery of quantum effects has changed everyday life. It has allowed he distribution of speech, music and films. The numerous possibilities of elecommunications and of the internet, the progress in chemistry, materials science, electronics and medicine would not have been possible without quantum effects. Many other improvements of our everyday life are due to quantum physics, and many are still expected. In the following, we give a short overview of this vast field.

# CHEMISTRY - FROM ATOMS TO DNA

**G** Bier macht dumm.\*\*

Albert Einstein

It is an old truth that Schrödinger's equation contains all of chemistry. With quantum theory, for the first time people were able to calculate the strengths of chemical bonds, and what is more important, the angle between them. Quantum theory thus explains the *shape* of molecules and thus indirectly, the shape of all matter. In fact, the correct statement is: the *Dirac* equation contains all of chemistry. The relativistic effects that distinguish the two equations are necessary, for example, to understand why gold is yellow and does not rust or why mercury is liquid.

To understand molecules and everyday matter, the first step is to understand atoms. The early quantum theorists, lead by Niels Bohr, dedicated their life to understanding their atoms and their detailed structure. The main result of their efforts is what you learn in secondary school: in atoms with more than one electron, the various electron clouds form spherical layers around the nucleus. The electron layers can be grouped into groups of related clouds that are called *shells*. For electrons outside the last fully occupied shell, the nucleus and the inner shells, the atomic *core*, can often be approximated as a single charged entity.

Shells are numbered from the inside out. This *principal quantum number*, usually written n, is deduced and related to the quantum number that identifies the states in the hydrogen atom. The relation is shown in Figure 17.

Quantum theory shows that the first atomic shell has room for two electrons, the second for 8, the third for 18, and the general n-th shell for  $2n^2$  electrons. The (neutral)

<sup>\*\* &#</sup>x27;Beer makes stupid.'

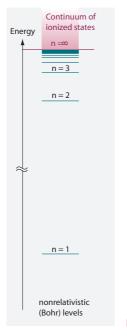


FIGURE 17 The principal quantum numbers in hydrogen.

atom with one electron is hydrogen, the atom with two electrons is called helium. Every chemical element has a specific number of electrons (and the same number of protons, as we will see). A way to picture this connection is shown in Figure 18. It is called the *periodic table of the elements*. The standard way to show the table is found on page 346 and, more vividly, in Figure 19. (For a periodic table with a video about each element, see www.periodicvideos.com.)

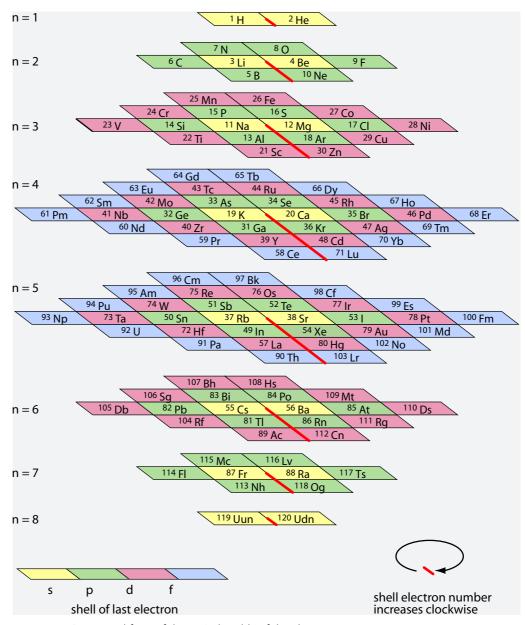
Experiments show that different atoms that share the *same* number of electrons in their outermost shell show *similar* chemical behaviour. Chemists know that the chemical behaviour of an element is decided by the ability of its atoms to from bonds. For example, the elements with one electron in their outer s shell are the *alkali metals* lithium, sodium, potassium, rubidium, caesium and francium; hydrogen, the exception, is conjectured to be metallic at high pressures. The elements with filled outermost shells are the *noble gases* helium, neon, argon, krypton, xenon, radon and ununoctium.

### ATOMIC BONDS

Ref. 42

When two atoms approach each other, their electron clouds are deformed and mixed. The reason for these changes is the combined influence of the two nuclei. These cloud changes are highest for the outermost electrons: they form chemical *bonds*.

Bonds can be pictured, in the simplest approximation, as cloud overlaps that *fill* the outermost shell of both atoms. These overlaps lead to a gain in energy. The energy gain is the reason that fire is hot. In wood fire, chemical reactions between carbon and oxygen atoms lead to a large release of energy. After the energy has been released, the atomic bond produces a fixed distance between the atoms, as shown in Figure 20. This distance is due to an energy minimum: a lower distance would lead to electrostatic repulsion



61

FIGURE 18 An unusual form of the periodic table of the elements.

between the atomic cores, a higher distance would increase the electron cloud energy.

Many atoms can bind to more than one neighbours. In this case, energy minimization also leads to specific bond angles, as shown in Figure 21. Maybe you remember those funny pictures of school chemistry about orbitals and dangling bonds. Such dangling bonds can now be measured and observed. Several groups were able to image them using scanning force or scanning tunnelling microscopes, as shown in Figure 22.

The repulsion between the clouds of each bond explains why angle values near that of tetrahedral skeletons (2 arctan  $\sqrt{2}$  = 109.47°) are so common in molecules. For example,

Challenge 36 e

Ref. 43



FIGURE 19 A modern periodic table of the elements (© Theodore Gray, for sale at www.theodoregray. com).

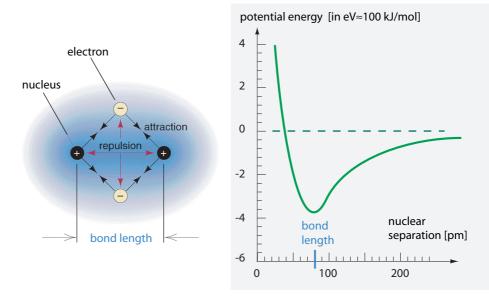


FIGURE 20 The forming of a chemical bond between two atoms, and the related energy minimum (left hand image © chemistry4gcms2011.wikispaces.com).

the H-O-H angle in water molecules is 107°.

Atoms can also be connected by *multiple* bonds. Double bonds appear in carbon dioxide, or  $CO_2$ , which is therefore often written as O = C = O, triple bonds appear in carbon monoxide, CO, which is often written as  $C \equiv O$ . Both double and triple bonds are common in organic compounds. (In addition, the well-known hexagonal benzene ring molecule  $C_6H_6$ , like many other compounds, has a one-and-a-half-fold bond.) Higher bonds are rare but do exist; quadruple bonds occur among transition metal atoms such

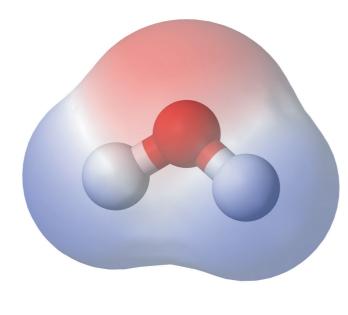


FIGURE 21 An artistic illustration of chemical bond angles when several atoms are involved: in a water molecule, with its charge distribution due to its covalent bonds, blue colour at the two ends indicates positive charge, and the red colour in upper vertex indicates negative charge. The central drawing shows a typical structural rendering of the water molecule (© Benjah-bmm27).

as rhenium or tungsten. Research also confirmed that the uranium  $U_2$  molecule, among others, has a quintuple bond, and that the tungsten  $W_2$  molecule has a hextuple bond.

# RIBONUCLEIC ACID AND DEOXYRIBONUCLEIC ACID

Probably the most fascinating molecule of all is human deoxyribonucleic acid, better known with its abbreviation DNA. The nucleic acids where discovered in 1869 by the physician Friedrich Miescher (b. 1844 Basel, d. 1895 Davos) in white blood cells. He also found it in cell nuclei, and thus called the substance 'Nuklein'. In 1874 he published an important study showing that the molecule is contained in spermatozoa, and discussed the question if this substance could be related to heredity. With his work, Miescher paved the way to a research field that earned many colleagues Nobel Prizes (though not for himself, as he died before they were established). They changed the name to 'nucleic acid'.

DNA is, as shown in Figure 23, a polymer. A polymer is a molecule built of many similar units. In fact, DNA is among the longest molecules known. Human DNA molecules, for example, can be up to 5 cm in length. Inside each human cell there are 46 chromosomes. In other words, inside each human cell there are molecules with a total length of 2 m. The way nature keeps them without tangling up and knotting is a fascinating topic in itself. All DNA molecules consist of a double helix of sugar derivates, to which four nuclei acids are attached in irregular order. Nowadays, it is possible to make images of single DNA molecules; an example is shown in Figure 24.

Ref. 46 single DNA molecules; an example is shown in Figure 24. At the start of the twentieth century it became clear that Desoxyribonukleinsäure (DNS) – translated as deoxyribonucleic acid (DNA) into English – was precisely what Erwin Schrödinger had predicted to exist in his book *What Is Life?* As central part of the chromosomes contained the cell nuclei, DNA is responsible for the storage and reproduction of the information on the construction and functioning of Eukaryotes. The

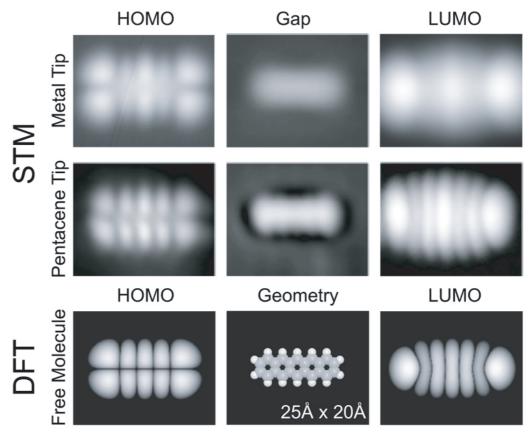


FIGURE 22 Top two rows: measured chemical bonds in the pentacene molecule, using different techniques; bottom row: textbook calculations and illustrations of the same experiment (© IBM).

information is coded in the ordering of the four nucleic acids. DNA is the carrier of hereditary information. DNA determines in great part how the single cell we all once have been grows into the complex human machine we are as adults. For example, DNA determines the hair colour, predisposes for certain illnesses, determines the maximum size one can grow to, and much more. Of all known molecules, human DNA is thus most intimately related to human existence. The large size of the molecules is the reason that understanding its full structure and its full contents is a task that will occupy scientists for several generations to come.

To experience the wonders of DNA, have a look at the animations of DNA copying and of other molecular processes at the unique website www.wehi.edu.au/education/wehitv.

## CURIOSITIES AND FUN CHALLENGES ABOUT CHEMISTRY

Among the fascinating topics of chemistry are the studies of substances that influence humans: toxicology explores *poisons*, pharmacology explores *medicines* (pharmaceutical drugs) and endocrinology explores *hormones*.

Over 50 000 poisons are known, starting with water (usually kills when drunk in amounts larger than about 10 l) and table salt (can kill when 100 g are ingested) up to

#### CHEMISTRY - FROM ATOMS TO DNA

Challenge 37 e

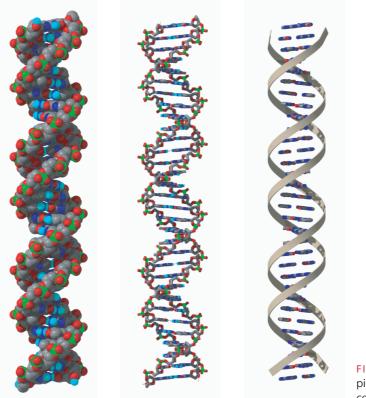


FIGURE 23 Several ways to picture B-DNA, all in false colours (© David Deerfield).

polonium 210 (kills in doses as low as 5 ng, far less than a spec of dust). Most countries have publicly accessible poison databases; see for example www.gsbl.de.

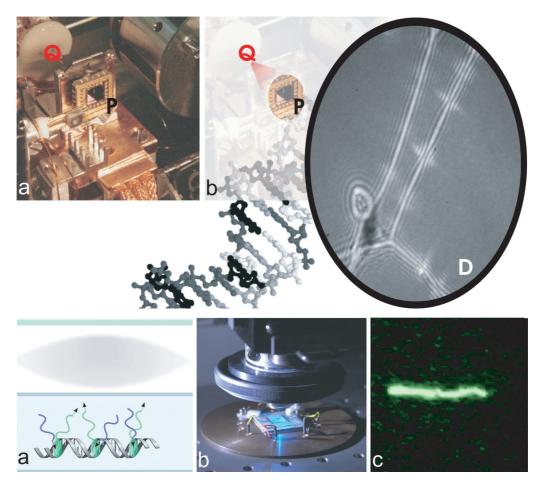
Can you imagine why 'toxicology', the science of poisons, actually means 'bow science' in Greek? In fact, not all poisons are chemical. Paraffin and oil for lamps, for example, regularly kill children who taste it because some oil enters the lung and forms a thin film over the alveoles, preventing oxygen intake. This so-called *lipoid pneumonia* can be deadly even when only a *single drop* of oil is in the mouth and then inhaled by a child. Paraffin should never be present in homes with children.

In the 1990s, the biologist Binie Ver Lipps discovered a substance, a simple polypeptide, that helps against venoms of snakes and other poisonous animals. The medical industry worldwide refuses to sell the substance – it could save many lives – because it is too cheap.

\* \*

Whether a substance is a poison depends on the animal ingesting it. Chocolate is poison for dogs, but not for children. Poisonous mushrooms are edible for snails; bitten mushrooms are thus not a sign of edibility.

Hormones are internal signalling substances produced by the human body. Chemically,



**FIGURE 24** Two ways to image single DNA molecules: by holography with electrons emitted from atomically sharp tips (top) and by fluorescence microscopy, with a commercial optical microscope (bottom) (© Hans-Werner Fink/Wiley VCH).

they can be peptides, lipids or monoamines. Hormones induce mood swings, organize the fight, flight or freeze responses, stimulate growth, start puberty, control cell death and ageing, activate or inhibit the immune system, regulate the reproductive cycle and activate thirst, hunger and sexual arousal.

\* \*

When one mixes 50 ml of distilled water and 50 ml of ethanol (alcohol), the volume ofChallenge 38 sthe mixture has less than 100 ml. Why?

Why do *organic* materials, i.e., materials that contain several carbon atoms, usually burn at much lower temperature than *inorganic* materials, such as aluminium or magnesium?

\* \*

\* \*

Challenge 39 ny

A cube of sugar does not burn. However, if you put some cigarette ash on top of it, it burns. Why?

\* \*

Challenge 40 ny

Sugars are essential for life. One of the simplest sugars is *glucose*, also called *dextrose* or grape sugar. Glucose is a so-called monosaccharide, in contrast to cane sugar, which is a disaccharide, or starch, which is a polysaccharide.

The digestion of glucose and the burning, or combustion, of glucose follow the same chemical reaction:

$$C_6H_{12}O_6 + 6O_2 \rightarrow 6CO_2 + 6H_2O + 2808 \text{ kJ}$$
 (8)

This is the simplest and main reaction that fuels the muscle and brain activities in our body. The reaction is the reason we have to eat even if we do not grow in size any more. The required oxygen,  $O_2$ , is the reason that we breather in, and the resulting carbon dioxide,  $CO_2$ , is the reason that we breathe out. Life, in contrast to fire, is thus able to 'burn' sugar at 37°. That is one of the great wonders of nature. Inside cells, the energy gained from the digestion of sugars is converted into adenosinetriphosphate (ATP) and then converted into motion of molecules.

Chemical reactions can be slow but still dangerous. Spilling mercury on aluminium will lead to an amalgam that reduces the strength of the aluminium part after some time. That is the reason that bringing mercury thermometers on aeroplanes is strictly forbidden.

\* \*

Two atoms can form bound states by a number of effects that are weaker than electron bonds. A famous one is the bound state formed by two sodium atoms at a distance of around 60 Bohr radii, thus much larger than usual bond distances. The bond appears due to the continuous exchange of a photon between the two atoms.

What happens if you take the white powder potassium iodide - KJ - and the white powder lead nitrate –  $Pb(NO_3)_2$  – and mix them with a masher? (This needs to be done Challenge 41 s with proper protection and supervision.)

> Writing on paper with a pen filled with lemon juice instead of ink produces invisible writing. Later on, the secret writing can be made visible by carefully heating the paper on top of a candle flame.

> > \* \*

\* \*

How is the concentration of *ozone*, with the chemical composition O<sub>3</sub>, maintained in the high atmosphere? It took many years of research to show that the coolants used in refrigerators, the so-called fluoro-chloro-hydrocarbons or FCHCs, slowly destroyed this important layer. The reduction of ozone has increased the rate of skin cancer all across

the world. By forbidding the most dangerous refrigerator coolants all over the world, it is hoped that the ozone concentration can recover. The first results are encouraging. In 1995, Paul Crutzen, Mario Molina and Sherwood Rowland received the Nobel Price for Chemistry for the research that led to these results and policy changes.

In 2008, it was shown that perispinal infusion of a single substance, *etanercept*, reduced Alzheimer's symptoms in a patient with late-onset Alzheimer's disease, within a few minutes. Curing Alzheimer's disease is one of the great open challenges for modern medicine. In 2013, Jens Pahnke found that an extract of *Hypericum* has positive effects on the cognition and memory of Alzheimer patients. The extract is already available as free medication, for other uses, with the name LAIF900.

Cyanoacrylate is a fascinating substance. It is the main ingredient of instant glue, the glue that starts to harden after a few seconds of exposure to moisture. The smell of evaporating cyanoacrylate glue is strong and known to everybody who has used this kind of adhesive. The vapour also has another use: they make finger prints visible. You can try this at home!

\*

Challenge 42 e

Ref. 48

Fireworks fascinate many. A great challenge of firework technology is to produce forest green and greenish blue colours. Producers are still seeking to solve the problem. For more information about fireworks, see the cc.oulu.fi/~kempmp website.

\* \*

## MATERIALS SCIENCE

G Did you know that one cannot use a boiled egg as a toothpick? Karl Valentin

We mentioned several times that the quantum of action explains all properties of matter. Many researchers in physics, chemistry, metallurgy, engineering, mathematics and biology have cooperated in the proof of this statement. In our mountain ascent we have only a little time to explore this vast but fascinating topic. Let us walk through a selection.

## Why does the floor not fall?

We do not fall through the mountain we are walking on. Some interaction keeps us from falling through. In turn, the continents keep the mountains from falling through them. Also the liquid magma in the Earth's interior keeps the continents from sinking. All these statements can be summarized in two ideas: First, atoms do not penetrate each other: despite being mostly empty clouds, atoms keep a distance. Secondly, atoms cannot be compressed in size. Both properties are due to Pauli's exclusion principle between electrons. The fermion character of electrons avoids that atoms shrink or interpenetrate – on Earth.

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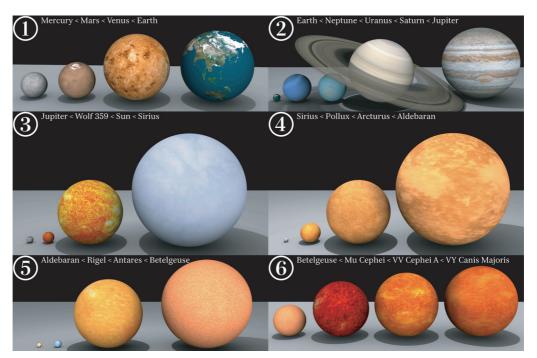


FIGURE 25 A comparison of star sizes (© Dave Jarvis).

In fact, not all floors keep up due to the fermion character of electrons. Atoms are not impenetrable at all pressures. At sufficiently large pressures, atoms can collapse, and form new types of floors. Such floors do not exist on Earth. Some people have spent their whole life to understand why such other floors, namely *surfaces of stars*, do not fall, or when they do, how it happens.

The floors and the sizes of all astronomic objects are due to quantum effects. Figure 25 illustrates the range of sizes that are found in astronomic objects. In each object, a quantum effect leads to an internal pressure which fixes the floor, and thus the size of the object.

In solid or liquid planets, the size is given by the incompressibility of condensed matter, which in turn is due to Pauli's exclusion principle. The effective internal pressure of condensed matter is often called the *Pauli pressure*. In gaseous planets, such a Jupiter, and in *usual stars*, such as in the Sun, the gas pressure takes the role that the incompressibility of solids and liquids has for smaller planets. The gas pressure is due to the heat stored in them; the heat is usually released by internal nuclear reactions.

Light pressure does play a role in determining the size of *red giants*, such as Betelgeuse; but for average stars, light pressure is negligible.

Other quantum effects appear in *dense* stars. Whenever light pressure, gas pressure and the electronic Pauli pressure cannot keep atoms from interpenetrating, atoms are compressed until all electrons are pushed into the protons. Protons then become neutrons, and the whole star has the same mass density of atomic nuclei, namely about  $2.3 \cdot 10^{17}$  kg/m<sup>3</sup>. A drop weighs about 200 000 tons. In these so-called *neutron stars*, the floor – or better, the size – is also determined by Pauli pressure; however, it is the Pauli

Page 187 pressure between neutrons, triggered by the nuclear interactions. These neutron stars are all around 10 km in radius.

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If the pressure increases still further, the star becomes a *black hole*, and never stops collapsing. Black holes have no floor at all; they still have a constant size though, determined by the horizon curvature.

The question whether other star types exist in nature, with other floor forming mechanisms – such as the conjectured *quark stars* – is still a topic of research.

# Rocks and stones

If a geologist takes a stone in his hands, he is usually able to give the age of the stone, within an error of a few per cent, simply by looking at it. The full story behind this astonishing ability forms a large part of geology, but the general lines should also be known to every physicist.

Generally speaking, the mass density of the Earth decreases from the centre towards the surface. The *upper mantle*, below the solid crust of the Earth, is mostly composed of *peridotite*, a dense, obviously igneous rock with a density of around  $3.3 \text{ g/cm}^3$ . The *oceanic crust*, with a thickness between 5 and 10 km, is mainly composed of igneous rocks such as basalt, diabase and gabbro. These rocks are somewhat less dense, around  $3 \text{ g/cm}^3$ , and are typically 200 million years old. The *continental crust* has a depth of 30 to 50 km, consists of lighter rocks, around  $2.7 \text{ g/cm}^3$ , such as granite. The age of the continental crust varies strongly; on average it is 2000 million years old, with a range from extremely young rocks to some older than 4300 million years. The continental crust contains most of the incompatible elements.

Every stone arrives in our hand through the *rock cycle(s)*. The main rock cycle is a process that transforms magma from the interior of the Earth into *igneous (or magmatic) rocks* through cooling and crystallization. Igneous rocks, such as basalt, can transform through erosion, transport and deposition into *sedimentary rocks*, such as sandstone. (Sedimentary rocks can also form from biogenic base materials.) Either of these two rock types can be transformed through high pressures or temperatures into *metamorphic rocks*, such as marble. Finally, most rocks are generally – but not always – transformed back into magma.

The main rock cycle takes around 110 to 170 million years. For this reason, rocks that are older than this age are less common on Earth. Any stone that we collect during a walk is the product of erosion of one of the rock types. A geologist can usually tell, just by looking at the stone, the type of rock it belongs to; if he sees or knows the original environment, he can also give the age and often tell the story of the formation, without any laboratory.

In the course of millions of years, minerals float upwards from the mantle or are pushed down the crust, they are transformed under heat and pressure, they dissolve or precipitate, and they get enriched in certain locations. These captivating stories about minerals are explored in detail by geologists. Geologists can tell where to find beaches with green sand (made of olivine); they can tell how contact between sedimentary limestone with molten igneous rocks leads to marble, ruby and other gemstones, and under which precise conditions; they can also tell from small crystals of quartz that enclose coesite that in earlier times the rock has been under extremely high pressure – either



**FIGURE 26** Igneous rocks (top three rows): gabbro, andesite, permatite, basalt, pumice, porphyry, obsidian, granite, tuff; sedimentary rocks (centre): clay, limestone, sandstone; and (below) two specimen of a metamorphic rock: marble (© Siim Sepp at www.sandatlas.org, Wikimedia).

Түре	Properties	Subtype	EXAMPLE
Igneous rocks (magmatites)	formed from magma, 95 % of all rocks	volcanic or extrusive	basalt (ocean floors, Giant's Causeway), andesite, obsidian
		plutonic or intrusive	granite, gabbro
Sedimentary rocks (sedimentites)	often with fossils, a few %	clastic	shale, siltstone, sandstone
		biogenic	limestone, chalk, dolostone
		precipitate	halite, gypsum
Metamorphic rocks (metamorphites)	transformed by heat and pressure, a few %	foliated	slate, schist, gneiss (Himalayas)
		non-foliated (grandoblastic or hornfelsic)	marble, skarn, quartzite
Meteorites	from the solar system	rock meteorites	
		iron meteorites	

TABLE 4 The types of rocks and stones.

because it once was at a depth of the order of 70 km, or because of an asteroid impact, or because of an atomic bomb explosion.

From the point of view of materials science, rocks are mixtures of minerals. Even though more than 5000 minerals are known, only about 200 form rocks. These rock-forming minerals can be grouped in a few general types. The main group are the silica-based rocks. They contain  $SiO_4$  tetrahedra and form around 92% of all rocks. The remaining 8% of rocks are of different composition, such as carbonates or oxides. Table 5 gives more details. The table covers the minerals found on the Earth's crust. However, the most common mineral in absolute is *Bridgmanite*, a form of MgSiO<sub>3</sub>. About one third of the Earth is made of Bridgmanite, a silicate perovskite; it is formed in the lower mantle, at temperatures of around 1800°C and pressures above 24 GPa. The mineral never appears on the Earth's crust. Recent research suggests that some forms of Bridgmanite may even have contributed, when it rose to the surface by convection, to the oxygen in the atmosphere.

Ref. 50

From the point of view of chemistry, rocks are even more uniform. 99 % of all rocks are made of only nine elements. Table 6 shows the details.

Almost all minerals are crystals. *Crystals* are solids with a regular arrangement of atoms and are a fascinating topic by themselves.

Group	M i n e r a l	Volume fraction	
Inosilicates	<i>single chain</i> silicates: pyroxenes, e.g., diopside	11(2)%	
	<i>double chain</i> silicates: amphiboles/hornblende, e.g., tremolite	5(1) %	
Phyllosilicates	<i>sheet</i> silicates:	10 (2) %	
	clays, e.g., kaolinite, talc	5(1)%	
	mica-based minerals, e.g., biotite, muscovite	5(1) %	
Tectosilicates	<i>volume</i> silicates:	65(5)%	
	quartz, tridymite, cristobalite, coesite	11(1)%	
	the plagioclase feldspar series, e.g., albite	43(4) %	
	the alkali feldspars, e.g., orthoclase	14(2) %	
Other silicates	with <i>isolated</i> , <i>double</i> or <i>cyclic</i> silica groups, e.g., olivine, beryl and garnets, or amorphous silicates, e.g., opal	3(1) %	
Oxide-based rocks	e.g., magnetite, hematite, bauxite	5(1) %	
Carbonate-based rocks	e.g., calcite, dolomite		
Sulfate-based rocks	e.g., gypsum, anhydrite		
Halide-based rocks	e.g., rock salt or halite, fluorite		
Other rocks			
	phosphates, e.g., apatite	1(0.5) %	
	sulfides, e.g., pyrite		
	native metals, e.g., gold		
	borates, e.g.,		
	and many others.		

 TABLE 5 The mineralogic composition of rocks and stones in the Earth's crust.

# CRYSTAL FORMATION

Have you ever admired a quartz crystal or some other crystalline material? The beautiful shape and atomic arrangement has formed spontaneously, as a result of the motion of atoms under high temperature and pressure, during the time that the material was deep under the Earth's surface. The details of crystal formation are complex and interesting.

Element	V o l u m e	
	FRACTION	
Oxygen	46.7(1.0) %	
Silicon	27.6(0.6) %	
Aluminium	8.1(0.1) %	
Iron	5(1) %	
Calcium	4.3(0.7) %	
Sodium	2.5(0.2) %	
Potassium	2.0(0.5) %	
Magnesium	2.5(0.4) %	
Titanium	0.5(0.1) %	
Other elements	0.8(0.8) %	

 TABLE 6
 The chemical composition of rocks and stones in the Earth's crust.

Challenge 43 s Ref. 51

Ref. 52

Ref. 53

Are regular crystal lattices *energetically optimal*? This simple question leads to a wealth of problems. We might start with the much simpler question whether a regular dense packing of spheres is the most *dense* packing possible. Its density is  $\pi/\sqrt{18}$ , i.e., a bit over 74 %. Even though this was conjectured to be the maximum possible value already in 1609 by Johannes Kepler, the statement was proven only in 1998 by Tom Hales. The proof is difficult because in small volumes it is possible to pack spheres up to almost 78 %. To show that over large volumes the lower value is correct is a tricky business.

Next, does a regular crystal of solid spheres, in which the spheres do *not* touch, really have the *highest possible entropy*? This simple problem has been the subject of research only from the 1990s onwards. Interestingly, *for low temperatures*, regular sphere arrangements indeed show the largest possible entropy. At low temperatures, spheres in a crystal can oscillate around their average position and be thus more disordered than if they were in a liquid; in the liquid state the spheres would block each other's motion and would not allow reaching the entropy values of a solid.

Many similar results deduced from the research into these so-called *entropic forces* show that the transition from solid to liquid is – at least in part – simply a geometrical effect. For the same reason, one gets the surprising result that even slightly repulsing spheres (or atoms) can form crystals and melt at higher temperatures. These are beautiful examples of how classical thinking can explain certain material properties, using from quantum theory only the particle model of matter.

But the energetic side of crystal formation provides other interesting questions. Quantum theory shows that it is possible that *two* atoms repel each other, while *three* attract each other. This beautiful effect was discovered and explained by Hans-Werner Fink in 1984. He studied rhenium atoms on tungsten surfaces and showed, as observed, that they cannot form dimers – two atoms moving together – but readily form trimers. This is an example contradicting classical physics; the effect is impossible if one pictures atoms as immutable spheres, but becomes possible when one remembers that the electron clouds around the atoms rearrange depending on their environment.

For an exact study of crystal energy, the interactions between all atoms have to be

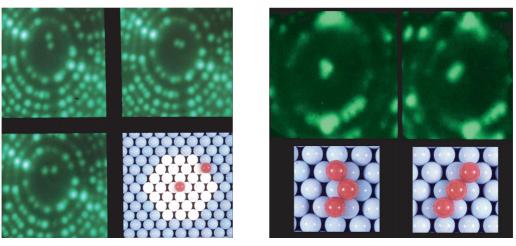


FIGURE 27 On tungsten tips, rhenium atoms, visible at the centre of the images, do not form dimers (left) but do form trimers (right) (© Hans-Werner Fink/APS, from Ref. 53).



FIGURE 28 Some snow flakes (© Furukawa Yoshinori).

included. The simplest question about crystal energy is to determine whether a regular array of alternatively charged spheres has lower energy than some irregular collection. Already such simple questions are still topic of research; the answer is still open.

The previous topics concerned bulk crystals. The next topic is the face formation in crystals. Can you confirm that crystal faces are those planes with the *slowest* growth speed, because all fast growing planes are eliminated? The finer details of the process form a complete research field in itself.

However, not always the slowest growing planes win out during crystal growth. Figure 28 shows some well-known exceptions: snow flakes. Explaining the shapes of snow flakes is possible today. Furukawa Yoshinori is one of the experts in the field, heading a dedicated research team. These explanations also settle the question of symmetry: why are crystals often symmetric, instead of asymmetric? This is a topic of self-organization, as mentioned already in the section of classical physics. It turns out that the symmetry is an automatic result of the way molecular systems grow under the combined influence of diffusion and non-linear growth processes. But as usual, the details are still a topic of research.

Challenge 44 s Ref. 54

Ref. 55

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## Some interesting crystals

Every crystal, like every structure in nature, is the result of growth. Every crystal is thus the result of motion. To form a crystal whose regularity is as high as possible and whose shape is as symmetric as possible, the required motion is a *slow* growth of facets from the liquid (or gaseous) basic ingredients. The growth requires a certain pressure, temperature and temperature gradient for a certain time. For the most impressive crystals, the gemstones, the conditions are usually quite extreme; this is the reason for their durability. The conditions are realized in specific rocks deep inside the Earth, where the growth process can take thousands of years. Mineral crystals can form in all three types of rocks: igneous (magmatic), metamorphic, and sedimentary. Other crystals can be made in the laboratory in minutes, hours or days and have led to a dedicated industry. Only a few crystals grow from liquids at standard conditions; examples are gypsum and several other sulfates, which can be crystallized at home, potassium bitartrate, which appears in the making of wine, and the crystals grown inside plants or animals, such as teeth, bones or magnetosensitive crystallites.

Growing, cutting, treating and polishing crystals is an important industry. Especially the growth of crystals is a science in itself. Can you show with pencil and paper that only the *slowest* growing facets are found in crystals? In the following, a few important crystals are presented.



FIGURE 29 Quartz found at St. Gotthard, Switzerland, picture size 12 cm (© Rob Lavinsky).

FIGURE 30 Citrine

found on Magaliesberg, South Africa, crystal height 9 cm (© Rob Lavinsky).



FIGURE 31 Amethystine and orange guartz found in the Orange River, Namibia, picture size 6 cm (© Rob Lavinsky).

\* \*

Quartz, amethyst (whose colour is due to radiation and iron Fe<sup>4+</sup> impurities), citrine (whose colour is due to  $Fe^{3+}$  impurities), *smoky quartz* (with colour centres induced by radioactivity), agate and onyx are all forms of crystalline silicon dioxide or SiO<sub>2</sub>. Quartz forms in igneous and in magmatic rocks; crystals are also found in many sedimentary rocks. Quartz crystals can sometimes be larger than humans. By the way, most amethysts

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Challenge 45 e

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lose their colour with time, so do not waste money buying them.

Quartz is the most common crystal on Earth's crust and is also grown synthetically for many high-purity applications. The structure is rombohedral, and the ideal shape is a six-sided prism with six-sided pyramids at its ends. Quartz melts at 1986 K and is piezoand pyroelectric. Its piezoelectricity makes it useful as electric oscillator and filter. A film of an oscillating clock quartz is found in the first volume. Quartz is also used for glass production, in communication fibres, for coating of polymers, in gas lighters, as source of silicon and for many other applications.



FIGURE 32 Corundum found in Laacher See, Germany, picture size 4 mm (© Stephan Wolfsried).



FIGURE 33 Ruby found in Jagdalak, Afghanistan, picture height 2 cm (© Rob Lavinsky).

FIGURE 34 Sapphire found in Ratnapura, Sri Lanka, size 1.6 cm (© Rob

Lavinsky).

\* \*

*Corundum*, *ruby* and *sapphire* are crystalline variations of alumina, or  $Al_2O_3$ . Corundum is pure and colourless crystalline alumina, ruby is Cr doped and blue sapphire is Ti or Fe doped. They have trigonal crystal structure and melt at 2320 K. Natural gems are formed in metamorphic rocks. Yellow, green, purple, pink, brown, grey and salmon-coloured sapphires also exist, when doped with other impurities. The colours of natural sapphires, like that of many other gemstones, are often changed by baking and other treatments.

Corundum, ruby and sapphire are used in jewellery, as heat sink and growth substrate, and for lasers. Corundum is the second-hardest material known, just after diamond, and is therefore used as scratch-resistant 'glass' in watches and, since a short time, in mobile phones. Ruby was the first gemstone that was grown synthetically in gem quality, in 1892 by Auguste Verneuil (1856-1913), who made his fortune in this way. Modern synthetic single crystals of corundum can weigh 30 kg and more. Also alumina ceramics, which can be white or even transparent, are important in industrial and medical systems.

Tourmaline is a frequently found mineral and can be red, green, blue, orange, yellow,



FIGURE 35 Left: raw crystals, or boules, of synthetic corundum, picture size c. 50 cm. Right: a modern, 115 kg corundum single crystal, size c. 50 cm (© Morion Company, GT Advanced).

pink or black, depending on its composition. The chemical formula is astonishingly complex and varies from type to type. Tourmaline has trigonal structure and usually forms columnar crystals that have triangular cross-section. It is only used in jewellery. Paraiba tourmalines, a very rare type of green or blue tourmaline, are among the most beautiful gemstones and can be, if natural and untreated, more expensive than diamonds.



FIGURE 36 Natural F bicoloured E tourmaline found in Paprok, Afghanistan, picture size 9 cm (© Rob Lavinsky).

FIGURE 37 Cut Paraiba tourmaline from Brazil, picture size 3 cm (© Manfred Fuchs).

\* \*

*Garnets* are a family of compounds of the type  $X_2Y_3(SiO_4)_3$ . They have cubic crystal structure. They can have any colour, depending on composition. They show no cleavage and their common shape is a rhombic dodecahedron. Some rare garnets differ in col-

our when looked at in daylight or in incandescent light. Natural garnets form in metamorphic rocks and are used in jewellery, as abrasive and for water filtration. Synthetic garnets are used in many important laser types.



FIGURE 38 Red garnet with smoky quartz found in Lechang, China, picture size 9 cm (© Rob Lavinsky).



FIGURE 39 Green demantoid, a garnet owing its colour to chromium doping, found in Tubussis, Namibia, picture size 5 cm (© Rob Lavinsky).



FIGURE 40 Synthetic Cr,Tm,Ho:YAG, a doped yttrium aluminium garnet, picture size 25 cm (© Northrop Grumman).

\* \*

Alexandrite, a chromium-doped variety of *chrysoberyl*, is used in jewellery and in lasers. Its composition is  $BeAl_2O_4$ ; the crystal structure is orthorhombic. Chrysoberyl melts at 2140 K. Alexandrite is famous for its colour-changing property: it is green in daylight or fluorescent light but amethystine in incandescent light, as shown in Figure 38. The effect is due to its chromium content: the ligand field is just between that of chromium in red ruby and that in green emerald. A few other gems also show this effect, in particular the rare blue garnet and some Paraiba tourmalines.



FIGURE 41 Alexandrite found in the Setubal river, Brazil, crystal height 1.4 cm, illuminated with daylight (left) and with incandescent light (right) (© Trinity Mineral).



**FIGURE 42** Synthetic alexandrite, picture size 20 cm (© Northrop Grumman).

#### \* \*

*Perovskites* are a large class of cubic crystals used in jewellery and in tunable lasers. Their general composition is XYO<sub>3</sub>, XYF<sub>3</sub> or XYCl<sub>3</sub>.



FIGURE 43 Perovskite found in Hillesheim, Germany. Picture width 3 mm (© Stephan Wolfsried).



FIGURE 44 Synthetic PZT, or lead zirconium titanate, is a perovskite used in numerous products. Picture width 20 cm (© Ceramtec).

*Diamond* is a metastable variety of *graphite*, thus pure carbon. Theory says that graphite is the stable form; practice says that diamond is still more expensive. In contrast to graphite, diamond has face-centred cubic structure, is a large band gap semiconductor and typically has octahedral shape. Diamond burns at 1070 K; in the absence of oxygen it converts to graphite at around 1950 K. Diamond can be formed in magmatic and in metamorphic rocks. Diamonds can be synthesized in reasonable quality, though gemstones of large size and highest quality are not yet possible. Diamond can be coloured and be doped to achieve electrical conductivity in a variety of ways. Diamond is mainly used in jewellery, for hardness measurements and as abrasive.

Silicon, Si, is not found in nature in pure form; all crystals are synthetic. The structure is face-centred cubic, thus diamond-like. It is moderately brittle, and can be cut in thin wafers which can be further thinned by grinding or chemical etching, even down to a thickness of  $10 \,\mu\text{m}$ . Being a semiconductor, the band structure determines its black colour, its metallic shine and its brittleness. Silicon is widely used for silicon chips and electronic semiconductors. Today, human-sized silicon crystals can be grown free of dislocations and other line defects. (They will still contain some point defects.)

*Teeth* are the structures that allowed animals to be so successful in populating the Earth. They are composed of several materials; the outer layer, the *enamel*, is 97 % hydroxylapatite, mixed with a small percentage of two proteins groups, the amelogenins and the enamelins. The growth of teeth is still not fully understood; neither the molecular level nor the shape-forming mechanisms are completely clarified. Hydroxylapatite is soluble in acids; addition of fluorine ions changes the hydroxylapatite to fluorapatite and greatly reduces the solubility. This is the reason for the use of fluorine in tooth paste.

Hydroxylapatite (or hydroxyapatite) has the chemical formula Ca<sub>10</sub>(PO<sub>4</sub>)<sub>6</sub>(OH)<sub>2</sub>, pos-



FIGURE 45 Natural diamond from Saha republic, Russia, picture size 4 cm (© Rob Lavinsky).



FIGURE 46 Synthetic diamond, picture size 20 cm (© Diamond Materials GmbH).



FIGURE 47 Ophthalmic diamond knife, picture size 1 cm (© Diamatrix Ltd.).

sesses hexagonal crystal structure, is hard (more than steel) but relatively brittle. It occurs as mineral in sedimentary rocks (see Figure 49), in bones, renal stones, bladders tones, bile stones, atheromatic plaque, cartilage arthritis and teeth. Hydroxylapatite is mined as a phosphorus ore for the chemical industry, is used in genetics to separate single and double-stranded DNA, and is used to coat implants in bones.

\* \*

*Pure metals*, such as *gold*, *silver* and even *copper*, are found in nature, usually in magmatic rocks. But only a few metallic compounds form crystals, such as *pyrite*. Monocrystalline pure metal crystals are all synthetic. Monocrystalline metals, for example iron, aluminium, gold or copper, are extremely soft and ductile. Either bending them repeatedly – a process called cold working – or adding impurities, or forming alloys makes them hard and strong. Stainless steel, a carbon-rich iron alloy, is an example that uses all three processes.

\* \*

In 2009, Luca Bindi of the Museum of Natural History in Florence, Italy, made headlines



**FIGURE 48** A silicon crystal growing machine and two resulting crystals, with a length of c. 2 m (© www.pvatepla.com).

Ref. 56 across the world with his discovery of the first natural *quasicrystal*. Quasicrystals are materials that show non-crystallographic symmetries. Until 2009, only synthetic materials were known. Then, in 2009, after years of searching, Bindi discovered a specimen in his collection whose grains clearly show fivefold symmetry.

There are about 4000 known mineral types. On the other hand, there are ten times as many obsolete mineral names, namely around 40 000. An official list can be found in

\* \*



FIGURE 49 Hydroxylapatite found in Oxsoykollen, Snarum, Norway, length 65 mm (© Aksel Österlöf).



FIGURE 50 The main and the reserve teeth on the jaw bone of a shark, all covered in hydroxylapatite, picture size 15 cm (© Peter Doe).



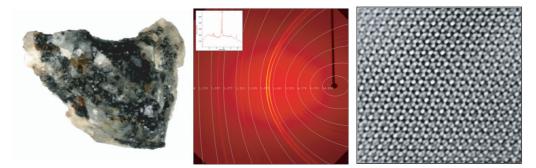
FIGURE 51 Pyrite, found in Navajún, Spain, picture width 5.7 cm (© Rob Lavinsky).



FIGURE 52 Silver from Colquechaca, Bolivia, picture width 2.5 cm (© Rob Lavinsky).



FIGURE 53 Synthetic copper single crystal, picture width 30 cm (© Lachlan Cranswick).



**FIGURE 54** The specimen, found in the Koryak Mountains in Russia, is part of a triassic mineral, about 220 million years old; the black material is mostly khatyrkite ( $CuAl_2$ ) and cupalite ( $CuAl_2$ ) but also contains quasicrystal grains with composition  $Al_{63}Cu_{24}Fe_{13}$  that have fivefold symmetry, as clearly shown in the X-ray diffraction pattern and in the transmission electron image. (© Luca Bindi).

various places on the internet, including www.mindat.org or www.minieralienatlas.de. To explore the world of crystal shapes, see the www.smorf.nl website. Around 40 new minerals are discovered each year. Searching for minerals and collecting them is a fascinating pastime.

## How can we look through matter?

Vol. IV, page 28

The quantum of action tells us that all obstacles have only finite potential heights. The quantum of action implies that matter is penetrable. That leads to a question: Is it possible to look through solid matter? For example, can we see what is hidden inside a mountain? To achieve this, we need a signal which fulfils two conditions: the signal must be able to *penetrate* the mountain, and it must be scattered in a *material-dependent* way. Indeed, such signals exist, and various techniques use them. Table 7 gives an overview of the possibilities.

Signal	Penet - ration depth	A C H I E - V E D R E S O L U -	M a - terial de -	U s e
	IN STONE	ΤΙΟΝ	P E N D - E N C E	
Fluid signals				
Diffusion of gases, such as helium	c. 5 km	<i>c</i> . 100 m	medium	exploring vacuum systems and tube systems
Diffusion of water or liquid chemicals	c. 5 km	<i>c</i> . 100 m	medium	mapping hydrosystems
Sound signals				
Infrasound and earthquakes	100 000 km	100 km	high	mapping of Earth crust and mantle
Sound, explosions, short seismic waves	0.1 – 10 m	<i>c</i> . λ/100	high	oil and ore search, structure mapping in rocks, searching for underwater treasures in sunken ship with sub-bottom-profilers
Ultrasound		1 mm	high	medical imaging, acoustic microscopy, sonar, echo systems
Acousto-optic or photoacoustic imaging		1 mm	medium	blood stream imaging, mouse imaging
Electromagnetic sig	nals			
Static magnetic field variations			medium	cable search, cable fault localization, search for structures and metal inside soil, rocks and the seabed
Electrical currents				soil and rock investigations, search for tooth decay
Electromagnetic sounding, 0.2 – 5 Hz				soil and rock investigations in deep water and on land
Radio waves	10 m	30 m to 1 mm	small	soil radar (up to 10 MW), magnetic resonance imaging, research into solar interior

TABLE 7 Signals penetrating mountains and other matter.

SIGNAL	PENET - RATION DEPTH IN STONE	A C H I E - V E D R E S O L U - T I O N	M A - T E R I A L D E - P E N D - E N C E	U S E
Ultra-wide band radio	10 cm	1 mm	sufficient	searching for wires and tubes in walls, breast cancer detection
THz and mm waves	below 1 mm	1 mm		see through clothes, envelopes and teeth Ref. 57
Infrared	<i>c</i> . 1 m	0.1 m	medium	mapping of soil over 100 m
Visible light	<i>c</i> . 1 cm	0.1 µm	medium	imaging of many sorts, including breast tumour screening
X-rays	a few metres	5 µm	high	medicine, material analysis, airports, food production check
γ-rays	a few metres	1 mm	high	medicine
Matter particle signa	als			
Neutrons from a reactor	up to <i>c</i> . 1 m	l mm	medium	tomography of metal structures, e.g., archaeologic statues or car engines
Muons created by cosmic radiation or technical sources	up to c. 300 m	0.1 m	small	finding caves in pyramids, imaging interior of trucks
Positrons	up to <i>c</i> . 1 m	2 mm	high	brain tomography
Electrons	up to <i>c</i> . 1 μm	10 nm	small	transmission electron microscopes
Neutrino beams	light years	none	very weak	studies of Sun
Radioactivity mapping	1 mm to 1 m			airport security checks
Gravitation				
Variation of $g$		50 m	low	oil and ore search

TABLE 7 (Continued) Signals penetrating mountains and other matter.

We see that many signals are able to penetrate a mountain, and even more signals are able to penetrate other condensed matter. To distinguish different materials, or to distinguish solids from liquids and from air, sound and radio waves are the best choice. In addition, any useful method requires a large number of signal sources and of signal receptors, and thus a large amount of money. Will there ever be a simple method that allows looking into mountains as precisely as X-rays allow looking into human bodies? For example, is it possible to map the interior of the pyramids? A motion expert should be able to give a definite answer.

Challenge 46 s

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method so far to look into matter with dimensions of about a metre or less: magnetic resonance imaging. We will discuss it later on.

Various modern imaging techniques, such as X-rays, ultrasound imaging and several

One of the high points of twentieth century physics was the development of the best

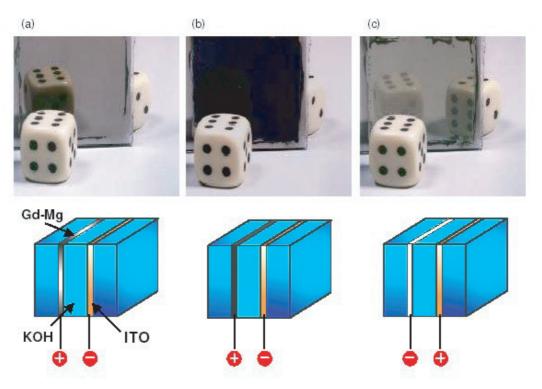


FIGURE 55 A switchable Mg-Gd mirror (© Ronald Griessen).

Vol. I, page 313 Vol. I, page 313 future ones, are useful in medicine. As mentioned before, the use of ultrasound imaging for prenatal diagnostics of embryos is not recommended. Studies have found that ultrasound produces extremely high levels of audible sound to the embryo, especially when the ultrasound is repeatedly switched on and off, and that babies react negatively to this loud noise.

Looking into the ground is important for another reason. It can help in *locating land mines*. Detecting land mines, especially metal-free mines, buried in the ground is a big technological challenge that is still unsolved. Many technologies have been tested: X-ray backscatter devices working at 350 to 450 keV, ground-penetrating radar and ultra-wideband radar, infrared detection, thermal or fast neutron bombardment and analysis, acoustic and sonar detection, electric impedance tomography, radio-frequency bombardment, nuclear quadrupole resonance, millimetre waves, visual detection, ion mobility spectrometers, using dogs, using rats, and explosive vapour detection with dedicated sensors. (And of course, for metallic mines, magnetometers and metal detectors are used.) But so far, the is still no solution in sight. Can you find one? If you do, get in touch with www.gichd.org.

## WHAT IS NECESSARY TO MAKE MATTER INVISIBLE?

You might have already imagined what adventures would be possible if you could be *invisible* for a while. In 1996, a team of Dutch scientists found a material, yttrium hydride or  $YH_3$ , that can be switched from mirror mode to transparent mode using an electrical

Ref. 58 signal. A number of other materials were also discovered. An example of the effect for Mg-Gd layers is shown in Figure 55.

Switchable mirrors might seem a first step to realize the dream to become invisible and visible at will. In 2006, and repeatedly since then, researchers made the headlines in the popular press by claiming that they could build a *cloak of invisibility*. This is a blatant lie. This lie is frequently used to get funding from gullible people, such as buyers of bad science fiction books or the military. For example, it is often claimed that objects can be made invisible by covering them with metamaterials. The impossibility of this aim has been already shown earlier on. But we now can say more.

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Nature shows us how to realize invisibility. An object is invisible if it has no surface, no absorption and small size. In short, invisible objects are either small clouds or composed of them. Most atoms and molecules are examples. Homogeneous non-absorbing gases also realize these conditions. That is the reason that air is (usually) invisible. When air is not homogeneous, it can be visible, e.g. above hot surfaces.

In contrast to gases, solids or liquids do have surfaces. Surfaces are usually visible, even if the body is transparent, because the refractive index changes there. For example, quartz can be made so transparent that one can look through 1 000 km of it; pure quartz is thus *more* transparent than usual air. Still, objects made of pure quartz are visible to the eye, due to their refractive index. Quartz can be invisible only when submerged in liquids with the same refractive index.

In short, anything that has a shape cannot be invisible. If we want to become invisible, we must transform ourselves into a diffuse gas cloud of non-absorbing atoms. On the way to become invisible, we would lose all memory and all genes, in short, we would lose all our individuality, because an individual cannot be made of gas. An individual is defined through its boundary. There is no way that we can be invisible and alive at the same time; a way to switch back to visibility is even less likely. In summary, quantum theory shows that only the dead can be invisible. Quantum theory has a reassuring side: we already found that quantum theory forbids ghosts; we now find that it also forbids any invisible beings.

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## WHAT MOVES INSIDE MATTER?

All matter properties are due to the motion of the components of matter. Therefore, we can correctly argue that understanding the motion of electrons and nuclei implies understanding all properties of matter. Sometimes, however, it is more practical to explore the motion of collections of electrons or nuclei as a whole. Here is a selection of such collective motions. Collective motions that appear to behave like single particles are called *quasiparticles*.

In crystalline solids, sound waves can be described as the motion of *phonons*. For example, transverse phonons and longitudinal phonons describe many processes in semiconductors, in solid state lasers and in ultrasound systems. Phonons approximately behave as bosons.

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In metals, the motion of crystal defects, the so-called *dislocations* and *disclinations*, is central to understand their hardening and their breaking.

Also in metals, the charge waves of the conductive electron plasma, can be seen as composed of so-called *plasmons*. Plasmons are also important in the behaviour of high-

speed electronics.

In magnetic materials, the motion of spin orientation is often best described with the help of magnons. Understanding the motion of magnons and that of magnetic domain walls is useful to understand the magnetic properties of magnetic material, e.g., in permanent magnets, magnetic storage devices, or electric motors. Magnons behave approximately like bosons.

In semiconductors and insulators, the motion of *conduction electrons* and *electron holes*, is central for the description and design of most electronic devices. They behave as fermions with spin 1/2, elementary electric charge, and a mass that depends on the material, on the specific conduction band and on the specific direction of motion. The bound system of a conduction electron and a hole is called an *exciton*. It can have spin 0 or spin 1.

In polar materials, the motion of light through the material is often best described in terms of *polaritons*, i.e., the coupled motion of photons and dipole carrying material excitations. Polaritons are approximate bosons.

In dielectric crystals, such as in many inorganic ionic crystals, the motion of an electron is often best described in terms of *polarons*, the coupled motion of the electron with the coupled polarization region that surrounds it. Polarons are fermions.

In fluids, the motion of vortices is central in understanding turbulence or air hoses. Especially in superfluids, vortex motion is quantized in terms of *rotons* which determines flow properties. Also in fluids, bubble motion is often useful to describe mixing processes.

In superconductors, not only the motion of *Cooper pairs*, but also the motion of *magnetic flux tubes* determines the temperature behaviour. Especially in thin and flat super-conductors – so-called 'two-dimensional' systems – such tubes have particle-like properties.

In all condensed matter systems, the motion of *surface states* – such as surface magnons, surface phonons, surface plasmons, surface vortices – has also to be taken into account.

Many other, more exotic *quasiparticles* exist in matter. Each quasiparticle in itself is an important research field where quantum physics and material science come together. To clarify the concepts, we mention that a *soliton* is not, in general, a quasiparticle. 'Soliton' is a mathematical concept; it applies to macroscopic waves with only one crest that remain unaltered after collisions. Many domain walls can be seen as solitons. But quasiparticles are concepts that describe physical observations similar to quantum particles.

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In summary, all the mentioned examples of collective motion inside matter, both macroscopic and quantized, are of importance in electronics, photonics, engineering and medical applications. Many are quantized and their motion can be studied like the motion of real quantum particles.

## CURIOSITIES AND FUN CHALLENGES ABOUT MATERIALS SCIENCE

Ref. 59

What is the maximum height of a mountain? This question is of course of interest to all climbers. Many effects limit the height. The most important is that under heavy pressure, solids become liquid. For example, on Earth this happens for a mountain with a height of about 27 km. This is quite a bit more than the highest mountain known, which is

Challenge 47 ny

\* \*

Challenge 48 s

Challenge 49 r

Page 299

Do you want to become rich? Just invent something that can be produced in the factory, is cheap and can fully substitute duck feathers in bed covers, sleeping bags or in badminton shuttlecocks. Another industrial challenge is to find an artificial substitute for latex, and a third one is to find a substitute for a material that is rapidly disappearing due to pollution: cork.

\* \*

Materials differ in density, in elasticity, in strength, stiffness, toughness, melting temperature, heat insulation, electric resistivity, and many other parameters. To get an overview, the so-called *Ashby charts* are most useful, of which Figure 56 shows an example. The race to find materials that are lighter and stiffer than wood, in particular balsa wood, is still ongoing.

\* \*

\* \*

How much does the Eiffel tower change in height over a year due to thermal expansion challenge 50 s and contraction?

What is the difference between the makers of bronze age knifes and the builders of the Eiffel tower? Only their control of defect distributions. The main defects in metals are *disclinations* and *dislocations*. Disclinations are crystal defects in form of surfaces; they are the microscopic aspect of grain boundaries. Dislocations are crystal defects in form of curved lines; above all, their distribution and their motion in a metal determines the stiffness. For a picture of dislocations, see below.

Challenge 51 e What is the difference between solids, liquids and gases?

One subject of materials science is the way a solid object breaks. The main distinction is between *brittle* fraction and *ductile* fraction. In brittle fraction, as in a breaking of a glass pane, the resulting edges are sharp and irregular; in ductile fraction, as occurs in hot glass, the edges are rounded and regular. The two fraction types also differ in their mechanisms, i.e., in the motion of the involved defects and atoms. This difference is important: when a car accident occurs at night, looking at the shapes of the fraction surface of the tungsten wire inside the car lamps with a microscope, it is easy to decide whether the car lamps were on or off at the time of the accident.

\*

\* \*

Material science can also help to make erased information visible again. Many laborat-

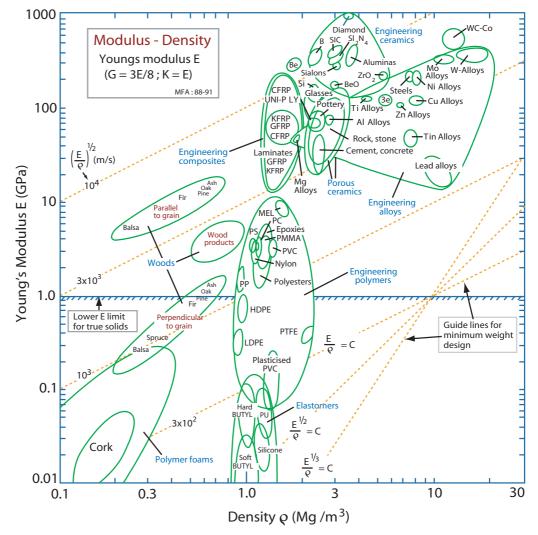


FIGURE 56 An overview of the elastic modulus and the density of materials. For structures that need to be light and stiff, a high ratio E /  $\rho^3$  is required; the graph shows that wood is well optimized for this task. (© Carol Livermore/Michael Ashby).

ories are now able to recover data from erased magnetic hard disks. Other laboratories can make erased serial numbers in cars bodies visible again, either by heating the metal part or by using magnetic microscopy.

\* \*

Quantum theory shows that tight walls do not exist. Every material is penetrable. Why? Challenge 52 s

> \* Quantum theory shows that even if tight walls would exist, the lid of a box made of such

\*

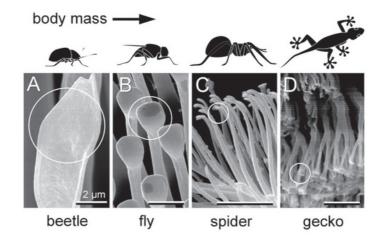


FIGURE 57 Insects and geckos stick to glass and other surfaces using the van der Waals force at the ends of a high number of spatulae (© Max Planck Gesellschaft).

## Challenge 53 s walls can never be tightly shut. Can you provide the argument?

\* \*

In 1936, Henry Eyring proposed that the shear viscosity of a liquid  $\eta$  obeys

$$\eta \ge \rho \hbar , \qquad (9)$$

Challenge 54 ny where  $\rho$  is the density of the fluid. Is the lower limit valid?

Heat can flow. Like for all flows, quantum theory predicts that heat transport quantized. This implied that thermal conductance is quantized. And indeed, in the year 2000, experiments have confirmed the prediction. Can you guess the smallest unit of thermal conductance?

\*

\*

Ref. 61 Vol. I, page 91

Challenge 55 s

Ref. 60

Robert Full has shown that van der Waals forces are responsible for the way that geckos walk on walls and ceilings. (A picture is found in Figure 56.) The gecko, a small reptile with a mass of about 100 g, uses an elaborate structure on its feet to perform the trick. Each foot has 500 000 hairs or setae, each split in up to 1000 small spatulae, and each spatula uses the van der Waals force (or alternatively, capillary forces) to stick to the surface. As a result of these 500 million sticking points, the gecko can walk on vertical glass walls or even on glass ceilings; the sticking force can be as high as 100 N per foot. The adhesion forces are so high that detaching the foot requires a special technique. The internet has slow-motion videos showing how geckos perform the feat, in each step they take.

Hairy feet as adhesion method are also used by jumping spiders (*Salticidae*). For example, *Evarcha arcuata* have hairs at their feet which are covered by hundred of thou-

Ref. 62 sands of setulae. Again, the van der Waals force in each setula helps the spider to stick on surfaces. Also many insects use small hairs for the same aim. Figure 57 shows a comparison. Researchers have shown that the hairs – or setae – are finer the more massive the animal is. Eduard Arzt likes to explain that small flies and beetles have simple, spherical setae with a diameter of a few micrometers whereas the considerably bigger and heavier geckos have branched nanohairs with diameters of 200 nm.

Researchers have copied the hairy adhesion mechanism for the first time in 2003, using microlithography on polyimide, and they hope to make durable sticky materials – without using any glue – in the future.

\* \*

One of the most fascinating materials in nature are bones. Bones are light, stiff, and can heal after fractures. If you are interested in composite materials, read more about bones: their structure, shown in Figure 58, and their material properties are fascinating and complex, and so are their healing and growth mechanisms. All these aspects are still subject of research.

A cereal stalk has a height-to-width ratio of about 300. No human-built tower or mast achieves this. Why?

\*

Millimetre waves or terahertz waves are emitted by all bodies at room temperature. Modern camera systems allow producing images with them. In this way, it is possible to see through clothes, as shown by Figure 59. (Caution is needed; there is the widespread suspicion that the image is a fake produced to receive more development funding.) This ability could be used in future to detect hidden weapons in airports. But the development of a practical and affordable detector which can be handled as easily as a binocular is still under way. The waves can also be used to see through paper, thus making it unnecessary to open letters in order to read them. Secret services are exploiting this technique. A third application of terahertz waves might be in medical diagnostic, for example for the search of tooth decay. Terahertz waves are almost without side effects, and thus superior to X-rays. The lack of low-priced quality sources is still an obstacle to their application.

Does the melting point of water depend on the magnetic field? This surprising claim was
 made in 2004 by Inaba Hideaki and colleagues. They found a change of 0.9 mK/T. It is known that the refractive index and the near infrared spectrum of water is affected by magnetic fields. Indeed, not everything about water might be known yet.

\* \*

Plasmas, or ionized gases, are useful for many applications. A few are shown in Figure 60. Not only can plasmas be used for heating or cooking and generated by chemical means (such plasmas are variously called fire or flames) but they can also be generated electrically and used for lighting or deposition of materials. Electrically generated plasmas are even being studied for the disinfection of dental cavities.

Ref. 64

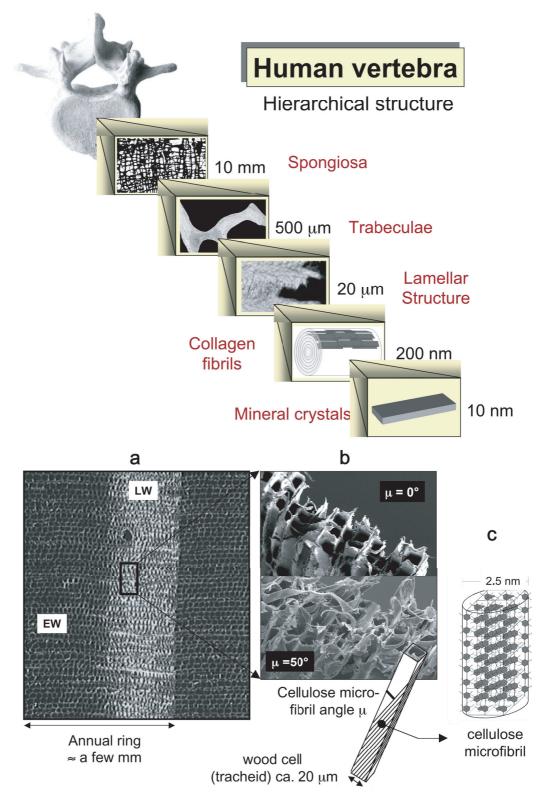


FIGURE 58 The structure of bones, shown for a human vertebra (© Peter Fratzl and Physik Journal).



FIGURE 59 An alleged image acquired with terahertz waves. Can you explain why it is a fake? (© Jefferson Lab)

\* \*

Ref. 66 Challenge 57 s

It is known that the concentration of  $CO_2$  in the atmosphere between 1800 and 2005 has increased from 280 to 380 parts per million, as shown in Figure 61. (In 2016, the value was already 403 ppm. How would you measure this?) It is known without doubt that this increase is due to human burning of fossil fuels, and not to natural sources such as the oceans or volcanoes. There are three arguments. First of all, there was a parallel decline of the  ${}^{14}C/{}^{12}C$  ratio. Second, there was a parallel decline of the  ${}^{13}C/{}^{12}C$  ratio. Finally, there was a parallel decline of the oxygen concentration. All three measurements independently imply that the CO<sub>2</sub> increase is due to the burning of fuels, which are low in <sup>14</sup>C and in <sup>13</sup>C, and at the same time decrease the oxygen ratio. Natural sources do not have these three effects. Since  $CO_2$  is a major greenhouse gas, the data implies that humans are also responsible for a large part of the temperature increase during the same period. Global warming exists and is mainly due to humans. On average, the Earth has cooled over the past 10 million years; since a few thousand years, the temperature has, however, slowly risen; together with the fast rise during the last decades the temperature is now at the same level as 3 million years ago. How do the decade global warming trend, the thousand year warming trend and the million year cooling trend interact? This is a topic of intense research.

Making crystals can make one rich. The first man who did so, the Frenchman Auguste Verneuil (b. 1856 Dunkerque, d. 1913 Paris), sold rubies grown in his laboratory for many years without telling anybody. Many companies now produce synthetic gems with machines that are kept secret. An example is given in Figure 62.

\* \*

Synthetic diamonds have now displaced natural diamonds in almost all applications. In the last years, methods to produce large, white, jewel-quality diamonds of ten carats and more are being developed. These advances will lead to a big change in all the domains that depend on these stones, such as the production of the special surgical knives used in eye lens operation.

Motion Mountain – The Adventure of Physics 🛛 copyright © Christoph Schiller June 1990–May 2020 🛛 free pdf file available at www.motionmounta

Ref. 68

Ref. 67

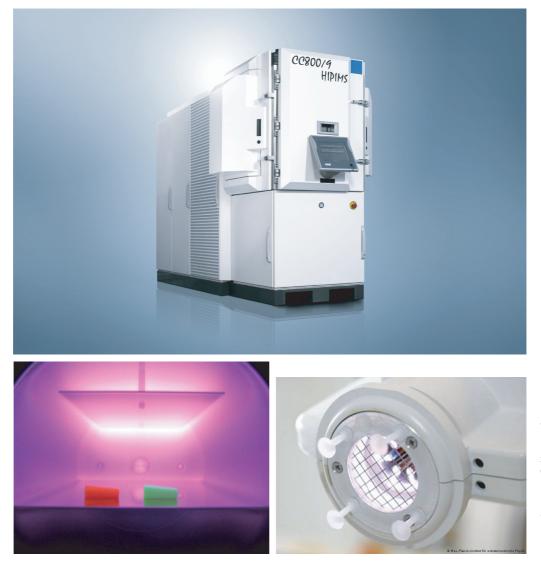


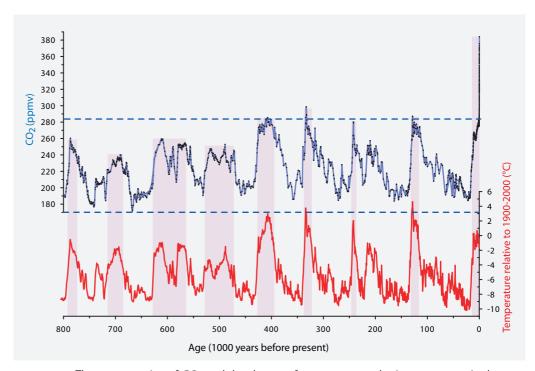
FIGURE 60 Some plasma machines: a machine for coating metal parts, a machine for cleaning polymer parts and a device for healing wounds (© www.cemecon.de, www.diener.de, Max Planck Gesellschaft).

\* \*

The technologies to produce *perfect* crystals, without grain boundaries or dislocations, are an important part of modern industry. Perfectly regular crystals are at the basis of the integrated circuits used in electronic appliances, are central to many laser and tele-communication systems and are used to produce synthetic jewels.

\* \*

Challenge 58 s How can a small plant pierce through tarmac?



**FIGURE 61** The concentration of CO<sub>2</sub> and the change of average atmospheric temperature in the past 0.8 million years (© Dieter Lüthi).

If you like abstract colour images, do not miss looking at liquid crystals through a microscope. You will discover a wonderful world. The best introduction is the text by Ingo Dierking.

\* \*

Ref. 69 I

The Lorentz force leads to an interesting effect inside materials. If a current flows along a conducting strip that is in a (non-parallel) magnetic field, a voltage builds up between two edges of the conductor, because the charge carriers are deflected in their flow. This effect is called the (classical) *Hall effect* after the US-American physicist Edwin Hall (b. 1855 Great Falls, d. 1938 Cambridge), who discovered it in 1879, during his PhD. The effect, shown in Figure 63, is regularly used, in so-called *Hall probes*, to measure magnetic fields; the effect is also used to read data from magnetic storage media or to measure electric currents (of the order of 1 A or more) in a wire without cutting it. Typical Hall probes have sizes of around 1 cm down to 1  $\mu$ m and less. The Hall voltage V turns out to be given by

$$V = \frac{IB}{ned} , \qquad (10)$$

where n is the electron number density, e the electron charge, and d is the thickness of the probe, as shown in Figure 63. Deducing the equation is a secondary school exercise. The Hall effect is a material effect, and the material parameter n determines the Hall voltage. The sign of the voltage also tells whether the material has positive or negative

Challenge 59 e

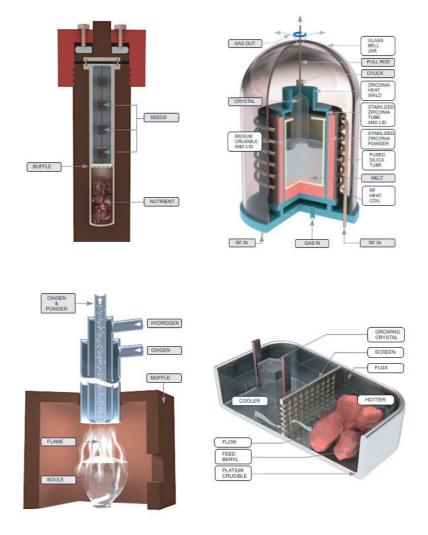


FIGURE 62 Four crystal and synthetic gemstone growing methods. Top: the hydrothermal technique, used to grow emeralds, quartz, rock crystal and amethyst, and Czochralski's pulling technique, used for growing ruby, sapphire, spinel, yttrium-aluminium-garnet, gadolinium-gallium-garnet and alexandrite. Bottom: Verneuil's flame fusion technique, used for growing corundum, sapphire, ruby and spinel boules, and the flux process, used for chrysoberyl (© Ivan Golota).

Challenge 60 e

Page 108

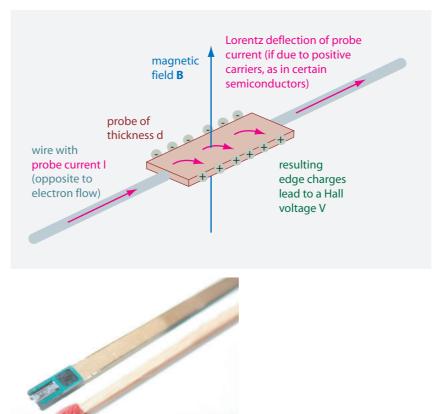
Ref. 70

charge carriers; indeed, for metal strips the voltage polarity is opposite to the one shown in the figure. Many variations of the Hall effect have been studied. For example, the *quantum* Hall

effect and the fractional quantum Hall effect will be explored below.

In 1998, Geert Rikken and his coworkers found that in certain materials photons can also be deflected by a magnetic field; this is the *photonic Hall effect*.

In 2005, again Geert Rikken and his coworkers found a material, a terbium gallium garnet, in which a flow of phonons in a magnetic field leads to temperature difference on



## FIGURE 63 Top: the (classical) Hall effect. Bottom: a modern miniature Hall probe using the effect to measure magnetic fields (© Metrolab).

Ref. 71 the two sides. They called this the *phonon Hall effect*.

Do magnetic fields influence the crystallization of calcium carbonate in water? This issue
 is topic of intense debates. It might be, or it might not be, that magnetic fields change the crystallization seeds from calcite to aragonite, thus influencing whether water tubes are covered on the inside with carbonates or not. The industrial consequences of reduction in *scaling*, as this process is called, would be enormous. But the issue is still open, as are convincing data sets.

\* \*

\*

**Ref. 73** It has recently become possible to make the thinnest possible sheets of graphite and other materials (such as BN,  $MoS_2$ ,  $NbSe_2$ ,  $Bi_2Sr_2CaCu_2O_x$ ): these crystal sheets are precisely one atom thick! The production of *graphene* – that is the name of a monoatomic graphite layer – is extremely complicated: you need graphite from a pencil and a roll of adhesive tape. That is probably why it was necessary to wait until 2004 for the development of the technique. (In fact, the stability of monoatomic sheets was questioned for many years before that. Some issues in physics cannot be decided with paper and pencil; sometimes you

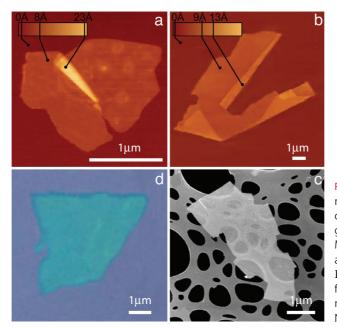
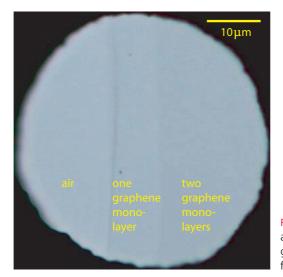


FIGURE 64 Single atom sheets, mapped by atomic force microscopy, of a: NbSe<sub>2</sub>, b: of graphite or graphene, d: a single atom sheet of  $MoS_2$  imaged by optical microscopy, and c: a single atom sheet of  $Bi_2Sr_2CaCu_2O_x$  on a holey carbon film imaged by scanning electron microscopy (from Ref. 73, © 2005 National Academy of Sciences).



**FIGURE 65** A microscope photograph shows the absorption of a single and of a double layer of graphene – and thus provides a way to see the fine structure constant. (© Andre Geim).

need adhesive tape as well.) Graphene and the other so-called *two-dimensional crystals* (this is, of course, a tabloid-style exaggeration) are studied for their electronic and mechanical properties; in the future, they might even have applications in high-performance batteries.

\* \*

A monolayer of graphene has an astonishing optical property. Its optical absorption over the full optical spectrum is  $\pi\alpha$ , where  $\alpha$  is the fine structure constant. (The exact expres-

#### 2 CHANGING THE WORLD WITH QUANTUM EFFECTS



FIGURE 66 The beauty of materials science: the surface of a lotus leaf leads to almost spherical water droplets; plasma-deposited PTFE, or teflon, on cotton leads to the same effect for the coloured water droplets on it (© tapperboy, Diener Electronics).

sion for the absorption is  $A = 1 - (1 + \pi \alpha/2)^{-2}$ .) The expression for the absorption is the consequence of the electric conductivity  $G = e^2/4\hbar$  for every monolayer of graphene. The numeric value of the absorption is about 2.3 %. This value is visible by the naked eye, as shown in Figure 65. Graphene thus yields a way to 'see' the fine structure constant.

\* \*

Gold absorbs light. Therefore it is used, in expensive books, to colour the edges of pages. Apart from protecting the book from dust, it also prevents that sunlight lets the pages turn yellow near the edges.

Like trees, crystals can have *growth rings*. Smoke quartz is known for these so-called *phantoms*, but also fluorite and calcite.

\* \*

The science and art of surface treatment is still in full swing, as Figure 66 shows. Making hydrophobic surfaces is an important part of modern materials science, that copies what the lotus, *Nelumbo nucifera*, does in nature. Hydrophobic surfaces allow that water droplets bounce on them, like table tennis balls on a table. The lotus surface uses this property to clean itself, hence the name *lotus effect*. This is also the reason that lotus plants have become a symbol of purity.

Sometimes research produces bizarre materials. An example are the so-called *aerogels*, highly porous solids, shown in Figure 67. Aerogels have a density of a few g/l, thus a few hundred times lower than water and only a few times that of air. Like any porous material, aerogels are good insulators; however, they are easily destroyed and therefore have not found important applications up to now.

\*

Where do the minerals in the Amazonian rainforest come from? The Amazonas river

\* \*

Ref. 74

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### QUANTUM TECHNOLOGY



FIGURE 67 A piece of aerogel, a solid that is so porous that it is translucent (courtesy NASA).

washes many nutrient minerals into the Atlantic Ocean. How does the rainforest get its minerals back? It was a long search until it became clear that the largest supply of minerals is airborne: from the Sahara. Winds blow dust from the Sahara desert to the Amazonas basin, across the Atlantic Ocean. It is estimated that 40 million tons of dust are moved from the Sahara to the Amazonas rainforest every year.

\* \*

Some materials undergo almost unbelievable transformations. What is the final state of *moss*? Large amounts of moss often become peat (turf). Old turf becomes lignite, or brown coal. Old lignite becomes black coal (bituminous coal). Old black coal can become *diamond*. In short, diamonds can be the final state of moss.

\* \*

In materials science, there is a dream: to make a material that is harder than diamond. It is not clear whether this dream can be realized. The coming years will tell.

## QUANTUM TECHNOLOGY

**(** I were better to be eaten to death with a rust than to be scoured to nothing with perpetual motion.

William Shakespeare King Henry IV.

Quantum effects do not appear only in microscopic systems or in material properties. Also *applied* quantum effects are important in modern life: technologies such as transistors, lasers, superconductivity and other effects and systems have deeply affected our civilisation.

## TRANSISTORS

Transistors are found in almost all devices that improve health, as well as in almost all devices for telecommunication. A *transistor*, shown in Figure 68 is a device that allows controlling a large electric current with the help of a small one; therefore it can play

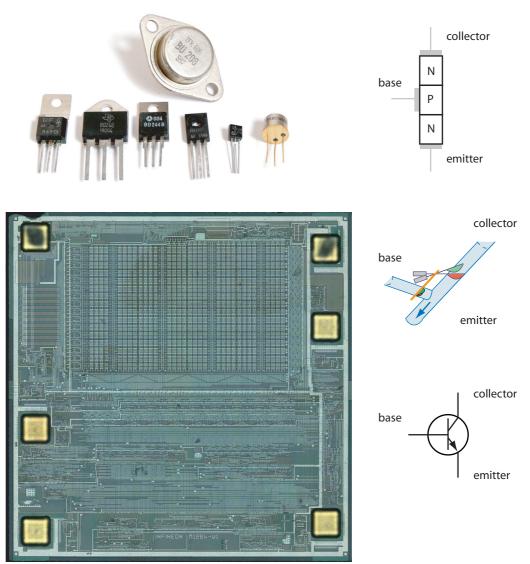


FIGURE 68 Top: examples of packaged single transistors. Right: the basic semiconductor structure, the equivalent water structure, and the technical drawing of an NPN transistor. Bottom: a typical integrated circuit for smart cards incorporating a large number of transistors. (© Benedikt Seidl, blog.ioactive.com)

the role of an electrically controlled switch or of an amplifier. Transistors are made from silicon and can be as small as a 2 by 2  $\mu$ m and as large as 10 by 10 cm. Transistors are used to control the signals in pacemakers for the heart and the current of electric train engines. Amplifying transistors are central to the transmitter in mobile phones and switching transistors are central to computers and their displays.

Transistors are (almost exclusively) based on *semiconductors*, i.e., on materials where the electrons that are responsible for electric conductivity are *almost* free. The devices

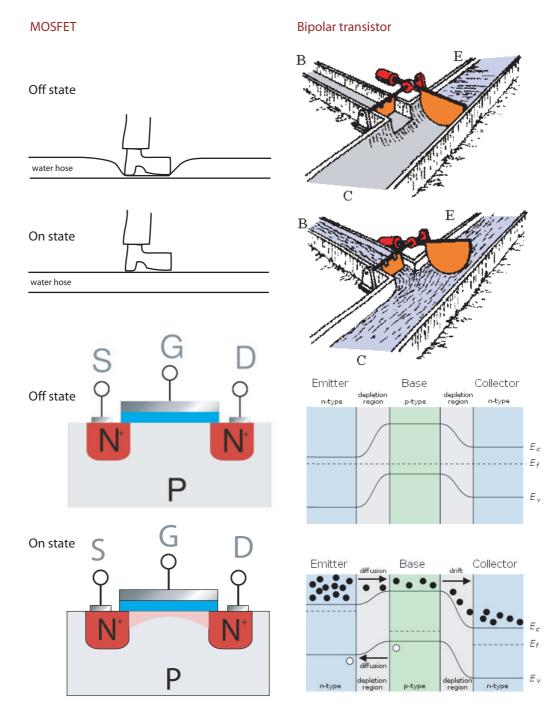


FIGURE 69 The working and construction of a metal-oxide silicon field effect transistor (left) and of a bipolar transistor (right). The 'off' and 'on' states are shown (© Leifi Physik, Wikimedia).

are built in such a way that applying an electric signal changes the conductivity. Every explanation of a transistor makes use of potentials and tunnelling; transistors are applied quantum devices.

The transistor is just one of a family of semiconductor devices that includes the fieldeffect transistor (FET), the metal-oxide-silicon field-effect transistor (MOSFET), the junction gate field-effect transistor (JFET), the insulated gate bipolar transistor (IGBT) and the unijunction transistor (UJT), but also the memristors, diode, the PIN diode, the Zener diode, the avalanche diode, the light-emitting diode (LED), the photodiode, the photovoltaic cell, the diac, the triac, the thyristor and finally, the integrated circuit (IC). These are important in industrial applications: the semiconductor industry has at least 300 thousand million Euro sales every year (2010 value) and employ millions of people across the world.

## MOTION WITHOUT FRICTION - SUPERCONDUCTIVITY AND SUPERFLUIDITY

We are used to thinking that friction is inevitable. We even learned that friction was an inevitable result of the particle structure of matter. It should come to the surprise of every physicist that motion *without* friction is indeed possible.

In 1911 Gilles Holst and Heike Kamerlingh Onnes discovered that at low temperatures, electric currents can flow with no resistance, i.e., with no friction, through lead. The observation is called *superconductivity*. In the century after that, many metals, alloys and ceramics have been found to show the same behaviour.

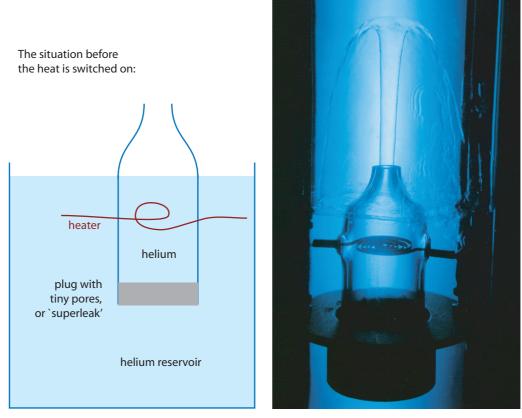
The condition for the observation of motion without friction is that quantum effects play an essential role. To ensure this, low temperature is usually needed. Despite a large amount of data, it took over 40 years to reach a full understanding of superconductivity. This happened in 1957, when Bardeen, Cooper and Schrieffer published their results. At low temperatures, electron behaviour in certain materials is dominated by an *attractive* interaction that makes them form pairs. These so-called *Cooper pairs* are effective bosons. And bosons can all be in the same state, and can thus effectively move without friction.

In superconductivity, the attractive interaction between electrons is due to the deformation of the lattice. At low temperature, two electrons attract each other in the same way as two masses attract each other due to deformation of the space-time mattress. However, in the case of solids, these deformations are quantized. With this approach, Bardeen, Cooper and Schrieffer explained the lack of electric resistance of superconducting materials, their complete diamagnetism ( $\mu_r = 0$ ), the existence of an energy gap, the second-order transition to normal conductivity at a specific temperature, and the dependence of this temperature on the mass of the isotopes. As a result, they received the Nobel Prize in 1972.\*

Another type of motion without friction is *superfluidity*. In 1937, Pyotr Kapitsa had understood that usual liquid helium, i.e., <sup>4</sup>He, below a transition observed at the temperature of 2.17 K, is a *superfluid*: the liquid effectively moves without friction through

Ref. 75

<sup>\*</sup> For John Bardeen (b. 1908 Madison, d. 1991 Boston), this was his second, after he had got the first Nobel Prize in Physics in 1956, shared with William Shockley and Walter Brattain, for the discovery of the transistor. The first Nobel Prize was a problem for Bardeen, as he needed time to work on superconductivity. In an example to many, he reduced the tam-tam around himself to a minimum, so that he could work as much as possible on the problem of superconductivity. By the way, Bardeen is topped by Frederick Sanger and by Marie Curie. Sanger first won a Nobel Prize in Chemistry in 1958 by himself and then won a second one shared with Walter Gilbert in 1980; Marie Curie first won one with her husband and a second one by herself, though in two different fields.



**FIGURE 70** The superfluidity of helium 4 can be used to produce the fountain effect above a disc with very small pores, through which superfluid helium can pass, but normal fluid cannot. Superfluid helium 4 has a large thermal conductivity and flows towards a heated region trying to cool it down again, whereas the normal liquid cannot return back through the pores. This thermomechanical effect leads to the fountain (© Pacific Institute of Theoretical Physics).

devices, tubes, etc. More precisely, liquid helium remains a mixture of a superfluid component and a normal component; only the superfluid component moves without friction. Superfluid helium is even able, after an initial kick, to flow over obstacles, such as glass walls, or to flow out of bottles. A well-known effect of superfluidity is shown in Figure 70. Superfluidity occurs because the <sup>4</sup>He atom is a boson. Therefore no pairing is necessary for it to move without friction. This research earned Kapitsa a Nobel Prize in 1978.

In 1972, Richardson, Lee and Osheroff found that even <sup>3</sup>He is superfluid, provided that the temperature is lowered below 2.7 mK. <sup>3</sup>He is a fermion, and requires *pairing* to become superfluid. In fact, below 2.2 mK, <sup>3</sup>He is even superfluid in two different ways; one speaks of phase A and phase B. They received the Nobel Prize in 1996 for this discovery.

In the case of <sup>3</sup>He, the theoreticians had been faster than the experimentalists. The theory for superconductivity through pairing had been adapted to superfluids already in 1958 – before any data were available – by Bohr, Mottelson and Pines. This theory was then adapted and expanded by Anthony Leggett.\* The attractive interaction between

<sup>\*</sup> Aage Bohr, son of Niels Bohr, and Ben Mottelson received the Nobel Prize in 1975, Anthony Leggett in

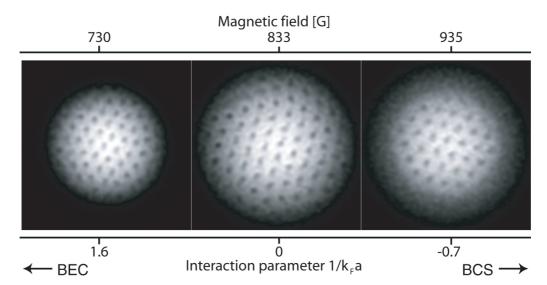


FIGURE 71 A vortex lattice in cold lithium gas, showing their quantized structure (© Andre Schirotzek).

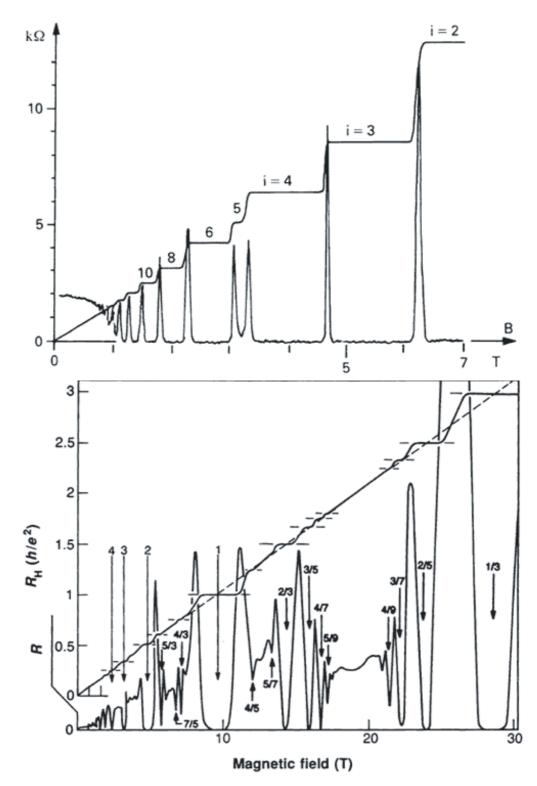
<sup>3</sup>He atoms, the basic mechanism that leads to superfluidity, turns out to be the spin-spin interaction.

Superfluidity has also been observed in a number of *gases*, though at much lower temperatures. Studying the behaviour of gases at lowest temperatures has become popular in recent years. When the temperature is so low that the de Broglie wavelength is comparable to the atom-atom distance, bosonic gases form a Bose–Einstein condensate. The first such states were realized in 1995 by several groups; the group around Eric Cornell and Carl Wieman used <sup>87</sup>Rb, Rand Hulet and his group used <sup>7</sup>Li and Wolfgang Ketterle and his group used <sup>23</sup>Na. For fermionic gases, the first degenerate gas, <sup>40</sup>K, was observed in 1999 by the group around Deborah Jin. In 2004, the same group observed the first gaseous Fermi condensate, after the potassium atoms paired up. All these condensates show superfluidity.

Superfluids are fascinating substances. Vortices also exist in them. But in superfluids, be they gases or liquids, vortices have properties that do not appear in normal fluids. In the superfluid <sup>3</sup>He-B phase, vortices are *quantized*: vortices only exist in integer multiples of the elementary circulation  $h/2m_{^{3}\text{He}}$ . (This is also the case in superconductors.) Vortices in superfluids have quantized angular momentum. An effect of the quantization can be seen in Figure 71. In superfluids, these quantized vortices flow forever! Like in ordinary fluids, also in superfluids one can distinguish between laminar and turbulent flow. The transition between the two regimes is mediated by the behaviour the *vortices* in the fluid. Present research is studying how these vortices behave and how they induce

Ref. 76

the transition.



**FIGURE 72** The quantum Hall effect (above) and the fractional quantum Hall effect (below): each graph yielded a Nobel prize. The graphs show how the Hall resistance and the Ohmic resistance vary with the applied magnetic field at very low temperature. The step height is quantized in integer or simple fractions of  $h/e^2 = 25.812\,807\,557(18)\,\mathrm{k\Omega}$ . Quantum Hall experiments allow the most precise determination known to date of this constant of nature.

### THE FRACTIONAL QUANTUM HALL EFFECT

The fractional quantum Hall effect is one of the most intriguing discoveries of materials science, and possibly, of physics as a whole. The effect concerns the flow of electrons in a two-dimensional surface. In 1982, Robert Laughlin predicted that in this system one should be able to observe objects with electrical charge *e*/3. This strange and fascinating

Ref. 78 prediction was indeed verified in 1997. Page 98 We encountered the (classical) Hal

We encountered the (classical) Hall effect above. The story continues with the discovery by Klaus von Klitzing of the *quantum* Hall effect. In 1980, Klitzing and his

Ref. 79

covery by Klaus von Klitzing of the *quantum* Hall effect. In 1980, Klitzing and his collaborators found that in two-dimensional systems at low temperatures – about 1 K – the electrical conductance *S*, also called the Hall conductance, is quantized in multiples of the quantum of conductance

$$S = n \, \frac{e^2}{h} \,. \tag{11}$$

The explanation is straightforward: it is the quantum analogue of the classical Hall effect, which describes how conductance varies with applied magnetic field. The corresponding resistance values are

$$R = \frac{1}{n} \frac{h}{e^2} = \frac{1}{n} 25,812\,807\,557(18)\,\mathrm{k}\Omega\;. \tag{12}$$

The values are independent of material, temperature, or magnetic field. They are constants of nature. Von Klitzing received the Nobel Prize in Physics for the discovery, because the effect was unexpected, allows a highly precise measurement of the fine structure constant, and also allows one to build detectors for the smallest voltage variations measurable so far. His discovery started a large wave of subsequent research.

Ref. 80

Ref. 77

Only two years later, in 1982, it was found that in extremely strong magnetic fields and at extremely low temperatures, the conductance could vary in steps *one third* that size. Shortly afterwards, even stranger numerical fractions were also found. In fact, all fractions of the form m/(2m+1) or of the form (m+1)/(2m+1), m being an integer, are possible. This is the *fractional quantum Hall effect*. In a landmark paper, Robert Laughlin explained all these results by assuming that the electron gas could form collective states showing quasiparticle excitations with a charge e/3. This was confirmed experimentally 15 years later and earned him a Nobel Prize as well. We have seen in several occasions that quantization is best discovered through noise measurements; also in this case, the clearest confirmation came from electrical current noise measurements.

Subsequent experiments confirmed Laughlin's deduction. He had predicted the appearance of a new form of a *composite* quasi-particle, built of electrons and of one or several magnetic flux quanta. If an electron bonds with an *even* number of quanta, the composite is a fermion, and leads to Klitzing's *integral* quantum Hall effect. If the electron bonds with an *odd* number of quanta, the composite is a boson, and the *fractional* quantum Hall effect appears. The experimental and theoretical details of these quasiparticles might well be the most complex and fascinating aspects of physics, but exploring them would lead us too far from the aim of our adventure.

Ref. 81

In 2007, a new chapter in the story was opened by Andre Geim and his team, and a

Рнаѕе	Түре	Low temperature behaviour	EXAMPLE
Solid	conductor	superconductivity antiferromagnet	lead, MgB <sub>2</sub> (40 K) chromium, MnO
	insulator	ferromagnet diamagnet	iron
Liquid	bosonic	Bose–Einstein condensation, i.e., superfluidity	<sup>4</sup> He
	fermionic	pairing, then BEC, i.e., superfluidity	<sup>3</sup> He
Gas	bosonic	Bose-Einstein condensation	<sup>87</sup> Rb, <sup>7</sup> Li, <sup>23</sup> Na, H, <sup>4</sup> He, <sup>41</sup> K
	fermionic	pairing, then Bose–Einstein condensation	<sup>40</sup> K, <sup>6</sup> Li

TABLE 8 Matter	at lowest tem	peratures.
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Page 99

second team, when they discovered a new type of quantum Hall effect at room temperature. They used graphene, i.e., single-atom layers of graphite, and found a relativistic analogue of the quantum Hall effect. This effect was even more unexpected than the previous ones, is equally interesting, and can be performed on a table top. The groups are good candidates for a trip to Stockholm.\*

What do we learn from these results? Systems in two dimensions have states which follow different rules than systems in three dimensions. The fractional charges in superconductors have no relation to quarks. Quarks, the constituents of protons and neutrons, have charges e/3 and 2e/3. Might the quarks have something to do with a mechanism similar to superconductivity? At this point we need to stand the suspense, as no answer is possible; we come back to this issue in the last part of this adventure.

# How does matter behave at the lowest temperatures?

The low-temperature behaviour of matter has numerous experimental and theoretical aspects. The first issue is whether matter is always solid at low temperatures. The answer is no: all phases exist at low temperatures, as shown in Table 8.

Concerning the electric properties of matter at lowest temperatures, the present status is that matter is either insulating or superconducting. Finally, one can ask about the magnetic properties of matter at low temperatures. We know already that matter can not be paramagnetic at lowest temperatures. It seems that matter is either ferromagnetic, diamagnetic or antiferromagnetic at lowest temperatures.

#### LASERS AND OTHER SPIN-ONE VECTOR BOSON LAUNCHERS

Ref. 82

Photons are vector bosons; a lamp is thus a vector boson launcher. All existing lamps fall into one of three classes. *Incandescent lamps* use emission from a hot solid, *gas discharge lamps* use excitation of atoms, ions or molecules through collision, and *recombination lamps* generate (cold) light through recombination of charges in semiconductors or li-

<sup>\*</sup> This prediction from the December 2008 edition became reality in December 2010.



FIGURE 73 The beauty of lasers: the fine mesh created by a green laser delay line (© Laser Zentrum Hannover).

quids. The latter are the only lamp types found in living systems. The other main sources of light are *lasers*. All light sources are based on quantum effects, but for lasers the connection is especially obvious. The following table gives an overview of the main types and their uses.

TABLE 9 A selection of lamps and lasers.

LAMP TYPE, APPLICATION	Wave- Length	Bright - Ness or Power	Соѕт	L I F E - T I M E
Incandescent lamps				
Oil lamps, candles, for illumination	white	up to 500 lm	1 cent/lm	5 h
Tungsten wire light bulbs, halogen lamps, for illumination	300 to 800 nm	5 to 25 lm/W	0.1 cent/lm	700 h
Stars, for production of heavy elements	full spectrum	up to 10 <sup>44</sup> W	free	up to thousands of millions of years
Gas discharge lamps				
Neon lamps, for advertising	red			up to 30 kh
Mercury lamps, for illumination	UV plus spectrum	45 to 110 lm/W	0.05 cent/lm	3000 to 24 000 h
Metal halogenide lamps (ScI <sub>3</sub> or 'xenon light', NaI, DyI <sub>3</sub> , HoI <sub>3</sub> , TmI <sub>5</sub> for car headlights and illumination	white )	110 lm/W	l cent/lm	up to 20 kh
Sodium low pressure lamps for street illumination	589 nm yellow	200 lm/W	0.2 cent/lm	up to 18 kh

# QUANTUM TECHNOLOGY

LAMP TYPE, APPLICATION	WAVE-	Bright -	Соѕт	Life -
	LENGTH	NESS OR POWER	0031	TIME
Sodium high pressure lamps for street illumination	broad yellow	120 lm/W	0.2 cent/lm	up to 24 kh
Xenon arc lamps, for cinemas	white	30 to 150 lm/W, up to 15 kW		100 to 2500 h
Stars, for production of heavy elements	many lines	up to 10 <sup>20</sup> W	free	up to thousands of millions of years
Recombination lamps				
Foxfire in forests, e.g. due to <i>Armillaria mellea</i> , <i>Neonothopanus</i> <i>gardneri</i> or other bioluminescent fungi	green	just visible	free	years
Firefly, to attract mates	green-yellow		free	<i>c</i> . 10 h
Large deep sea squid, <i>Taningia</i> <i>danae</i> , producing light flashes, to confuse prey	red	<i>c</i> . 1 W	free	years
Deep-sea fish, such as <i>angler fish</i> , to attract prey or find mates	white	<i>c</i> . 1 μW	free	years
Deep-sea medusae, to produce attention so that predators of predators are attracted	blue and all other colours		free	years
Light emitting diodes, for measurement, illumination and communication	red, green, blue, UV	up to 150 lm/W, up to 5 W	10 cent/lm	15k to 100 kh
Synchrotron radiation sources				
Electron synchroton source	X-rays to radio waves	pulsed	many MEuro	years
Maybe some stars	broad spectrum		free	thousands of years
Ideal white lamp or laser	visible	<i>c</i> . 300 lm/W	0	$\infty$
Ideal coloured lamp or laser	green	683 lm/W	0	$\infty$
Gas lasers				
He-Ne laser (obsolete), for school experiments	632.8 nm	550 lm/W	2000 cent/lm	300 h
Argon laser, for pumping and laser shows, now obsolete	several blue and green lines	up to 100 W	10 kEuro	

 TABLE 9 A selection of lamps and lasers (continued).

LAMP TYPE, APPLICATION	Wave- length	Bright - ness or power	Соѕт	Life - time
Krypton laser, for pumping and laser shows, now obsolete	several blue, green, red lines	50 W		
Xenon laser	many lines in the IR, visible and near UV	20 W		
Nitrogen (or 'air') laser, for pumping of other lasers, for hobbyists	337.1 nm	pulsed up to 1 MW	down to a few hundred Euro	•
Water vapour laser, for research, now obsolete	many lines between 7 and 220 μm, often 118 μm	CW 0.5 W, pulsed much higher	a few kEuro	
$\rm CO_2$ laser, for cutting, welding, glass welding and surgery	s 10.6 μm	CW up to 100 kW, pulsed up to 10 TW	<i>c</i> . 100 Euro/W	1500 h
Excimer laser, for lithography in silicon chip manufacturing, eye surgery, laser pumping, psoriasis treatment, laser deposition	193 nm (ArF), 248 nm (KrF), 308 nm (XeCl) 353 nm (XeF)		10 to 500 kEuro	years
Metal vapour lasers (Cu, Cd, Se, Ca Ag, Au, Mn, Tl, In, Hg)	9			
Copper vapour laser, for pumping, photography, dermatology, laser cutting, hobby constructions and explorative research	248 nm, 511 nm and 578 nm	pulses up to 5 MW	10 kEuro	1 khour
Cadmium vapour laser, for printing typesetting and recognition of forged US dollar notes	, 325 nm and 442 nm	up to 200 mW	12 kEuro	10 kh
Gold vapour laser, for explorative research, dermatology	627 nm	pulses up to 1 MW	from a few hundred Euro upwards	
Chemical gas lasers				
HF, DF and oxygen-iodine laser, used as weapons, pumped by chemical reactions, all obsolete	1.3 to 4.2 μm	up to MW in CW mode	over 10 MEuro	unknown
Liquid dye lasers				

 TABLE 9 A selection of lamps and lasers (continued).

1	. ,			
LAMP TYPE, APPLICATION	Wave- Length	Bright - ness or power	Соѕт	Life - time
Rhodamine, stilbene, coumarin etc. lasers, for spectroscopy and medical uses	tunable, range depends on dye in 300 to 1100 nm range	up to 10 W	10 kEuro	dye- dependen
Beer, vodka, whiskey, diluted marmelade and many other liquids work as laser material	IR, visible	usually mW	1 kEuro	a few minutes
Solid state lasers				
Ruby laser (obsolete), for holography and tattoo removal	694 nm		1 kEuro	
Nd:YAG (neodymium:yttrium aluminium granate) laser, for material processing, surgery, pumping, range finding, velocimetry, also used with doubled frequency (532 nm), with tripled frequency (355 nm) and with quadrupled frequency (266 nm), also used as slab laser	1064 nm	CW 10 kW, pulsed 300 MW	50 to 500 kEuro	1000 h
Er:YAG laser, for dermatology	2940 nm			
Ti:sapphire laser, for ultrashort pulses for spectroscopy, LIDAR, and research	650 to 1200 nm l	nCW 1 W, pulsed 300 TW	from 5 kEuro upwards	
Alexandrite laser, for laser machining, dermatology, LIDAR Cr:LiSAF laser	700 to 840 nm	pulsed 10 TW, down to 30 fs		
Cr:YAG laser	1.35 to 1.6 µm	pulsed, down to 100 fs		
Cr:Forsterite laser, optical tomography	1200 to 1300 nm	pulsed, below 100 fs		
Erbium doped glass fibre laser, used in optical communications (undersea cables) and optical amplifiers	1.53 to 1.56 μm			years
Perovskite laser, such as Co:KZnF <sub>3</sub> , for research	NIR tunable, 1650 to 2070 nm	100 mW	2 kEuro	
F-centre laser, for spectroscopy (NaCl:OH-, KI:Li, LiF)	tuning ranges between 1.2 and 6 μm	100 mW	20 kEuro	

 TABLE 9 A selection of lamps and lasers (continued).

LAMP TYPE, APPLICATION	Wave- Length	Bright - ness or power	Соѕт	Life - time
Semiconductor lasers				
GaN laser diode, for optical recording	355 to 500 nm, depending on doping	up to 150 mW	a few Euro to 5 kEuro	<i>c.</i> 10 000 ł
AlGaAs laser diode, for optical recording, pointers, data communication, laser fences, bar code readers (normal or vertical cavity)	620 to 900 nm, depending on doping	up to 1 W	below 1 Euro to 100 Euro	o <i>c</i> . 10 000 ł
InGaAsP laser diode, for fiberoptic communication, laser pumping, material processing, medial uses (normal and vertical cavity or VCSEL)	1 to 2.5 μm	up to 100 W	below 1 Euro up to a few k Euro	up to 20 000 h
Lead salt (PbS/PbSe) laser diode, for spectroscopy and gas detection	c 3 to 25 μm	0.1 W	a few 100 Euro	
Quantum cascade laser, for research and spectroscopy	2.7 to 350 µm	up to 4 W	<i>c.</i> 10 kEuro	<i>c</i> . 1 000 h
Hybrid silicon lasers, for research	IR	nW	0.1 MEuro	
Free electron lasers				
Used for materials science	5 nm to 1 mm	CW 20 kW, pulsed in GW range	10 MEuro	years
Nuclear-reaction pumped lasers				

TABLE 9 A selection of lamps and lasers (continued).

Have uses only in science fiction and for getting money from gullible military

#### FROM LAMPS TO LASERS

Most solid state lamps are light emitting diodes. The large progress in brightness of light emitting diodes could lead to a drastic reduction in future energy consumption, if their cost is lowered sufficiently. Many engineers are working on this task. Since the cost is a good estimate for the energy needed for production, can you estimate which lamp is the most friendly to the environment?

Nobody thought much about lamps, until Albert Einstein and a few other great physicists came along, such as Theodore Maiman and Hermann Haken. Many other researchers later received Nobel Prizes by building on their work. In 1916, Einstein showed that there are two types of sources of light – or of electromagnetic radiation in general – both of which actually 'create' light. He showed that every lamp whose brightness is turned up high enough will change behaviour when a certain intensity threshold is passed. The

Challenge 61 s

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main mechanism of light emission then changes from spontaneous emission to *stimulated emission*. Nowadays such a special lamp is called a *laser*. (The letters 'se' in laser are an abbreviation of 'stimulated emission'.) After a passionate worldwide research race, in 1960 Maiman was the first to build a laser emitting visible light. (So-called *masers* emitting microwaves were already known for several decades.) In summary, Einstein and the other physicists showed that whenever a lamp is sufficiently turned up, it becomes a laser. Lasers consist of some light producing and amplifying material together with a mechanism to pump energy into it. The material can be a gas, a liquid or a solid; the pumping process can use electrical current or light. Usually, the material is put between two mirrors, in order to improve the efficiency of the light production. Common lasers are semiconductor lasers (essentially strongly pumped LEDs or light emitting diodes), He–Ne lasers (strongly pumped neon lamps), liquid lasers (essentially strongly pumped fire flies) and ruby lasers (strongly pumped luminescent crystals). Most materials can be used to make lasers for fun, including water, beer and vodka.

Lasers produce radiation in the range from microwaves and extreme ultraviolet. They have the special property of emitting *coherent* light, usually in a collimated beam. Therefore lasers achieve much higher light intensities than lamps, allowing their use as tools. In modern lasers, the coherence length, i.e., the length over which interference can be observed, can be thousands of kilometres. Such high quality light is used e.g. in gravitational wave detectors.

People have become pretty good at building lasers. Lasers are used to cut metal sheets up to 10 cm thickness, others are used instead of knives in surgery, others increase surface hardness of metals or clean stones from car exhaust pollution. Other lasers drill holes in teeth, measure distances, image biological tissue or grab living cells.

Some materials amplify light so much that end mirrors are not necessary. This is the case for nitrogen lasers, in which nitrogen, or simply air, is used to produce a UV beam. Even a laser made of a single atom (and two mirrors) has been built; in this example, only eleven photons on average were moving between the two mirrors. Quite a small lamp. Also lasers emitting light in two dimensions have been built. They produce a light plane instead of a light beam.

#### THE THREE LIGHTBULB SCAMS

Ref. 83

In the 1990s, all major light bulb producers in the world were fined large sums because they had agreed to keep the lifetimes of light bulbs constant. It is no technical problem to make light bulbs that last 2000 hours; however, the producers agreed not to increase the lifetime above 700 hours, thus effectively making every lightbulb three times as expensive as it should. This was the first world-wide light bulb scam.

Despite the fines, the crooks in the light bulb industry did not give up. In 2012, a large German light bulb maker explained in its advertising that its new light sources were much longer living than its conventional light bulbs, which, they explained on their ads, lasted only 500 hours. In other words, not only did the fines not help, the light bulb industry even *reduced* the lifetimes of the light bulbs from the 1990s to 2012. This was the second light bulb scam.

Parallel to the second scam, in the years around 2000, the light bulb industry started lobbying politics with the false statement that light bulbs were expensive and would waste energy. As a result of the false data provided from the other two scams, light bulbs were forbidden in Europe, with the result that consumers in Europe are now forced to buy other, much more expensive means of illumination. On top of this, many of these more expensive light sources are bad for the eyes. Indeed, flickering mercury or flickering LED lamps, together with their reduced colour spectrum, force the human visual system in overload mode, a situation that does not occur with the constantly glowing light bulbs. In other words, with this third scam, the light bulb industry increased their profits even more, while ruining the health of consumers at the same time. One day, maybe, parliaments will be less corrupt and more sensible. The situation will then again improve.

#### Applications of lasers

As shown in Figure 74, lasers can be used to make beautiful parts – including good violins and personalized bicycle parts – via sintering of polymer or metal powders. Lasers are used in rapid prototyping machines and to build architectural models. Lasers can cut paper, metal, plastics and flesh.

Lasers are used to read out data from compact discs (CDs) and digital versatile discs

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(DVDs), are used in the production of silicon integrated circuits and for the transport telephone signals through optical fibres. In our adventure, we already encountered lasers that work as loudspeakers. Important advances in recent years came from the applications of *femtosecond laser* pulses. Femtosecond pulses generate high-temperature plasmas in the materials they propagate through; this happens even in air, if the pulses are focused. The effect has been used to create luminous three-dimensional displays floating in mid-air, as shown in Figure 74, or in liquids. Such short pulses can also be used to cut material without heating it, for example to cut bones in skull operations. The lack of heating is so complete that femtosecond lasers can be used to engrave matches and even dynamite without triggering a reaction. Femtosecond lasers have been used to make high resolution holograms of human heads within a single flash. Recently such lasers have been used to guide lightning along a predetermined path; they seem promising candidates for laser ligtning rods. A curious demonstration application of femtosecond lasers is the storage of information in fingernails (up to 5 Mbit for a few months), in a way not unlike that used in recordable compact discs (CD-R).

Ref. 85

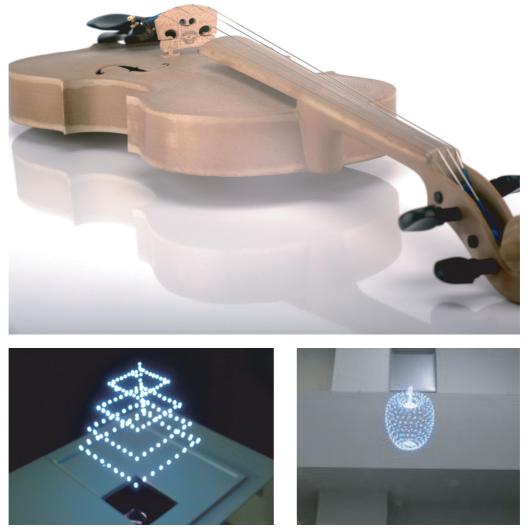
Ref. 84

Lasers are used in ophthalmology, with a technique called *optical coherence tomography*, to diagnose eye and heart illnesses. Around 2025, there will finally be laser-based breast screening devices that use laser light to search for cancer without any danger to the patient. The race to produce the first working system is already ongoing since the 1990s. Additional medical laser applications will appear in the coming years.

Lasers have been used in recent demonstrations, together with image processing software, to kill mosquitos in flight; other lasers are burning weeds while the laser is moved over a field of crops. One day, such combined laser and vision systems will be used to evaporate falling rain drops one by one; as soon as the first such *laser umbrella* will be available, it will be presented here. The feat should be possible before the year 2022.

Ref. 86

#### QUANTUM TECHNOLOGY



**FIGURE 74** Some laser applications. Top: a violin, with excellent sound quality, made of a single piece of polymer (except for the chords and the black parts) through laser sintering of PEEK by EOS from Krailling, in Germany. Bottom: a display floating in mid-air produced with a galvanometer scanner and a fast focus shifter (© Franz Aichinger, Burton).

# Challenges, dreams and curiosities about quantum technology

Nowadays, we carry many electronic devices in our jacket or trousers. Almost all use batteries. In the future, there is a high chance that some of these devices will extract energy from the human body. There are several options. One can extract thermal energy with thermoelements, or one can extract vibrational energy with piezoelectric, electrostatic or electromagnetic transducers. The challenge is to make these elements small and cheap. It will be interesting to find out which technology will arrive to the market first.

\* \*



**FIGURE 75** The most expensive laser pointer: a yellow 10W laser that is frequency-stabilized at the wavelength of sodium lamps allows astronomers to improve the image quality of terrestrial telescopes. By exciting sodium atoms found at a height of 80 to 90 km, the laser provides an artificial guide star that is used to compensate for atmospheric turbulence, using the adaptive optics built into the telescope. (© ESO/Babak Tafreshi).

In 2007, Humphrey Maris and his student Wei Guo performed an astonishing experiment: they filmed *single electrons* with a video camera. Actually the truth is a bit more complicated, but it is not a lie to summarize it in this way.

Maris is an expert on superfluid helium. For many years he knew that free electrons in superfluid helium repel helium atoms, and can move, surrounded by a small vacuum bubble, about 2 nm across, through the fluid. He also discovered that under negative pressure, these bubbles can grow and finally explode. When they explode, they are able to scatter light. With his student Wei Guo, he then injected electrons into superfluid helium through a tungsten needle under negative voltage, produced negative pressure by focussing waves from two piezoelectric transducers in the bulk of the helium, and

Ref. 87

#### QUANTUM TECHNOLOGY

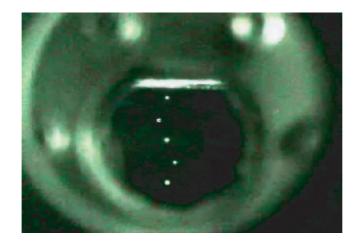


FIGURE 76 How to image single electrons with a video camera: isolated electrons surrounded by bubbles that explode in liquid helium under negative pressure produce white spots (mpg film © Humphrey Maris).

	shone light through the helium. When the pressure became negative enough they saw the explosions of the bubbles. Figure 76 shows the video. The experiment is one of the highlights of experimental physics in the last decade.
	* *
Challenge 62 d	Is it possible to make A4-size flexible colour displays for an affordable price and with print-like quality?
	* *
	Will there ever be rechargeable batteries with an energy content per mass that is com- parable to diesel oil? How long will it take, from 2014 onwards, until the last company producing electric cars powered by batteries stops production?
	* *
	How many companies promising free energy, engineers promising cars powered by wa- ter, politicians promising fusion energy or quacks promising food additives or sugar pills that cure cancer will we see every year?
	* *
Challenge 63 r	Will there ever be room-temperature superconductivity?
	* *
Challenge 64 r	Will there ever be desktop laser engravers for 1000 euro?
	* *
Challenge 65 s	Will there ever be teleportation of everyday objects?
	* *
	One process that quantum physics does not allow is telephathy. An unnamed space

- The Adventure of Physics

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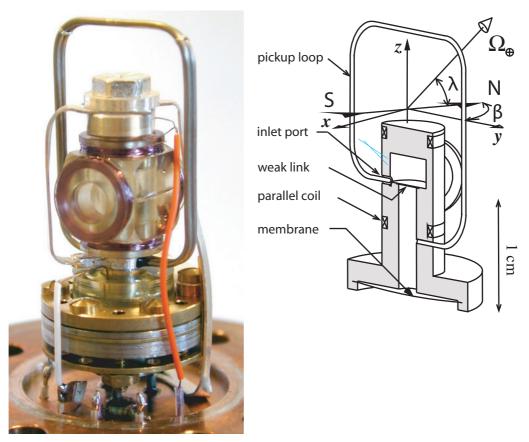


FIGURE 77 The interior of a gyroscope that uses superfluid helium (© Eric Varoquaux).

Ref. 88	agency found this out during the Apollo 14 mission, when, during the flight to the moon, cosmonaut Edgar Mitchell tested telepathy as communication means. Unsurprisingly, he found that telepathy was useless. It is unclear why the space agency spent so much money for a useless experiment – an experiment that could have been performed, at a cost of a phone call, also down here on earth.		
	* *		
Challenge 66 d	Will there ever be applied quantum cryptology?		
	* *		
Challenge 67 d	Will there ever be printable polymer electronic circuits, instead of lithographically pat- terned silicon electronics as is common now?		
	* *		
Challenge 68 r	Will there ever be radio-controlled flying toys in the size of insects?		
	* *		
Ref. 107	By shining an invisible and harmless laser onto cars driving by, it is now possible to		

#### QUANTUM TECHNOLOGY

Challenge 70 e



FIGURE 78 These colours were produced on steel using just an infrared laser shining on it. (© Trotec Laser at www. troteclaser.com)

detect whether the persons inside have drunk alcohol. Will this method ever become Challenge 69 s widespread?

In 1997, Eric Varoquaux and his group built a quantum version of the Foucault pendulum, using the superfluidity of helium. In this beautiful piece of research, they cooled a small ring of fluid helium below the temperature of 0.28 K, below which the helium moves without friction. In such situations helium can behave like a Foucault pendulum. With a clever arrangement, shown in Figure 77, they were able to measure the rotation of the helium in the ring using phonon signals, and, finally, to detect the rotation of the Earth.

Lasers are quantum devices that can be used for many applications. Figure 78 shows a way to produce colours on steel by scanning a focused infrared laser beam over the surface. Why and how do the colours appear?

\*

# Summary on changing the world with quantum effects

Atoms form bonds. Quantum effects thus produce molecules, gases, liquids and solids, as well as all effects and properties of all materials. In the past, quantum effects have been used to develop numerous materials with desired properties, such as new steel types, new carbon fibre composites, new colourants, new magnetic materials and new polymers.

Quantum effects have been used to develop modern electronics, lasers, light detectors, data storage devices, superconducting magnets, new measurement systems and new production machines. Magnetic resonance imaging, computers, polymers, telecommunication and the internet resulted from applying quantum effects to technology.

Quantum effects will continue to be used to design new materials and systems: new nanoparticles to deliver drugs inside the body, new polymers, new crystals, new environmentally friendly production processes and new medical devices, among others.

# 2 CHANGING THE WORLD WITH QUANTUM EFFECTS



# CHAPTER 3 QUANTUM ELECTRODYNAMICS - THE ORIGIN OF VIRTUAL REALITY

The central concept that quantum field theory adds to the description of nature is he idea of *virtual particles*. Virtual particles are short-lived particles; they owe heir existence exclusively to the quantum of action. Because of the quantum of action, they do not need to follow the energy-mass relation that special relativity requires of usual, *real* particles. Virtual particles can move faster than light and can move backward in time. Despite these strange properties, they have many observable effects. We explore the most spectacular ones.

# Ships, mirrors and the Casimir effect

When two parallel ships roll in a big swell, *without* even the slightest wind blowing, they will attract each other. The situation is illustrated in Figure 79. It might be that this effect was known before the nineteenth century, when many places still lacked harbours.\*\*

Waves induce oscillations of ships because a ship absorbs energy from the waves. When oscillating, the ship also emits waves. This happens mainly towards the two sides of the ship. As a result, for a single ship, the wave emission has no net effect on its position. Now imagine that two parallel ships oscillate in a long swell, with a wavelength much larger than the distance between the ships. Due to the long wavelength, the two ships will oscillate in phase. The ships will thus not be able to absorb energy from each other. As a result, the energy they radiate towards the outside will push them towards each other.

The effect is not difficult to calculate. The energy of a rolling ship is

$$E = mgh \, \alpha^2 / 2 \tag{13}$$

where  $\alpha$  is the roll angle amplitude, *m* the mass of the ship and  $g = 9, 8 \text{ m/s}^2$  the acceleration due to gravity. The *metacentric height h* is the main parameter characterizing a ship, especially a sailing ship; it tells with what torque the ship returns to the vertical when inclined by an angle  $\alpha$ . Typically, one has h = 1.5 m.

When a ship is inclined, it will return to the vertical by a damped oscillation. A damped oscillation is characterized by a period T and a quality factor Q. The *quality factor* is the number of oscillations the system takes to reduce its amplitude by a factor

 <sup>\*\*</sup> Sipko Boersma published a paper in which he gave his reading of shipping manuals, advising captains to
 Ref. 89 let the ships be pulled apart using a well-manned rowing boat. This reading has been put into question by
 subsequent research, however.

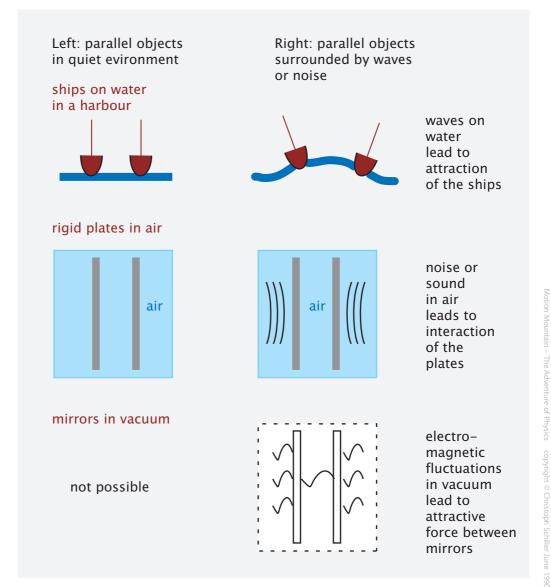


FIGURE 79 The analogy between ships in a harbour, metal plates in air and metal mirrors in vacuum.

e = 2.718. If the quality factor Q of an oscillating ship and its oscillation period T are given, the radiated power W is

$$W = 2\pi \frac{E}{QT} . \tag{14}$$

Vol. III, page 120We saw above that radiation force (radiation pressure times area) is W/c, where c is<br/>the wave propagation velocity. For gravity water waves in deep water, we have the well-<br/>Vol. III, page 295Vol. III, page 295known relation

$$c = \frac{gT}{2\pi} . \tag{15}$$

Assuming that for two nearby ships each one completely absorbs the power emitted from the other, we find that the two ships are attracted towards each other following

$$ma = m2\pi^2 \frac{h\alpha^2}{OT^2} .$$
 (16)

Inserting typical values such as Q = 2.5, T = 10 s,  $\alpha = 0.14$  rad and a ship mass of 700 tons, we get about 1.9 kN. Long swells thus make ships attract each other. The strength of the attraction is comparatively small and could be overcome with a rowing boat. On the other hand, even the slightest wind will damp the oscillation amplitude and have other effects that will hide or overshadow this attraction.

Sound waves or noise in air show the same effect. It is sufficient to suspend two metal plates in air and surround them by loudspeakers. The sound will induce attraction (or repulsion) of the plates, depending on whether the sound wavelength cannot (or can) be taken up by the other plate.

In 1948, the Dutch physicist Hendrik Casimir made one of the most spectacular predictions of quantum theory: he predicted a similar effect for metal plates in vacuum. Casimir, who worked at the Dutch Electronics company Philips, wanted to understand why it was so difficult to build television tubes. The light-emitting surface in a cathode ray tube – or today, in a plasma display – of a television, the phosphor, is made by deposing small neutral, but conductive particles on glass. Casimir observed that the particles somehow attracted each other. Casimir got interested in understanding how neutral particles interact. During these theoretical studies he discovered that two neutral metal plates (or metal mirrors) would attract each other even in complete vacuum. This is the famous *Casimir effect*. Casimir also determined the attraction strength between a sphere and a plate, and between two spheres. In fact, all *conducting* neutral bodies attract each other in vacuum, with a force depending on their geometry.

Ref. 92, Ref. 93 eac

Ref. 91

In all these situations, the role of the sea is taken by the zero-point fluctuations of the electromagnetic field, the role of the ships by the conducting bodies. Casimir understood that the space between two parallel conducting mirrors, due to the geometrical constraints, had different zero-point fluctuations than the free vacuum. Like in the case of two ships, the result would be the attraction of the two mirrors.

Casimir predicted that the attraction for two mirrors of mass m and surface A at distance d is given by

$$\frac{ma}{A} = \frac{\pi^3}{120} \frac{\hbar c}{d^4} \,.$$
 (17)

The effect is a pure quantum effect; in classical electrodynamics, two neutral bodies do not attract. The effect is small; it takes some dexterity to detect it. The first experimental confirmation was by Derjaguin, Abrikosova and Lifshitz in 1956; the second experimental confirmation was by Marcus Sparnaay, Casimir's colleague at Philips, in 1958. Two beautiful high-precision measurements of the Casimir effect were performed in 1997 by Lamoreaux and in 1998 by Mohideen and Roy; they confirmed Casimir's prediction with a precision of 5 % and 1 % respectively. (Note that at very small distances,

Ref. 97 the dependence is not  $1/d^4$ , but  $1/d^3$ .) In summary, uncharged bodies attract through electromagnetic field fluctuations.

The Casimir effect thus confirms the existence of the zero-point fluctuations of the electromagnetic field. It confirms that quantum theory is valid also for electromagnetism.

The Casimir effect between two spheres is proportional to  $1/r^7$  and thus is much weaker than between two parallel plates. Despite this strange dependence, the fascination of the Casimir effect led many amateur scientists to speculate that a mechanism similar to the Casimir effect might explain gravitational attraction. Can you give at least three arguments why this is impossible, even if the effect had the correct distance dependence?

Like the case of sound, the Casimir effect can also produce repulsion instead of attraction. It is sufficient that one of the two materials be perfectly permeable, the other a perfect conductor. Such combinations repel each other, as Timothy Boyer discovered in 1974.

In a cavity, spontaneous emission is suppressed, if it is smaller than the wavelength of the emitted light! This effect has also been observed. It confirms that spontaneous emission is emission stimulated by the zero point fluctuations.

The Casimir effect bears another surprise: between two metal plates, the speed of light changes and can be larger than *c*. Can you imagine what exactly is meant by 'speed of light' in this context?

In 2006, the Casimir effect provided another surprise. The ship story just presented is beautiful, interesting and helps understanding the effect; but it seems that the story is based on a misunderstanding. Alas, the interpretation of the old naval text given by Sipko Boersma seems to be wishful thinking. There might be such an effect for ships, but

Ref. 90 Sipko Boersma seems to be wishful thinking. There might be such an effect for ships, but it has never been observed nor put into writing by seamen, as Fabrizio Pinto has pointed out after carefully researching naval sources. As an analogy however, it remains valid.

# THE LAMB SHIFT

In the old days, it was common that a person receives the Nobel Prize in Physics for observing the colour of a lamp – if the observation was sufficiently careful. In 1947, Willis Lamb (b. 1913 Los Angeles, d. 2008 Tucson) performed such a careful measurement of the spectrum of hydrogen. He found that the  $2S_{1/2}$  energy level in atomic hydrogen lies slightly above the  $2P_{1/2}$  level. This observation is in contrast to the calculation performed earlier on, where the two levels are predicted to have the same energy. In contrast, the measured energy difference is 1057.864 MHz, or 4.3 µeV. This discovery had important consequences for the description of quantum theory and yielded Lamb a share of the 1955 Nobel Prize in Physics. Why?

The reason for contrast between calculation and observation is an approximation performed in the relativistic calculation of the hydrogen levels that took over twenty years to clarify. There are two equivalent explanations. One explanation is to say that the relativistic calculation neglects the coupling terms between the Dirac equation and the Maxwell equations. This explanation lead to the first calculations of the Lamb shift, around the year 1950. The other, equivalent explanation is to say that the calculation *neglects virtual particles*. In particular, the calculation neglects the virtual photons emitted and absorbed during the motion of the electron around the nucleus. This second explanation is in line with the modern vocabulary of quantum electrodynamics. Quantum electrodynamics, or QED, is the (perturbative) approach to solve the coupled Dirac and Maxwell equations.

Challenge 71 s

Ref. 99

Ref. 98

Challenge 72 s

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In short, Lamb discovered the first effect due to virtual particles. In fact, Lamb used microwaves for his experiments; only in the 1970 it became possible to see the Lamb shift with optical means. For this and similar feats Arthur Schawlow received the Nobel Prize in Physics in 1981.

# THE QED LAGRANGIAN AND ITS SYMMETRIES

In simplified terms, *quantum electrodynamics* is the description of electron motion. This implies that the description is fixed by the effects of mass and charge, and by the quantum of action. The QED Lagrangian density is given by:

$$\mathcal{L}_{\text{QED}} = \overline{\psi}(i\hbar c \partial - c^2 m_k) \psi$$
 the matter term  

$$-\frac{1}{4\mu_0} F_{\mu\nu} F^{\mu\nu}$$
 the electromagnetic field term (18)  

$$+ e\hbar c A_{\mu} \overline{\psi} \gamma^{\mu} \psi .$$
 the electromagnetic interaction term

We know the matter term from the Dirac equation for free particles; it describes the kinetic energy of free electrons. We know the term of the electromagnetic field from the Maxwell's equations; it describes the kinetic energy of photons. The interaction term is the term that encodes the gauge symmetry of electromagnetism, also called 'minimal coupling'; it encodes the potential energy. In other words, the Lagrangian describes the motion of electrons and photons.

All experiments ever performed agree with the prediction by this Lagrangian. In other words, this Lagrangian is the final and correct description of the motion of electrons and photons. In particular, the Lagrangian describes the size, shape and colour of atoms, the size, shape and colour of molecules, as well as all interactions of molecules. In short, the Lagrangian describes all of materials science, all of chemistry and all of biology. Exaggerating a bit, this is the Lagrangian that describes life. (In fact, the description of atomic nuclei must be added; we will explore it below.)

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All electromagnetic effects, including the growth of the coloured spots on butterfly wings, the functioning of the transistor or the cutting of paper with scissors, are completely described by the QED Lagrangian. In fact, the Lagrangian also describes the motion of muons, tau leptons and all other charged particles. Since the Lagrangian is part of the final description of motion, it is worth thinking about it in more detail.

Which requirements are necessary to deduce the QED Lagrangian? This issue has been explored in great detail. The answer is given by the following list:

- compliance with the observer-invariant quantum of action for the motion of electrons and photons,
- symmetry under the permutation group among many electrons, i.e., fermion behaviour of electrons,
- compliance with the invariance of the speed of light, i.e., symmetry under transformations of special relativity,
- symmetry under U(1) gauge transformations for the motion of photons and of charged electrons,
- symmetry under renormalization group,

- low-energy interaction strength described by the *fine structure constant*, the electromagnetic coupling constant,  $\alpha \approx 1/137.036$ .

The last two points require some comments. As in all cases of motion, the action is the time-volume integral of the Lagrangian density. All fields, be they matter and radiation, move in such a way that this action remains minimal. In fact there are no known differences between the prediction of the least action principle based on the QED Lagrangian density and observations. Even though the Lagrangian density is known since 1926, it took another twenty years to learn how to calculate with it. Only in the years around 1947 it became clear, through the method of *renormalization*, that the Lagrangian density of QED is the *final* description of all motion of matter due to electromagnetic interaction in flat space-time. The details were developed independently by Julian Schwinger, Freeman Dyson, Richard Feynman and Tomonaga Shin'ichiro, four among the smartest physicists ever. \*

The QED Lagrangian density contains the strength of the electromagnetic interaction in the form of the fine structure constant  $\alpha = e^2/(4\pi\epsilon_0\hbar c) \approx 1/137.036(1)$ . This number is part of the Lagrangian; no explanation for its value is given, and the explanation was still unknown in the year 2016. It is one of the hardest puzzles of physics. Also the U(1) gauge group is specific to electromagnetism. All others requirements are valid for every type of interaction. Indeed, the search for the Lagrangians of the two nuclear interactions became really focused and finally successful only when the necessary requirements were clearly spelled out, as we will discover in the rest of this volume.

#### Vol. I, page 434 Challenge 73 e

The Lagrangian density retains all symmetries that we know from classical physics. Motion is continuous, it conserves energy-momentum and angular momentum, it is relative, it is right-left symmetric, it is reversible, i.e., symmetric under change of velocity sign, and it is lazy, i.e., it minimizes action. In short, within the limits given by the quantum of action, also motion due to QED remains predictable.

#### INTERACTIONS AND VIRTUAL PARTICLES

The electromagnetic interaction is exchange of virtual photons. So how can the interaction be attractive? At first sight, any exchange of virtual photons should drive the electrons from each other. However, this is not correct. The momentum of virtual photons does not have to be in the direction of its energy flow; it can also be in opposite direction.\*\* Obviously, this is only possible within the limits provided by the indeterminacy relation.

But virtual particles have also other surprising properties: virtual photons for example, cannot be counted.

<sup>\*</sup> Tomonaga Shin'ichiro (b. 1906 Tokio, d. 1979 Tokio) developed quantum electrodynamics and won the 1965 Nobel Prize in Physics together with Feynman and Schwinger. Later he became an important figure of science politics; together with his class mate from secondary school and fellow physics Nobel Prize winner, Yukawa Hidei, he was an example to many scientists in Japan.

<sup>\*\*</sup> One of the most beautiful booklets on quantum electrodynamics which makes this point remains the text by RICHARD FEYNMAN, *QED: the Strange Theory of Light and Matter*, Penguin Books, 1990.

#### VACUUM ENERGY: INFINITE OR ZERO?

The strangest result of quantum field theory is the energy density of the vacuum. On one side, the vacuum has, to an excellent approximation, no mass and no energy content. The vacuum energy of vacuum is thus measured and expected to be *zero* (or at least extremely small).\*

On the other side, the energy density of the zero-point fluctuations of the electromagnetic field is given by

$$\frac{E}{V} = \frac{4\pi h}{c^3} \int_0^\infty v^3 \mathrm{d}v \;. \tag{19}$$

The result of this integration is infinite. Quantum field theory thus predicts an *infinite* energy density of the vacuum.

We can try to moderate the problem in the following way. As we will discover in the last part of our adventure, there are good arguments that a smallest measurable distance exists in nature; this smallest length appears when gravity is taken into account. The minimal distance is of the order of the *Planck length* 

$$l_{\rm Pl} = \sqrt{\hbar G/c^3} \approx 1.6 \cdot 10^{-35} \,\mathrm{m} \;.$$
 (20)

Vol. VI, page 40 A minimal distance leads to a maximum cut-off frequency. But even in this case the vacuum density that follows is still a huge number, and is much larger than observed by over 100 orders of magnitude. In other words, QED seems to predict an infinite, or, when gravity is taken into account, a huge vacuum energy. But measurements show a tiny value. What exactly is wrong in this simple calculation? The answer cannot be given at this point; it will become clear in the last volume of our adventure.

# MOVING MIRRORS

Mirrors also work when they or the light source is in motion. In contrast, walls, i.e., sound mirrors, do *not* produce echoes for every sound source or for every wall speed. For example, experiments show that walls do not produce echoes if the wall or the sound source moves faster than sound. Walls do not produce echoes even if the sound source moves with them, if both objects move faster than sound. On the other hand, light mirrors *always* produce an image, whatever the involved speed of the light source or the mirror may be. These observations confirm that the speed of light is the same for all observers: it is *invariant* and a limit speed. (Can you detail the argument?) In contrast, the speed of sound in air depends on the observer; it is *not* invariant.

Challenge 74 s

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Vol. II, page 22

Light mirrors also differ from tennis rackets. (Rackets are tennis ball mirrors, to continue the previous analogy.) We have seen that light mirrors cannot be used to change the speed of the light they hit, in contrast to what tennis rackets can do with balls. This observation shows that the speed of light is a *limit* speed. In short, the simple existence of mirrors and of their properties are sufficient to derive special relativity.

<sup>\*</sup> In 1998, this side of the issue was confused even further. Astrophysical measurements, confirmed in the subsequent years, have found that the vacuum energy has a small, but non-zero value, of the order of  $0.5 \text{ nJ/m}^3$ . The reason for this value is not yet understood, and is one of the open issues of modern physics.

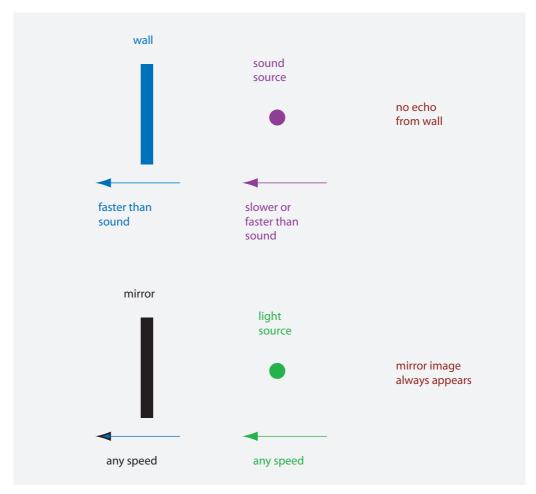


FIGURE 80 A fast wall does not produce an echo; a fast mirror does.

But there are more interesting things to be learned from mirrors. We only have to ask whether mirrors work when they undergo *accelerated* motion. This issue yields a surprising result.

In the 1970s, quite a number of researchers independently found that there is no vacuum for accelerated observers. This effect is called *Fulling–Davies–Unruh effect*. (The incorrect and rarely used term *dynamical Casimir effect* has been abandoned.) For an accelerated observer, the vacuum is full of heat radiation. We will discuss this below. This fact has an interesting consequence for accelerated mirrors: a mirror in accelerated motion reflects the heat radiation it encounters. In short, *an accelerated mirror emits light*! Unfortunately, the intensity of this so-called *Unruh radiation* is so weak that it has not been measured directly, up to now. We will explore the issue in more detail below. (Can you explain why accelerated mirrors emit light, but not matter?)

Page 147 Challenge 75 s 130

# Photons hitting photons

Usually, light can cross light undisturbed: interference is the proof and the result of this basic property of light. But there is an exception. When virtual particles are taken into account, light beams can 'bang' onto each other – though only slightly. This result is in full contrast to classical electrodynamics.

Indeed, QED shows that the appearance of virtual electron-positron pairs allow photons to hit each other. And such pairs are found in any light beam. However, the cross-section for photons banging onto each other is small. In other words, the bang is extremely weak. When two light beams cross, most photons will pass undisturbed. The cross-section *A* is approximately

$$A \approx \frac{973}{10\,125\pi} \,\alpha^4 \left(\frac{\hbar}{m_{\rm e}c}\right)^2 \left(\frac{\hbar\omega}{m_{\rm e}c^2}\right)^6 \tag{21}$$

for the everyday case that the energy  $\hbar \omega$  of the photon is much smaller than the rest energy  $m_ec^2$  of the electron. This low-energy value is about 18 orders of magnitude smaller than what was measurable in 1999; the future will show whether the effect will ever be observable for visible light. However, for high energy photons these effects are observed daily in particle accelerators. In these settings one observes not only interaction through virtual electron–antielectron pairs, but also through virtual muon–antimuon pairs, virtual quark–antiquark pairs, and much more.

Everybody who consumes science fiction knows that matter and antimatter annihilate and transform into pure light. More precisely, a matter particle and an antimatter particle annihilate into two or more photons. Interestingly, quantum theory predicts that the opposite process is also possible: photons hitting photons can produce matter! In 1997, this prediction was also confirmed experimentally.

At the Stanford particle accelerator, photons from a high energy laser pulse were bounced off very fast electrons. In this way, the reflected photons acquired a large energy, when seen in the inertial frame of the experimenter. The green laser pulse, of 527 nm wavelength or 2.4 eV photon energy, had a peak power density of  $10^{22}$  W/m<sup>2</sup>, about the highest achievable so far. That is a photon density of  $10^{34}$  /m<sup>3</sup> and an electric field of  $10^{12}$  V/m, both of which were record values at the time. When this green laser pulse was reflected off a 46.6 GeV electron beam, the returning photons had an energy of 29.2 GeV and thus had become high-energy gamma rays. These gamma rays then collided with other, still incoming green photons and produced electron–positron pairs through the reaction

$$\gamma_{29.2\text{GeV}} + n \gamma_{\text{green}} \rightarrow e^+ + e^-$$
(22)

for which both final particles were detected by special apparatuses. The experiment thus showed that light can hit light in nature, and above all, that doing so can produce matter. This is the nearest we can get to the science fiction fantasy of light swords or of laser swords *banging* onto each other.

Ref. 100

Challenge 76 e

#### IS THE VACUUM A BATH?

If the vacuum is a sea of virtual photons and particle–antiparticle pairs, vacuum could be suspected to act as a bath. In general, the answer is negative. Quantum field theory works because the vacuum is *not* a bath for single particles. However, there is always an exception. For dissipative systems made of many particles, such as electrical conductors, the vacuum *can* act as a viscous fluid. Irregularly shaped, neutral, but conducting bodies can emit photons when accelerated, thus damping such type of motion. This is due to the Fulling–Davies–Unruh effect, as described above. The damping depends on the shape and thus also on the direction of the body's motion.

In 1998, Gour and Sriramkumar even predicted that Brownian motion should also appear for an imperfect, i.e., partly absorbing *mirror* placed in vacuum. The fluctuations of the vacuum should produce a mean square displacement

$$\langle d^2 \rangle = \frac{\hbar}{m} t \tag{23}$$

that increases linearly with time; however, the extremely small displacement produced in this way is out of experimental reach so far. But the result is not a surprise. Are you able to give another, less complicated explanation for it?

#### RENORMALIZATION - WHY IS AN ELECTRON SO LIGHT?

In classical physics, the field energy of a point-like charged particle, and hence its mass, was predicted to be infinite. QED effectively *smears out* the charge of the electron over its Compton wavelength; as a result, the field energy contributes only a small correction to its total mass. Can you confirm this?

QED is a *perturbative* description. This means, that any predicted result *R* is found as a Taylor series of powers of a small parameter:

$$R = R_0 + R_1 \alpha + R_2 \alpha^2 + R_3 \alpha^3 + R_4 \alpha^4 + \dots$$
(24)

In QED, the small parameter is the fine structure constant  $\alpha = 1/137.036(1)$ . With the help of the perturbation series, the exact result *R* is approximated more and more precisely.

Now, in QED, many intermediate results in the perturbation expansion are divergent integrals, i.e., integrals with infinite value. The divergence is due to the assumption that infinitely small distances are possible in nature. The divergences thus are artefacts that can be eliminated; the elimination procedure is called renormalization.

Sometimes it is claimed that the infinities appearing in quantum electrodynamics in the intermediate steps of the calculation show that the theory is incomplete or wrong. However, this type of statement would imply that classical physics is also incomplete or wrong, on the ground that in the definition of the velocity v with space x and time t, namely

$$v = \frac{\mathrm{d}x}{\mathrm{d}t} = \lim_{\Delta t \to 0} \frac{\Delta x}{\Delta t} = \lim_{\Delta t \to 0} \Delta x \frac{1}{\Delta t} , \qquad (25)$$

Ref. 101

Vol. I, page 391

Ref. 102

Challenge 77 ny

Vol. III, page 243

Challenge 78 s

#### THE ORIGIN OF VIRTUAL REALITY

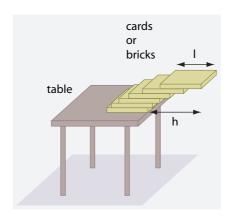


FIGURE 81 What is the maximum possible value of h/l?

one gets an infinity as intermediate step. Indeed, dt being vanishingly small, one could argue that one is dividing by zero. Both arguments show the difficulty to accept that the result of a limit process can be a finite quantity even if infinite quantities appear in the calculation. The parallel between electron mass and velocity is closer than it seems; both intermediate 'infinities' stem from the assumption that space-time is continuous, i.e., infinitely divisible. The infinities necessary in limit processes for the definition of differentiation, integration or for renormalization appear only when space-time is approximated, as physicists say, as a 'continuous' set, or as mathematicians say, as a 'complete' set.

On the other hand, the conviction that the appearance of an infinity might be a sign of incompleteness of a theory was an interesting development in physics. It shows how uncomfortable many physicists had become with the use of infinity in our description of nature. Notably, this was the case for Paul Dirac himself, who, after having laid in his youth the basis of quantum electrodynamics, has tried for the rest of his life to find a way, without success, to change the theory so that intermediate infinities are avoided.

Renormalization is a procedure that follows from the requirement that continuous space-time and gauge theories must work together. In particular, renormalization follows form the requirement that the particle concept is consistent, i.e., that perturbation expansions are possible. Intermediate infinities are not an issue. In a bizarre twist, a few decades after Dirac's death, his wish has been fulfilled after all, although in a different manner than he envisaged. The final part of this mountain ascent will show the way out of the issue.

Ref. 103

Vol. VI, page 37

# Curiosities and fun challenges of quantum electrodynamics

Motion is an interesting topic, and when a curious person asks a question about it, most of the time quantum electrodynamics is needed for the answer. Together with gravity, quantum electrodynamics explains almost all of our everyday experience, including numerous surprises. Let us have a look at some of them.

\* \*

A famous riddle, illustrated in Figure 81, asks how far the last card (or the last brick) of a stack can hang over the edge of a table. Of course, only gravity, no glue nor any other

Challenge 79 s

Ref. 104

Page 154

Ref. 105

Page 343

life.

Challenge 80 s

means is allowed to keep the cards on the table. After you solved the riddle, can you give the solution in case that the quantum of action is taken into account?

Quantum electrodynamics explains why there are only a *finite* number of different atom types. In fact, it takes only two lines to prove that pair production of electronantielectron pairs make it impossible that a nucleus has more than about 137 protons. Can you show this? In short, the fine structure constant limits the number of chemical elements in nature. The effect at the basis of this limit, the polarization of the vacuum, also plays a role in much larger systems, such as charged black holes, as we will see shortly.

Stripping 91 of the 92 electrons off an uranium atom allows researchers to check with high precision whether the innermost electron still is described by QED. The electric field near the uranium nucleus, 1 EV/m, is the highest achievable in the laboratory; the field value is near the threshold for spontaneous pair production. The field is the highest constant field producible in the laboratory, and an ideal testing ground for precision QED experiments. The effect of virtual photons is to produce a Lamb shift; but even for these extremely high fields, the value matches the calculation.

\* \*

\* \*

Challenge 81 ny Challenge 81 ny Spontaneous pair production? \*\* Microscopic evolution can be pretty slow. Light, especially when emitted by single atoms, is always emitted by some metastable state. Usually, the decay times, being induced by the vacuum fluctuations, are much shorter than a microsecond. However, there are metastable atomic states with a lifetime of ten years: for example, an ytterbium ion in the  ${}^{2}F_{7/2}$ state achieves this value, because the emission of light requires an octupole transition, in which the angular momentum changes by  $3\hbar$ ; this is an extremely unlikely process. In radioactive decay, the slowness record is held by  ${}^{209}$ Bi, with over  $10^{19}$  years of half-

Challenge 82 s Microscopic evolution can be pretty fast. Can you imagine how to deduce or to measure the speed of electrons inside atoms? And inside metals?

If an electrical wire is sufficiently narrow, its electrical conductance is quantized in steps<br/>of  $2e^2/\hbar$ . The wider the wire, the more such steps are added to its conductance. Can you<br/>explain the effect? By the way, quantized conductance has also been observed for light<br/>and for phonons.

\* \*

\* \*

The Casimir effect, as well as other experiments, imply that there is a specific and *finite* energy density that can be ascribed to the vacuum. Does this mean that we can apply the Banach–Tarski effect to pieces of vacuum?

Challenge 85 s Can you explain why mud is not clear?

Ref. 201

The instability of the vacuum also yields a (trivial) limit on the fine structure constant. The fine structure constant value of around 1/137.036 cannot be explained by quantum electrodynamics. However, it can be deduced that it must be lower than 1 to lead to a consistent theory. Indeed, if its value were larger than 1, the vacuum would become unstable and would spontaneously generate electron-positron pairs.

\* \*

Challenge 86 s Can the universe ever have been smaller than its own Compton wavelength?

In the past, the description of motion with formulae was taken rather seriously. Before computers appeared, only those examples of motion were studied that could be described with simple formulae. But this narrow-minded approach turns out to be too restrictive. Indeed, mathematicians showed that Galilean mechanics cannot solve the three-body problem, special relativity cannot solve the two-body problem, general relativity the one-body problem and quantum field theory the zero-body problem. It took some time to the community of physicists to appreciate that understanding motion does not depend on the description by formulae, but on the description by clear equations based on space and time.

\* \*

In fact, quantum electrodynamics, or QED, provides a vast number of curiosities and every year there is at least one interesting new discovery. We now conclude the theme with a more general approach.

### How can one move on perfect ice? - The ultimate physics test

In our quest, we have encountered motion of many sorts. Therefore, the following test – not to be taken too seriously – is the ultimate physics test, allowing you to check your understanding and to compare it with that of others.

Imagine that you are on a perfectly frictionless surface and that you want to move to its border. How many methods can you find to achieve this? Any method, so tiny its effect may be, is allowed.

*Classical physics* provided quite a number of methods. We saw that for rotating ourselves, we just need to turn our arm above the head. For translation motion, throwing a shoe or inhaling vertically and exhaling horizontally are the simplest possibilities. Can you list at least six additional methods, maybe some making use of the location of the surface on Earth? What would you do in space?

Challenge 87 s

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	Electrodynamics and thermodynamics taught us that in vacuum, heating one side of
	the body more than the other will work as motor; the imbalance of heat radiation will
	push you, albeit rather slowly. Are you able to find at least four other methods from these
Challenge 88 s	two domains?
	General relativity showed that turning one arm will emit gravitational radiation un-
Challenge 89 s	symmetrically, leading to motion as well. Can you find at least two better methods? <i>Quantum theory</i> offers a wealth of methods. Of course, quantum mechanics shows
	that we actually are always moving, since the indeterminacy relation makes rest an im-
	possibility. However, the average motion can be zero even if the spread increases with
	time. Are you able to find at least four methods of moving on perfect ice due to quantum
Challenge 90 s	effects?
	Materials science, geophysics, atmospheric physics and astrophysics also provide ways
Challenge 91 s	to move, such as cosmic rays or solar neutrinos. Can you find four additional methods? <i>Self-organization, chaos theory and biophysics</i> also provide ways to move, when the
	inner workings of the human body are taken into account. Can you find at least two
Challenge 92 s	methods?
	Assuming that you read already the section following the present one, on the effects
	of semiclassical quantum gravity, here is an additional puzzle: is it possible to move by
Challenge 93 s	accelerating a pocket mirror, using the emitted Unruh radiation? Can you find at least two other methods to move yourself using quantum gravity effects? Can you find one
	from string theory?
	If you want points for the test, the marking is simple. For students, every working
	method gives one point. Eight points is ok, twelve points is good, sixteen points is very good, and twenty points or more is excellent. For graduated physicists, the point is given
	only when a back-of-the-envelope estimate for the ensuing momentum or acceleration
	is provided.
	A SUMMARY OF QUANTUM ELECTRODYNAMICS
	The shortest possible summary of quantum electrodynamics is the following:

▷ Everyday matter is made of charged elementary particles that interact through photon exchange in the way described by Figure 82.

No additional information is necessary. In a bit more detail, quantum electrodynamics starts with *elementary particles* – characterized by their mass, spin, charge, and parities – and with the *vacuum*, essentially a sea of virtual particle–antiparticle pairs. *Interactions* between charged particles are described as the exchange of virtual photons, and electromagnetic *decay* is described as the interaction with the virtual photons of the vacuum.

▷ The Feynman diagram of Figure 82 provides an *exact* description of *all* electromagnetic phenomena and processes.

No contradiction between observation and calculation are known. In particular, the Page 127 Feynman diagram is equivalent to the QED Lagrangian of equation (18). Because QED is a perturbative theory, the Feynman diagram directly describes the first order effects;

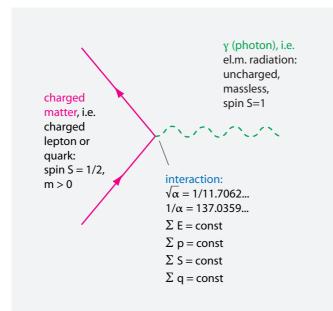


FIGURE 82 The basis of QED; more precisely, the fundamental diagram of QED as a perturbation theory in space-time.

its composite diagrams describe effects of higher order. QED is a perturbative theory.

QED describes all everyday properties of matter and radiation. It describes the *divis-ibility* down to the smallest constituents, the *isolability* from the environment and the *impenetrability* of matter. It also describes the *penetrability* of radiation. All these properties are due to electromagnetic interactions of constituents and follow from Figure 82. Matter is divisible because the interactions are of finite strength, matter is also divisible because the interactions are of finite range, and matter is impenetrable because interactions among the constituents increase in intensity when they approach each other, in particular because matter constituents are fermions. Radiation is divisible into photons, and is penetrable because photons are bosons and first order photon-photon interactions do not exist.

Both matter and radiation are made of *elementary* constituents. These elementary constituents, whether bosons or fermions, are indivisible, isolable, indistinguishable, and point-like.

It is necessary to use quantum electrodynamics in all those situations for which the characteristic dimensions d are of the order of the Compton wavelength

$$d \approx \lambda_{\rm C} = \frac{h}{m \, c} \,. \tag{26}$$

In situations where the dimensions are of the order of the de Broglie wavelength, or equivalently, where the action is of the order of the Planck value, simple quantum mechanics is sufficient:

$$d \approx \lambda_{\rm dB} = \frac{h}{m \, v} \,. \tag{27}$$

For even larger dimensions, classical physics will do.

Together with gravity, quantum electrodynamics explains almost all observations of motion on Earth; QED unifies the description of matter and electromagnetic radiation in daily life. All everyday objects and all images are described, including their properties, their shape, their transformations and their other changes. This includes self-organization and chemical or biological processes. In other words, QED gives us full grasp of the effects and the variety of motion due to electromagnetism.

# Open questions in QED

Even though QED describes motion due to electromagnetism without any discrepancy from experiment, that does not mean that we understand every detail of every example of such motion. For example, nobody has described the motion of an animal with QED yet.\* In fact, there is beautiful and fascinating research going on in many branches of electromagnetism.

Atmospheric physics still provides many puzzles and regularly delivers new, previously unknown phenomena. For example, the detailed mechanisms at the origin of au-

Ref. 112

Ref. 113

Ref. 110

Ref. 111

rorae are still controversial; and the recent unexplained discoveries of discharges *above* clouds should not make one forget that even the precise mechanism of charge separation *inside* clouds, which leads to lightning, is not completely clarified. In fact, all examples of electrification, such as the charging of amber through rubbing, the experiment which gave electricity its name, are still poorly understood.

Materials science in all its breadth, including the study of solids, fluids, and plasmas, as well as biology and medicine, still provides many topics of research. In particular, the twenty-first century will undoubtedly be the century of the life sciences.

The study of the interaction of atoms with intense light is an example of present research in atomic physics. Strong lasers can strip atoms of many of their electrons; for such phenomena, there are not yet precise descriptions, since they do not comply to the weak field approximations usually assumed in physical experiments. In strong fields, new effects take place, such as the so-called Coulomb explosion.

But also the skies have their mysteries. In the topic of cosmic rays, it is still not clear how rays with energies of 10<sup>22</sup> eV are produced outside the galaxy. Researchers are intensely trying to locate the electromagnetic fields necessary for their acceleration and to understand their origin and mechanisms.

In the theory of quantum electrodynamics, discoveries are expected by all those who study it in sufficient detail. For example, Dirk Kreimer has discovered that higher order interaction diagrams built using the fundamental diagram of Figure 82 contain relations to the theory of knots. This research topic will provide even more interesting results in the near future. Relations to knot theory appear because QED is a *perturbative* description, with the vast richness of its non-perturbative effects still hidden. Studies of QED at high energies, where perturbation is *not* a good approximation and where particle numbers are not conserved, promise a wealth of new insights.

<sup>\*</sup> On the other hand, outside QED, there is beautiful work going on how humans move their limbs; it seems that any general human movement is constructed in the brain by combining a small set of fundamental movements.

#### THE ORIGIN OF VIRTUAL REALITY



**FIGURE 83** The rainbow can only be explained fully if the fine structure constant  $\alpha$  can be calculated (© ed g2s, Christophe Afonso).

Ref. 116

If we want to be very strict, we need to add that we do *not* fully understand any colour, because we still do not know the origin of the fine structure constant. In particular, the fine structure constant determines the refractive index of water, and thus the formation of a rainbow, as pictured in Figure 83.

Many other open issues of more practical nature have not been mentioned. Indeed, by far the largest numbers of physicists get paid for some form of applied QED. In our

adventure however, our quest is the description of the *fundamentals* of motion. And so far, we have not achieved it. In particular, we still need to understand motion in the realm of atomic nuclei and the effect of the quantum of action in the domain of gravitation. We start with the latter topic.

V A

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# CHAPTER 4 QUANTUM MECHANICS WITH GRAVITATION - FIRST STEPS

Gravity, cause the worst accidents. Despite its weakness, the inclusion of ravity into quantum theory raises a number of issues. We must solve them all in order to complete our mountain ascent.

Gravity acts on quantum systems: in the chapter on general relativity we already mentioned that light frequency changes with height. Thus gravity has a simple and measurable effect on photons. But gravity also acts on all other quantum systems, such as atoms and neutrons, as we will see. And the quantum of action plays an important role in the behaviour of black holes. We explore these topics now.

#### FALLING ATOMS

In 2004 it finally became possible to repeat Galileo's leaning tower experiment with single atoms instead of steel balls. This is not an easy experiment because even the smallest effects disturb the motion. The result is as expected: single atoms do fall like stones. In particular, atoms of different mass fall with the same acceleration, within the experimental precision of one part in 6 million.

The experiment was difficult to perform, but the result is not surprising, because all falling everyday objects are made of atoms. Indeed, Galileo himself had predicted that atoms fall like stones, because parts of a body have to fall with the same acceleration as the complete body. But what is the precise effect of gravity on wave functions? This question is best explored with the help of neutrons.

# Playing table tennis with neutrons

The gravitational potential also has directly measurable effects on quantum particles. Classically, a table tennis ball follows a parabolic path when bouncing over a table tennis table, as long as friction can be neglected. The general layout of the experiment is shown in Figure 84. How does a quantum particle behave in the same setting?

In the gravitational field, a bouncing quantum particle is still described by a wave function. In contrast to the classical case however, the possible energy values of a falling quantum particle are discrete. Indeed, the quantization of the action implies that for a

Vol. I, page 202

Ref. 117

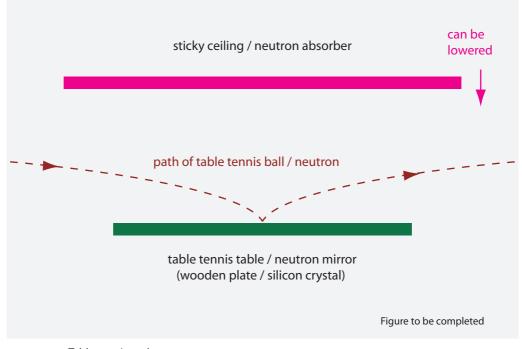


FIGURE 84 Table tennis and neutrons.

Challenge 94 e bounce of energy  $E_n$  and duration  $t_n$ ,

Ref. 118

$$n\hbar \sim E_n t_n \sim \frac{E_n^{3/2}}{qm^{1/2}}$$
 (28)

In other words, only discrete bounce heights, distinguished by the number *n*, are possible in the quantum case. The discreteness leads to an expected probability density that changes with height in discrete steps, as shown in Figure 84.

The best way to realize the experiment with quantum particles is to produce an intense beam of neutral particles, because neutral particles are not affected by the stray electromagnetic fields that are present in every laboratory. Neutrons are ideal, as they are produced in large quantities by nuclear reactors. The experiment was first performed in 2002, by Hartmut Abele and his group, after years of preparations. Using several clever tricks, they managed to slow down neutrons from a nuclear reactor to the incredibly small value of 8 m/s, comparable to the speed of a table tennis ball. (The equivalent temperature of these ultracold neutrons is 1 mK, or 100 neV.) They then directed the neutrons onto a neutron mirror made of polished glass – the analogue of the table tennis table – and observed the neutrons bouncing back up. To detect the bouncing, they lowered an absorber – the equivalent of a sticky ceiling – towards the table tennis table, i.e., towards the neutron mirror, and measured how many neutrons still reached the other end of the table. (Both the absorber and the mirror were about 20 cm in length.)

Why did the experiment take so many years of work? The lowest energy levels for neutrons due to gravity are  $2.3 \cdot 10^{-31}$  J, or 1.4 peV, followed by 2.5 peV, 3.3 peV, 4.1 peV,

stion Mountain – The Adventure of Physics copyright © Christoph Schiller June 1990–May 2020 free pdf file available at www.motionmountain.r

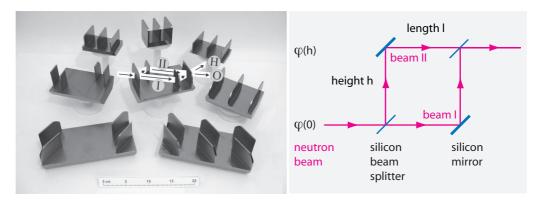


FIGURE 85 The weakness of gravitation. A neutron interferometer made of a silicon single crystal (with the two neutron beams I and II) can be used to detect the effects of gravitation on the phase of wave functions (photo © Helmut Rauch and Erwin Seidl).

and so forth. To get an impression of the smallness of these values, we can compare it to the value of  $2.2 \cdot 10^{-18}$  J or 13.6 eV for the lowest state in the hydrogen atom. Despite these small energy values, the team managed to measure the first few discrete energy levels. The results confirmed the prediction of the Schrödinger equation, with the gravitational potential included, to the achievable measurement precision.

In short, gravity influences wave functions. In particular, gravity changes the phase of wave functions, and does so as expected.

#### The gravitational phase of wave functions

Challenge 95 s Ref. 119

Ref. 120

Not only does gravity change the shape of wave functions; it also changes their *phase*. Can you imagine why? The prediction was first confirmed in 1975, using a device invented by Helmut Rauch and his team. Rauch had developed neutron interferometers based on single silicon crystals, shown in Figure 85, in which a neutron beam – again from a nuclear reactor – is split into two beams and the two beams are then recombined and brought to interference.

By rotating the interferometer mainly around the horizontal axis, Samuel Werner and his group let the two neutron beams interfere after having climbed a small height h at two different locations. The experiment is shown schematically on the right of Figure 85. The neutron beam is split; the two beams are deflected upwards, one directly, one a few centimetres further on, and then recombined.

For such a experiment in gravity, quantum theory predicts a phase difference  $\Delta \varphi$ Challenge 96 ny between the two beams given by

$$\Delta \varphi = \frac{mghl}{\hbar v} , \qquad (29)$$

where l is the horizontal distance between the two climbs and v and m are the speed and mass of the neutrons. All experiments – together with several others of similar simple elegance – have confirmed the prediction by quantum theory within experimental errors. In the 1990s, similar experiments have even been performed with complete atoms.

Ref. 121

These atom interferometers are so sensitive that local gravity g can be measured with a precision of more than eight significant digits.

In short, neutrons, atoms and photons show no surprises in gravitational fields. Gravity can be included into all quantum systems of everyday life. By including gravity in the potential, the Schrödinger and Dirac equations can thus be used, for example, to describe the growth and the processes inside trees. Trees can mostly be described with quantum electrodynamics in weak gravity.

# The gravitational Bohr atom

Can gravity lead to *bound* quantum systems? A short calculation shows that an electron circling a proton due to gravity alone, without electrostatic attraction, would do so at a gravitational Bohr radius of

$$r_{\rm gr.B.} = \frac{\hbar^2}{G \, m_{\rm e}^2 \, m_{\rm p}} = 1.1 \cdot 10^{29} \, {\rm m}$$
 (30)

which is about a thousand times the distance to the cosmic horizon. A gravitational Bohr atom would be larger than the universe. This enormous size is the reason that in a normal hydrogen atom there is not a *single way* to measure gravitational effects between its components. (Are you able to confirm this?)

But why is gravity so weak? Or equivalently, why are the universe and normal atoms so much smaller than a gravitational Bohr atom? At the present point of our quest these questions cannot be answered. Worse, the weakness of gravity even means that with high probability, future experiments will provide little additional data helping to decide among competing answers. The only help is careful thought.

We might conclude from all this that gravity does not require a quantum description. Indeed, we stumbled onto quantum effects because classical electrodynamics implies, in stark contrast with reality, that atoms decay in about 0.1 ns. Classically, an orbiting electron would emit radiation until it falls into the nucleus. Quantum theory is thus necessary to explain the existence of matter.

When the same stability calculation is performed for the emission of gravitational radiation by orbiting electrons, one finds a decay time of around  $10^{37}$  s. (True?) This extremely large value, trillions of times longer than the age of the universe, is a result of the low emission of gravitational radiation by rotating masses. Therefore, the existence of normal atoms does not require a quantum theory of gravity.

# Curiosities about quantum theory and gravity

Due to the influence of gravity on phases of wave functions, some people who do not believe in bath induced decoherence have even studied the influence of gravity on the decoherence process of usual quantum systems in flat space-time. Predictably, the calculated results do not reproduce experiments.

\* \*

Despite its weakness, gravitation provides many puzzles. Most famous are a number of

144

Challenge 98 e

Challenge 99 nv

Vol. II, page 179

Ref. 145

curious coincidences that can be found when quantum mechanics and gravitation are combined. They are usually called 'large number hypotheses' because they usually involve large dimensionless numbers. A pretty, but less well known version connects the Planck length, the cosmic horizon  $R_0$ , and the number of baryons  $N_b$ :

Ref. 146

Ref. 148

Challenge 100 s

$$\left(N_{\rm b}\right)^3 \approx \left(\frac{R_0}{l_{\rm Pl}}\right)^4 = \left(\frac{t_0}{t_{\rm Pl}}\right)^4 \approx 10^{244} \tag{31}$$

in which  $N_b = 10^{81}$  and  $t_0 = 1.2 \cdot 10^{10}$  a were used. There is no known reason why the number of baryons and the horizon size  $R_0$  should be related in this way. This coincidence is equivalent to the one originally stated by Dirac,\* namely

$$m_{\rm p}^3 \approx \frac{\hbar^2}{Gct_0} \,. \tag{33}$$

where  $m_p$  is the proton mass. This approximate equality seems to suggest that certain microscopic properties, namely the mass of the proton, is connected to some general properties of the universe as a whole. This has lead to numerous speculations, especially since the time dependence of the two sides differs. Some people even speculate whether relations (31) or (33) express some long-sought relation between local and global topological properties of nature. Up to this day, the only correct statement seems to be that they are *coincidences* connected to the time at which we happen to live, and that they should not be taken too seriously.

Photons not travelling parallel to each other attract each other through gravitation and thus deflect each other. Could two such photons form a bound state, a sort of atom of light, in which they would circle each other, provided there were enough empty space for this to happen?

\* \*

In summary, quantum gravity is unnecessary in every single domain of everyday life. However, we will see now that quantum gravity is necessary in domains which are more remote, but also more fascinating.

$$m_0^2/R_0^2 \approx m_{\rm Pl}^2/R_{\rm Pl}^2 = c^4/G^2$$
 (32)

Ref. 147 \* The equivalence can be deduced using  $Gn_bm_p = 1/t_0^2$ , which, as Weinberg explains, is required by several Vol. VI, page 104 cosmological models. Indeed, this can be rewritten simply as

Together with the definition of the baryon density  $n_b = N_b/R_0^3$  one gets Dirac's large number hypothesis, substituting protons for pions. Note that the Planck time and length are defined as  $\sqrt{\hbar G/c^5}$  and  $\sqrt{\hbar G/c^3}$  and are the natural units of length and time. We will study them in detail in the last part of the mountain ascent.

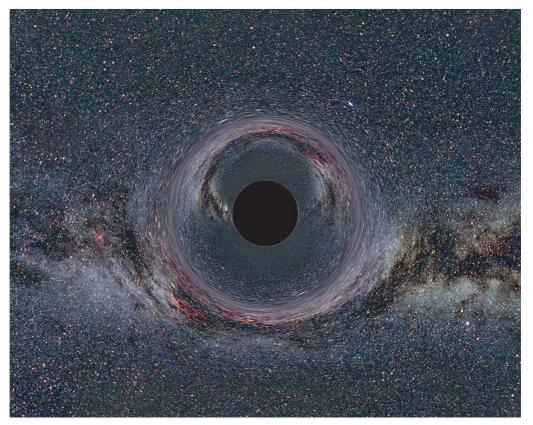


FIGURE 86 A simplified simulated image – not a photograph – of how a black hole of ten solar masses, with Schwarzschild radius of 30 km, seen from a constant distance of 600 km, will distort an image of the Milky Way in the background (image © Ute Kraus at www.tempolimit-lichtgeschwindigkeit.de).

#### GRAVITATION AND LIMITS TO DISORDER

C Die Energie der Welt ist constant. Die Entropie der Welt strebt einem Maximum zu.\* Rudolph Clausius

Vol. I, page 256

We have already encountered the famous statement by Clausius, the father of the term 'entropy'. We have also found that the Boltzmann constant k is the smallest entropy value found in nature.

What is the influence of gravitation on entropy, and on thermodynamics in general? For a long time, nobody was interested in this question. In parallel, for many decades nobody asked whether there also exists a theoretical *maximum* for entropy. The situations changed dramatically in 1973, when Jacob Bekenstein discovered that the two issues are related.

Ref. 122

Bekenstein was investigating the consequences gravity has for quantum physics. He

<sup>\* &#</sup>x27;The energy of the universe is constant. Its entropy tends towards a maximum.'

found that the entropy *S* of an object of energy *E* and size *L* is bound by

$$S \leq EL \frac{k\pi}{\hbar c} \tag{34}$$

for all physical systems, where k is the Boltzmann constant. In particular, he deduced that (nonrotating) *black holes* saturate the bound. We recall that black holes are the densest systems for a given mass. They occur when matter collapses completely. Figure 86 shows an artist's impression.

Challenge 101 s

Vol. II, page 262

Bekenstein found that black holes have an entropy given by

$$S = A \frac{kc^3}{4G\hbar} = M^2 \frac{4\pi kG}{\hbar c}$$
(35)

where A is now the area of the *horizon* of the black hole. It is given by  $A = 4\pi R^2 = 4\pi (2GM/c^2)^2$ . In particular, the result implies that every black hole has an entropy. Black holes are thus disordered systems described by thermodynamics. In fact, *black holes are the most disordered systems known.*\*

As an interesting note, the maximum entropy also implies an upper memory limit for memory chips. Can you find out how?

Black hole entropy is somewhat mysterious. What are the different microstates leading to this macroscopic entropy? It took many years to convince physicists that the microstates are due to the various possible states of the black hole horizon itself, and that they are somehow due to the diffeomorphism invariance at this boundary. As Gerard 't Hooft explains, the entropy expression implies that the number of degrees of freedom of a black hole is about (but not exactly) one per Planck area of the horizon.

If black holes have entropy, they must have a temperature. What does this temperature mean? In fact, nobody believed this conclusion until two unrelated developments confirmed it within a short time.

# Measuring acceleration with a thermometer: Fulling-Davies-Unruh radiation

Ref. 125

Independently, Stephen Fulling in 1973, Paul Davies in 1975 and William Unruh in 1976 made the same theoretical discovery while studying quantum theory: if an inertial observer observes that he is surrounded by vacuum, a second observer *accelerated* with respect to the first does not: he observes black body radiation. The appearance of radiation for an accelerated observer in vacuum is called the *Fulling–Davies–Unruh effect*. All

Ref. 124

Challenge 103 s

Challenge 102 s

<sup>\*</sup> The precise discussion that black holes are the most disordered systems in nature is quite subtle. The issue Ref. 123 is summarized by Bousso. Bousso claims that the area appearing in the maximum entropy formula cannot be taken naively as the area at a given time, and gives four arguments why this should be not allowed. However, all four arguments are wrong in some way, in particular because they assume that lengths smaller than the Planck length or larger than the universe's size can be measured. Ironically, he brushes aside some of the arguments himself later in the paper, and then deduces an improved formula, which is exactly the same as the one he criticizes first, just with a different interpretation of the area *A*. Later in his career, Bousso revised his conclusions; he now supports the maximum entropy bound. In short, the expression of black hole entropy is indeed the maximum entropy for a physical system with surface *A*.

these results about black holes were waiting to be discovered since the 1930s; incredibly, nobody had thought about them for the subsequent 40 years.

The radiation has a spectrum corresponding to the temperature

$$T = \frac{\hbar}{2\pi kc} a , \qquad (36)$$

where *a* is the magnitude of the acceleration. The result means that there is no vacuum on Earth, because any observer on its surface can maintain that he is accelerated with 9.8 m/s<sup>2</sup>, thus leading to T = 40 zK! We can thus measure gravity, at least in principle, using a thermometer. However, even for the largest practical accelerations the temperature values are so small that it is questionable whether the effect will ever be confirmed experimentally in this precise way. But if it will, it will be a beautiful experimental result.

When this effect was predicted, people explored all possible aspects of the argument. For example, also an observer in rotational motion detects radiation following expression (36). But that was not all. It was found that the simple acceleration of a *mirror* leads to radiation *emission*! Mirrors are thus harder to accelerate than other bodies of the same mass.

When the acceleration is high enough, also *matter* particles can be emitted and detected. If a particle counter is accelerated sufficiently strongly across the vacuum, it will start counting particles! We see that the difference between vacuum and matter becomes fuzzy at large accelerations. This result will play an important role in the search for unification, as we will discover later on.

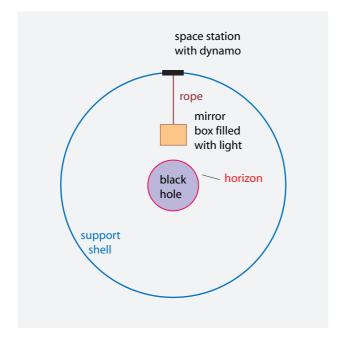
Surprisingly, at the end of the twentieth century it became clear that the Fulling-Davies-Unruh effect possibly had already been observed before it was predicted! The Fulling-Davies-Unruh effect turned out be related to a well-established observation: the so-called Sokolov-Ternov effect. In 1963, the Russian physicist Igor Ternov, together with Arsenji Sokolov, had used the Dirac equation to predict that electrons in circular accelerators and in storage rings that circulate at high energy would automatically polarize. The prediction was first confirmed by experiments at the Russian Budker Institute of Nuclear Physics in 1971, and then confirmed by experiments in Orsay, in Stanford and in Hamburg. Nowadays, the effect is used routinely in many accelerator experiments. In the 1980s, Bell and Leinaas realized that the Sokolov-Ternov effect is the same effect as the Fulling–Davies–Unruh effect, but seen from a different reference frame! The equival-Ref. 127 ence is somewhat surprising. In charges moving in a storage ring, the emitted radiation is not thermal, so that the analogy is not obvious or simple. But the effect that polarizes the beam - namely the difference in photon emission for spins that are parallel and antiparallel to the magnetic field – is the same as the Fulling–Davies–Unruh effect. We thus have another case of a theoretical discovery that was made much later than necessary. In 2006 however, this equivalence was put into question again. The issue is not closed. Ref. 127

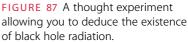
## Black holes aren't black

In 1973 and 1974, Jacob Bekenstein, and independently, Stephen Hawking, famous for the intensity with which he fights a disease which forces him into the wheelchair, surprised the world of general relativity with a fundamental theoretical discovery. They found that

Ref. 126

Vol. VI, page 65





if a virtual particle–antiparticle pair appeared in the vacuum near the horizon, there is a finite chance that one particle escapes as a real particle, while the virtual antiparticle is captured by the black hole. The virtual antiparticle is thus of negative energy, and reduces the mass of the black hole. The mechanism applies both to fermions and bosons. From far away this effect looks like the emission of a particle. A detailed investigation showed that the effect is most pronounced for photon emission. In short, Bekenstein and Hawking showed that *black holes radiate as black bodies*.

Black hole radiation confirms both the result on black hole entropy by Bekenstein and the effect for observers accelerated in vacuum found by Fulling, Davies and Unruh. When all this became clear, a beautiful thought experiment was published by William Unruh and Robert Wald, showing that the whole result could have been deduced already 50 years earlier!

pletely converted heat radiation into mechanical energy. Nothing else has changed: the

50 years earlier! Shameful as this delay of the discovery is for the community of theoretical physicists, the story itself remains beautiful. It starts in the early 1970s, when Robert Geroch studied the issue shown in Figure 87. Imagine a mirror box full of heat radiation, thus full of light. The mass of the box is assumed to be negligible, such as a box made of thin aluminium paper. We lower the box, with all its contained radiation, from a space station towards a black hole. On the space station, lowering the weight of the heat radiation allows generating energy. Obviously, when the box reaches the black hole horizon, the heat radiation is red-shifted to infinite wavelength. At that point, the full amount of energy originally contained in the heat radiation has been provided to the space station. We can now do the following: we can open the box on the horizon, let drop out whatever is still inside, and wind the empty and massless box back up again. As a result, we have com-

black hole has the same mass as beforehand.

But the lack of change contradicts the second principle of thermodynamics! Geroch concluded that something must be wrong. We must have forgotten an effect which makes this process impossible.

In the 1980s, William Unruh and Robert Wald showed that black hole radiation is precisely the forgotten effect that puts everything right. Because of black hole radiation, the box feels buoyancy, so that it cannot be lowered down to the horizon completely. The box floats somewhat above the horizon, so that the heat radiation inside the box has not yet *zero* energy when it falls out of the opened box. As a result, the black hole does increase in mass and thus in entropy when the box is opened. In summary, when the empty box is pulled up again, the final situation is thus the following: only part of the energy of the heat radiation has been converted into mechanical energy, part of the energy went into the increase of mass and thus of entropy of the black hole. The second principle of thermodynamics is saved.

Well, the second principle of thermodynamics is only saved if the heat radiation has precisely the right energy density at the horizon and above. Let us have a look. The centre of the box can only be lowered up to a hovering distance *d* above the horizon. At the horizon, the acceleration due to gravity is  $g_{surf} = c^4/4GM$ . The energy *E* gained by lowering the box is

$$E = c^{2}m - mg_{\rm surf}\frac{d}{2} = c^{2}m\left(1 - \frac{dc^{2}}{8GM}\right).$$
 (37)

The efficiency of the process is  $\eta = E/c^2m$ . To be consistent with the second principle of thermodynamics, this efficiency must obey

$$\eta = \frac{E}{c^2 m} = 1 - \frac{T_{\rm BH}}{T} , \qquad (38)$$

where *T* is the temperature of the radiation inside the box. We thus find a black hole temperature  $T_{\rm BH}$  that is determined by the hovering distance *d*. The hovering distance is roughly given by the size of the box. The box size in turn must be at least the wavelength of the thermal radiation; in first approximation, Wien's relation gives  $d \approx \hbar c/kT$ . A precise calculation introduces a factor  $\pi$ , giving the result

$$T_{\rm BH} = \frac{\hbar c^3}{8\pi k GM} = \frac{\hbar c}{4\pi k} \frac{1}{R} = \frac{\hbar}{2\pi k c} g_{\rm surf} \quad \text{with} \quad g_{\rm surf} = \frac{c^4}{4GM} \,, \tag{39}$$

where *R* and *M* are the radius and the mass of the black hole. The quantity  $T_{BH}$  is either called the *black-hole temperature* or the *Bekenstein–Hawking temperature*. As an example, a black hole with the mass of the Sun would have the rather small temperature of 62 nK, whereas a smaller black hole with the mass of a mountain, say  $10^{12}$  kg, would have a temperature of 123 GK. That would make quite a good oven. All known black hole candidates have masses in the range from a few to a few million solar masses. The radiation is thus extremely weak – much too weak to be detectable.

The reason for the weakness of black hole radiation is that the emitted wavelength is of the order of the black hole radius, as you might want to check. The radiation emitted by black holes is often also called *Bekenstein–Hawking radiation*.

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Challenge 104 ny

PRINCIPLE	T h e r m o d y n a m i c s	Horizons		
Zeroth principle	the temperature $T$ is the same across a body at equilibrium	the surface gravity $a$ is the same across the horizon		
First principle	energy is conserved: $dE = TdS - pdV + \mu dN$	energy is con- served: $d(c^2m) = \frac{ac^2}{8\pi G} dA + \Omega dJ + \Phi dq$		
Second principle	entropy never decreases: $dS \ge 0$	surface area never de- creases: $dA \ge 0$ (except for black hole radiation)		
Third principle	T = 0 cannot be achieved	a = 0 cannot be achieved		

TABLE 10 The principles of thermodynamics and those of horizon mechanics.

All thermodynamic principles are valid for black holes, of course. A summary of the meaning of each thermodynamic principle in the case of black holes is given in Table 10. Black hole radiation is thus so weak that we must speak of an academic effect! It leads

to a luminosity that increases with decreasing mass or size as

$$L \sim \frac{1}{M^2} \sim \frac{1}{R^2}$$
 or  $L = nA\sigma T^4 = \frac{n}{15 \cdot 2^{11}\pi} \frac{c^6 \hbar}{G^2 M^2}$  (40)

Vol. III, page 239 where  $\sigma$  is the Stefan–Boltzmann or *black body radiation constant*, *n* is the number of particle degrees of freedom that can be radiated; as long as only photons are radiated – Ref. 130 the only case of practical importance – we have n = 2.

*Black holes thus shine*, and the more the smaller they are. For example, a solar-mass black holes emits less than 0.1 xW. This is a genuine *quantum* effect, since classically, black holes, as the name says, cannot emit any light at all. Even though the effect is academically weak, it will be of importance later on. In actual systems, many other effects around black holes increase the luminosity far above the Bekenstein–Hawking value; indeed, black holes are usually brighter than normal stars, due to the radiation emitted by the matter falling into them. But that is another story. Here we are treating isolated black holes, surrounded only by pure vacuum.

# The lifetime of black holes

Due to the emitted radiation, black holes gradually lose mass. Therefore their theoretical lifetime is *finite*. A calculation shows that the lifetime is given by

$$t = M^3 \frac{20\,480\,\pi\,G^2}{\hbar c^4} \approx M^3\,3.4 \cdot 10^{-16}\,\mathrm{s/kg^3} \tag{41}$$

as function of their initial mass *M*. For example, a black hole with mass of 1 g would have a lifetime of  $3.4 \cdot 10^{-25}$  s, whereas a black hole of the mass of the Sun,  $2.0 \cdot 10^{30}$  kg, would have a lifetime of about  $10^{68}$  years. Again, these numbers are purely academic.

Challenge 105 ny

Challenge 106 ny

The important point is that *black holes evaporate*. However, this extremely slow process for usual black holes determines their lifetime only if no other, faster process comes into play. We will present a few such processes shortly. Bekenstein–Hawking radiation is the weakest of all known effects. It is not masked by stronger effects only if the black hole is non-rotating, electrically neutral and with no matter falling into it from the surroundings.

So far, none of these quantum gravity effects has been confirmed experimentally, as the values are much too small to be detected. However, the deduction of a Hawking tem-

Ref. 131

perature has been beautifully confirmed by a theoretical discovery of William Unruh, who found that there are configurations of fluids in which sound waves cannot escape, so-called *'silent holes'*. Consequently, these silent holes radiate sound waves with a temperature satisfying the same formula as real black holes. A second type of analogue system, namely *optical black holes*, are also being investigated.

Ref. 132

# BLACK HOLES ARE ALL OVER THE PLACE

Around the year 2000, astronomers amassed a large body of evidence that showed something surprising: there seems to be a *supermassive* black hole at the centre of almost all galaxies. The most famous of all is of course the black hole at the centre of our own galaxy. Also quasars, active galactic nuclei and gamma-ray bursters seem to be due to supermassive black holes at the centre of galaxies. The masses of these black holes are typically higher than a million solar masses.

Astronomers also think that many other, smaller astrophysical objects contain black holes: ultraluminous X-ray sources and x-ray binary stars are candidates for black holes of *intermediate* mass.

Finally, one candidate explanation for dark matter on the outskirts of galaxies is a hypothetical cloud of *small* black holes.

In short, black holes seem to be quite common across the universe. Whenever astronomers observe a new class of objects, two questions arise directly: how do the objects form? And how do they disappear? We have seen that quantum mechanics puts an upper limit to the life time of a black hole. The upper limit is academic, but that is not important. The main point is that it exists. Indeed, astronomers think that most black holes disappear in other ways, and much before the Bekenstein–Hawking limit, for example through mergers. All this is still a topic of research. The detectors of gravitational waves might clarify these processes in the future.

Vol. II, page 174

How are black holes born? It turns out that the birth of black holes can actually be observed.

## FASCINATING GAMMA-RAY BURSTS

Nuclear explosions produce flashes of  $\gamma$  rays, or gamma rays. In the 1960s, several countries thought that detecting  $\gamma$  ray flashes, or better, their absence, using satellites, would be the best way to ensure that nobody was detonating nuclear bombs above ground. But when the military sent satellites into the sky to check for such flashes, they discovered something surprising. They observed about two  $\gamma$  flashes *every* day. For fear of being laughed at, the military kept this result secret for many years.

It took the military six years to understand what an astronomer could have told

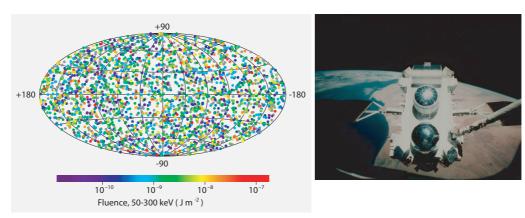


FIGURE 88 The location and energy of the 2704  $\gamma$  ray bursts observed in the sky between 1991 and 2000 by the BATSE experiment on board of the Compton Gamma Ray Observatory, a large satellite deployed by the space shuttle after over 20 years of planning and construction. The Milky Way is located around the horizontal line running from +180 to -180 (NASA).

them in five minutes: the flashes, today called *gamma-ray bursts*, were coming from outer space. Finally, the results were published; this is probably the only discovery about nature that was made by the military. Another satellite, this time built by scientists, the Compton Gamma Ray Observatory, confirmed that the bursts were *extragalactic* in origin, as proven by the map of Figure 88.

Measurements of gamma-ray bursts are done by satellites because most gamma rays do not penetrate the atmosphere. In 1996, the Italian-Dutch BeppoSAX satellite started mapping and measuring gamma-ray bursts systematically. It discovered that they were followed by an *afterglow* in the X-ray domain, lasting many hours, sometimes even days. In 1997, afterglow was discovered also in the optical domain. The satellite also allowed researchers to find the corresponding X-ray, optical and radio sources for each burst. These measurements in turn allowed determining the distance of the burst sources; red-shifts between 0.0085 and 4.5 were measured. In 1999 it finally became possible to detect the *optical* bursts corresponding to gamma-ray bursts.\*

All this data together showed that gamma-ray bursts have durations between milliseconds and about an hour. Gamma-ray bursts seem to fall into (at least) two classes: the *short bursts*, usually below 3 s in duration and emitted from closer sources, and the *long bursts*, emitted from distant galaxies, typically with a duration of 30 s and more, and with a softer energy spectrum. The long bursts produce luminosities estimated to be up to  $10^{45}$  W. This is about one hundredth of the brightness all stars of the whole visible universe taken together! Put differently, it is the same amount of energy that is released when converting several solar masses into radiation within a few seconds.

In fact, the measured luminosity of long bursts is near the theoretical maximum luminosity a body can have. This limit is given by

$$L < L_{\rm Pl} = \frac{c^5}{4G} = 0.9 \cdot 10^{52} \,\mathrm{W}$$
, (42)

Challenge 107 s

Ref. 137

Ref. 135

Vol. II, page 108

<sup>\*</sup> For more detail about this fascinating topic, see the www.aip.de/~jcg/grb.html website by Jochen Greiner.

Challenge 108 e

as you might want to check yourself. In short, the sources of gamma ray bursts are the biggest bombs found in the universe. The are explosions of almost unimaginable proportions. Recent research seems to suggest that long gamma-ray bursts are not isotropic, but that they are *beamed*, so that the huge luminosity values just mentioned might need to be divided by a factor of 1000.

Ref. 135

However, the mechanism that leads to the emission of gamma rays is still unclear. It is often speculated that short bursts are due to merging neutron stars, whereas long bursts are emitted when a black hole is formed in a supernova or hypernova explosion. In this case, long gamma-ray bursts would be 'primal screams' of black holes *in formation*. However, a competing explanation states that long gamma-ray bursts are due to the *death* of black holes.

Ref. 133

Indeed, already 1975, a powerful radiation emission mechanism was predicted for dying *charged* black holes by Damour and Ruffini. Charged black holes have a much shorter lifetime than neutral black holes, because during their formation a second process takes place. In a region surrounding them, the electric field is larger than the so-called vacuum polarization value, so that large numbers of electron-positron pairs are produced, which then almost all annihilate. This process effectively reduces the charge of the black hole to a value for which the field is below critical everywhere, while emitting large amounts of high energy light. It turns out that the mass is reduced by up to 30 % in a time of the order of seconds. That is quite shorter than the 10<sup>68</sup> years predicted by Bekenstein–Hawking radiation! This process thus produces an extremely intense gamma-ray burst.

Ruffini took up his 1975 model again in 1997 and with his collaborators showed that the gamma-ray bursts generated by the annihilation of electron-positrons pairs created by vacuum polarization, in the region they called the *dyadosphere*, have a luminosity and a duration exactly as measured, if a black hole of about a few up to 30 solar masses is assumed. Charged black holes therefore reduce their charge and mass through the vacuum polarization and electron positron pair creation process. (The process reduces the mass because it is one of the few processes which is *reversible*; in contrast, most other attempts to reduce charge on a black hole, e.g. by throwing in a particle with the opposite charge, increase the mass of the black hole and are thus irreversible.) The left over remnant then can lose energy in various ways and also turns out to be responsible for the afterglow discovered by the BeppoSAX satellite. Among others, Ruffini's team speculates that the remnants are the sources for the high energy cosmic rays, whose origin had not been localized so far. All these exciting studies are still ongoing.

Ref. 136

Vol. II, page 271

Understanding long gamma-ray bursts is one of the most fascinating open questions in astrophysics. The relation to black holes is generally accepted. But many processes leading to emission of radiation from black holes are possible. Examples are matter falling into the black hole and heating up, or matter being ejected from rotating black holes through the Penrose process, or charged particles falling into a black hole. These mechanisms are known; they are at the origin of *quasars*, the extremely bright quasi-stellar sources found all over the sky. They are assumed to be black holes surrounded by matter, in the development stage following gamma-ray bursters. But even the details of what happens in quasars, the enormous voltages (up to  $10^{20}$  V) and magnetic fields generated, as well as their effects on the surrounding matter are still object of intense research in astrophysics.

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#### MATERIAL PROPERTIES OF BLACK HOLES

Once the concept of entropy of a black hole was established, people started to think about black holes like about any other material object. For example, black holes have a matter density, which can be defined by relating their mass to a fictitious volume defined by  $4\pi R^3/3$ , where *R* is their radius. This density is then given by

$$\rho = \frac{1}{M^2} \frac{3c^6}{32\pi G^3}$$
(43)

and can be quite low for large black holes. For the largest black holes known, with 1000 million solar masses or more, the density is of the order of the density of air. Nevertheless, even in this case, the density is the highest possible in nature for that mass.

By the way, the gravitational acceleration at the horizon is still appreciable, as it is given by

$$g_{\rm surf} = \frac{1}{M} \frac{c^4}{4G} = \frac{c^2}{2R}$$
 (44)

Challenge 110 e which is still  $15 \text{ km/s}^2$  for an air density black hole.

Challenge 109 e

Challenge 111 e

Challenge 112 ny

Challenge 113 s

Ref. 138

Obviously, the black hole temperature is related to the entropy S by its usual definition

$$\frac{1}{T} = \left. \frac{\partial S}{\partial E} \right|_{\rho} = \left. \frac{\partial S}{\partial (c^2 M)} \right|_{\rho} \tag{45}$$

All other thermal properties can be deduced by the standard relations from thermostatics.

In particular, black holes are the systems in nature with the largest possible entropy. Can you confirm this statement?

It also turns out that black holes have a *negative* heat capacity: when heat is added, they cool down. In other words, black holes cannot achieve equilibrium with a bath. This is not a real surprise, since *any* gravitationally bound material system has negative specific heat. Indeed, it takes only a bit of thinking to see that any gas or matter system collapsing under gravity follows dE/dR > 0 and dS/dR > 0. That means that while collapsing, the energy and the entropy of the system shrink. (Can you find out where they go?) Since temperature is defined as 1/T = dS/dE, temperature is always positive; from the temperature increase dT/dR < 0 during collapse one deduces that the specific heat dE/dT is negative.

Black holes, like any object, oscillate when slightly perturbed. These vibrations have Ref. 139 also been studied; their frequency is proportional to the mass of the black hole.

Nonrotating black holes have no magnetic field, as was established already in the 1960s Ref. 130 by Russian physicists. On the other hand, black holes have something akin to a finite electrical conductivity and a finite viscosity. Some of these properties can be understood if

Ref. 140 the horizon is described as a membrane, even though this model is not always applicable. In any case, we can study and describe isolated macroscopic black holes like any other macroscopic material body. The topic is not closed.

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## How do black holes evaporate?

When a nonrotating and uncharged black hole loses mass by radiating Hawking radiation, eventually its mass reaches values approaching the Planck mass, namely a few micrograms. Expression (41) for the lifetime, applied to a black hole of Planck mass, yields a value of over sixty thousand Planck times. A surprising large value. What happens in those last instants of evaporation?

A black hole approaching the Planck mass at some time will get smaller than its own Compton wavelength; that means that it behaves like an elementary particle, and in particular, that quantum effects have to be taken into account. It is still unknown how these final evaporation steps take place, whether the mass continues to diminish smoothly or in steps (e.g. with mass values decreasing as  $\sqrt{n}$  when *n* approaches zero), how its internal structure changes, whether a stationary black hole starts to rotate (as the author predicts), or how the emitted radiation deviates from black body radiation. There is still enough to study. However, one important issue *has* been settled.

## The information paradox of black holes

When the thermal radiation of black holes was discovered, one question was hotly debated for many years. The matter forming a black hole can contain lots of information; e.g., we can imagine the black hole being formed by a large number of books collapsing onto each other. On the other hand, a black hole radiates thermally until it evaporates. Since thermal radiation carries no information, it seems that information somehow disappears, or equivalently, that entropy increases.

An incredible number of papers have been written about this problem, some even claiming that this example shows that physics as we know it is incorrect and needs to be changed. As usual, to settle the issue, we need to look at it with precision, laying all prejudice aside. Three intermediate questions can help us finding the answer.

- What happens when a book is thrown into the Sun? When and how is the information radiated away?
- How precise is the sentence that black hole radiate *thermal* radiation? Could there be a slight deviation?
- Could the deviation be measured? In what way would black holes radiate information?

Challenge 114 e You might want to make up your own mind before reading on.

Let us walk through a short summary. When a book or any other highly complex – or low entropy – object is thrown into the Sun, the information contained is radiated away. The information is contained in some slight deviations from black hole radiation, namely in slight correlations between the emitted radiation emitted over the burning time of the Sun. A short calculation, comparing the entropy of a room temperature book and the information contained in it, shows that these effects are extremely small and difficult to measure.

Ref. 141

A clear exposition of the topic was given by Don Page. He calculated what information would be measured in the radiation if the system of black hole and radiation *together* would be in a *pure* state, i.e., a state containing specific information. The result is simple. Even if a system is large – consisting of many degrees of freedom – and in pure state, any smaller *subsystem* nevertheless looks almost perfectly thermal. More specifically, if

a total system has a Hilbert space dimension N = nm, where *n* and  $m \le n$  are the dimensions of two subsystems, and if the total system is in a pure state, the subsystem *m* would have an entropy  $S_m$  given by

Challenge 115 ny

$$S_m = \frac{1-m}{2n} + \sum_{k=n+1}^{mn} \frac{1}{k}$$
(46)

which is approximately given by

$$S_m = \ln m - \frac{m}{2n} \quad \text{for} \quad m \gg 1 . \tag{47}$$

To discuss the result, let us think of n and m as counting degrees of freedom, instead of Hilbert space dimensions. The first term in equation (47) is the usual entropy of a mixed state. The second term is a small deviation and describes the amount of specific information contained in the original pure state; inserting numbers, one finds that it is extremely small compared to the first. In other words, the subsystem m is almost indistinguishable from a mixed state; it looks like a thermal system even though it is not.

A calculation shows that the second, small term on the right of equation (47) is indeed sufficient to radiate away, during the lifetime of the black hole, any information contained in it. Page then goes on to show that the second term is so small that not only it is lost in measurements; it is also lost in the usual, perturbative calculations for physical systems.

The question whether any radiated information could be measured can now be answered directly. As Don Page showed, even measuring half of the system only gives about one half of a bit of the radiated information. It is thus necessary to measure almost the *complete* radiation to obtain a sizeable chunk of the radiated information. In other words, it is extremely hard to determine the information contained in black hole radiation.

In summary, at any given instant, the amount of information radiated by a black hole is negligible when compared with the total black hole radiation; it is practically impossible to obtain valuable information through measurements or even through calculations that use usual approximations.

#### More paradoxes

A black hole is a macroscopic object, similar to a star. Like all objects, it can interact with its environment. It has the special property to swallow everything that falls into them. This immediately leads us to ask if we can use this property to cheat around the usual everyday 'laws' of nature. Some attempts have been studied in the section on general relativity and above; here we explore a few additional ones.

Vol. II, page 275

Challenge 116 ny

\* \*

Apart from the questions of entropy, we can look for methods to cheat around conservation of energy, angular momentum, or charge. But every thought experiment comes to the same conclusions. No cheats are possible. Every reasoning confirms that the maximum number of degrees of freedom in a region is proportional to the surface area of

the region, and *not* to its volume. This intriguing result will keep us busy for quite some time.

\* \*

A black hole transforms matter into antimatter with a certain efficiency. Indeed, a black hole formed by collapsing matter also radiates antimatter. Thus one might look for departures from particle number conservation. Are you able to find an example?

\* \*

Black holes deflect light. Is the effect polarization dependent? Gravity itself makes no difference of polarization; however, if virtual particle effects of QED are included, the story might change. First calculations seem to show that such an effect exists, so that gravitation might produce rainbows. Stay tuned.

If lightweight boxes made of mirrors can float in radiation, one might deduce a strange consequence: such a box could self-accelerate in free space. In a sense, an accelerated box could float on the Fulling–Davies–Unruh radiation it creates by its own acceleration. Are you able to show the that this situation is impossible because of a small but significant difference between gravity and acceleration, namely the absence of tidal effects? (Other reasons, such as the lack of perfect mirrors, also make the effect impossible.)

\* \*

Ref. 144

Challenge 118 ny

Challenge 117 nv

Ref 143

In 2003, Michael Kuchiev has made the spectacular prediction that matter and radiation with a wavelength *larger* than the diameter of a black hole is partly reflected when it hits a black hole. The longer the wavelength, the more efficient the reflection would be. For stellar or even larger black holes, he predicts that only photons or gravitons are reflected. Black holes would thus not be complete trash cans. Is the effect real? The discussion is still ongoing.

## QUANTUM MECHANICS OF GRAVITATION

Let us take a conceptual step at this stage. So far, we looked at quantum theory *with* gravitation; now we have a glimpse at quantum theory *of* gravitation.

If we bring to our mind the similarity between the electromagnetic field and the gravitational 'field,' our next step should be to find the quantum description of the gravitational field. However, despite attempts by many brilliant minds for almost a century, this search was not successful. Indeed, modern searches take another direction, as will be explained in the last part of our adventure. But let us see what was achieved and why the results are not sufficient.

# DO GRAVITONS EXIST?

Quantum theory says that everything that moves is made of particles. What kind of particles are gravitational waves made of? If the gravitational field is to be treated quantum mechanically like the electromagnetic field, its waves should be quantized. Most properties of these quanta of gravitation can be derived in a straightforward way.

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The  $1/r^2$  dependence of universal gravity, like that of electricity, implies that the quanta of the gravitational field have *vanishing* mass and move at light speed. The independence of gravity from electromagnetic effects implies a *vanishing* electric charge.

We observe that gravity is always attractive and never repulsive. This means that the field quanta have *integer* and *even* spin. Vanishing spin is ruled out, since it implies no coupling to energy. To comply with the property that 'all energy has gravity', spin S = 2 is needed. In fact, it can be shown that *only* the exchange of a massless spin 2 particle leads, in the classical limit, to general relativity.

The coupling strength of gravity, corresponding to the fine structure constant of electromagnetism, is given either by

$$\alpha_{G1} = \frac{G}{\hbar c} = 2.2 \cdot 10^{-15} \text{ kg}^{-2} \quad \text{or by} \quad \alpha_{G2} = \frac{Gmm}{\hbar c} = \left(\frac{m}{m_{Pl}}\right)^2 = \left(\frac{E}{E_{Pl}}\right)^2 .$$
(48)

However, the first expression is not a pure number; the second expression is, but depends on the mass we insert. These difficulties reflect the fact that gravity is not properly speaking an interaction, as became clear in the section on general relativity. It is often argued that *m* should be taken as the value corresponding to the energy of the system in question. For everyday life, typical energies are 1 eV, leading to a value  $\alpha_{G2} \approx 1/10^{56}$ . Gravity is indeed weak compared to electromagnetism, for which  $\alpha_{em} = 1/137.036$ .

If all this is correct, *virtual* field quanta would also have to exist, to explain static gravitational fields. However, up to this day, the so-called *graviton* has not yet been detected, and there is in fact little hope that it ever will. On the experimental side, nobody knows yet how to build a graviton detector. Just try! On the theoretical side, the problems with the coupling constant probably make it impossible to construct a *renormalizable* theory of gravity; the lack of renormalization means the impossibility to define a perturbation expansion, and thus to define particles, including the graviton. It might thus be that relations such as  $E = \hbar \omega$  or  $p = \hbar/2\pi\lambda$  are not applicable to gravitational waves. In short, it may be that the particle concept has to be changed before applying quantum theory to gravity. The issue is still open at this point.

# Space-time foam

The indeterminacy relation for momentum and position also applies to the gravitational field. As a result, it leads to an expression for the indeterminacy of the metric tensor g in a region of size l, which is given by

$$\Delta g \approx 2 \frac{l_{\rm Pl}^2}{l^2} , \qquad (49)$$

Challenge 120 ny

where  $l_{\text{Pl}} = \sqrt{\hbar G/c^3}$  is the Planck length. Can you deduce the result? Quantum theory thus shows that like the momentum or the position of a particle, also the metric tensor *g* is a *fuzzy* observable.

But that is not all. Quantum theory is based on the principle that actions below  $\hbar$  cannot be observed. This implies that the observable values for the metric g in a region

Ref. 149

# Challenge 119 s

of size *L* are bound by

$$g \ge \frac{2\hbar G}{c^3} \frac{1}{L^2} \,. \tag{50}$$

Can you confirm this? The result has far-reaching consequences. A minimum value for the metric depending inversely on the region size implies that it is impossible to say what happens to the shape of space-time at extremely small dimensions. In other words, at extremely high energies, the concept of space-time itself becomes fuzzy. John Wheeler introduced the term *space-time foam* to describe this situation. The term makes clear that space-time is not continuous nor a manifold in those domains. But this was the basis on which we built our description of nature so far! We are forced to deduce that our description of nature is built on sand. This issue will be essential in the last volume of our mountain ascent.

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# DECOHERENCE OF SPACE-TIME

General relativity taught us that the gravitational field and space-time are the same. If the gravitational field evolves like a quantum system, we may ask why no superpositions of different macroscopic space-times are observed.

Ref. 150

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Challenge 121 ny

Challenge 122 e

The discussion is simplified for the simplest case of all, namely the superposition, in a vacuum region of size l, of a homogeneous gravitational field with value g and one with value g'. As in the case of a superposition of macroscopic distinct wave functions, such a superposition *decays*. In particular, it decays when particles cross the volume. A short calculation yields a decay time given by

$$t_{\rm d} = \left(\frac{2kT}{\pi m}\right)^{3/2} \frac{nl^4}{(g-g')^2} , \qquad (51)$$

where n is the particle number density, kT their kinetic energy and m their mass. Inserting typical numbers, we find that the variations in gravitational field strength are *extremely* small. In fact, the numbers are so small that we can deduce that the gravitational field is the *first* variable which behaves classically in the history of the universe. Quantum gravity effects for space-time will thus be extremely hard to detect.

In short, matter not only tells space-time how to curve, it also tells it to behave with class.

#### QUANTUM THEORY AS THE ENEMY OF SCIENCE FICTION

How does quantum theory change our ideas of space-time? The end of the twentieth century has brought several unexpected but strong results in semiclassical quantum gravity.

Ref. 151

In 1995 Ford and Roman found that *worm holes*, which are imaginable in general relativity, cannot exist if quantum effects are taken into account. They showed that macroscopic worm holes require unrealistically large negative energies. (For microscopic worm holes the issue is still unclear.)

Ref. 152

In 1996 Kay, Radzikowski and Wald showed that *closed time-like curves* do not exist in semiclassical quantum gravity; there are thus no time machines in nature.

Ref. 153

In 1997 Pfenning and Ford showed that warp drive situations, which are also imagin-

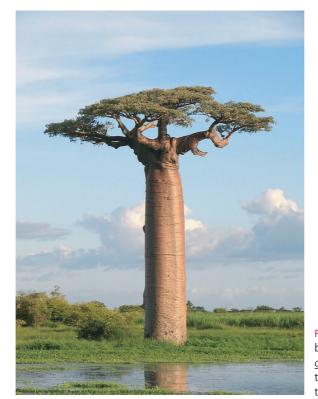


FIGURE 89 Every tree, such as this beautiful Madagascar baobab (*Adansonia grandidieri*), shows that nature, in contrast to physicists, is able to combine quantum theory and gravity (© Bernard Gagnon).

able in general relativity, cannot exist if quantum effects are taken into account. Such situations require unrealistically large negative energies.

In short, the inclusion of quantum effects destroys all those fantasies which were started by general relativity.

# NO VACUUM MEANS NO PARTICLES

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Gravity has an important consequence for quantum theory. To count and define particles, quantum theory needs a defined vacuum state. However, the vacuum state cannot be defined when the curvature radius of space-time, instead of being larger than the Compton wavelength, becomes comparable to it. In such highly curved space-times, particles cannot be defined. The reason is the impossibility to distinguish the environment from the particle in these situations: in the presence of strong curvatures, the vacuum is full of spontaneously generated matter, as black holes show. Now we just saw that at small dimensions, space-time fluctuates wildly; in other words, space-time is highly curved at small dimensions or high energies. In other words, strictly speaking particles cannot be defined; the particle concept is only a low energy approximation! We will explore this strange conclusion in more detail in the final part of our mountain ascent.

# Summary on quantum theory and gravity

Every tree tells us: everyday, *weak* gravitational fields can be included in quantum theory. *Weak* gravitational fields have measurable and predictable effects on wave functions: quantum particles fall and their phases change in gravitational fields. Conversely, the inclusion of quantum effects into general relativity leads to space-time foam, space-time superpositions and gravitons. The inclusion of quantum effects into gravity prevents the existence of wormholes, time-like curves and negative energy regions.

The inclusion of *strong* gravitational fields into quantum theory works for practical situations but leads to problems with the particle concept. Conversely, the inclusion of quantum effects into situations with high space-time curvature leads to problems with the concept of space-time.

In summary, the combination of quantum theory and gravitation leads to problems with both the particle concept and the space-time concept. The combination of quantum theory and general relativity puts into question the foundations of the description of nature that we used so far. As shown in Figure 89, nature is smarter than we are.

In fact, up to now we hid a simple fact: conceptually, quantum theory and general relativity *contradict* each other. This contradiction was one of the reasons that we stepped back to special relativity before we started exploring quantum theory. By stepping back we avoided many problems, because quantum theory does not contradict *special* relativity, but only *general* relativity. The issues are dramatic, changing everything from the basis of classical physics to the results of quantum theory. There will be surprising consequences for the nature of space-time, for the nature of particles, and for motion itself. Before we study these issues, however, we complete the theme of the present, quantum part of the mountain ascent, namely exploring motion inside matter, and in particular the motion of and in nuclei.

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# CHAPTER 5 THE STRUCTURE OF THE NUCLEUS - THE DENSEST CLOUDS

V uclear physics was born in 1896 in France, but is now a small activity. ot many open issues are left. But in its golden past, researchers produced ew ways for medical doctors to dramatically improve the healing rate of patients. Researchers also discovered why stars shine, how powerful bombs work, and how cosmic evolution produced the atoms we are made of. We will explore these topics now. A fascinating spin-off of nuclear physics, high energy particle physics, will keep us busy later on.

Nuclear physics is just low-density astrophysics. Anonymous

# A PHYSICAL WONDER - MAGNETIC RESONANCE IMAGING

Arguably, the most spectacular tool that physical research produced in the twentieth century was *magnetic resonance imaging*, or MRI for short. This imaging technique allows one to image the interior of human bodies with a high resolution and with no damage or danger to the patient, in strong contrast to X-ray imaging. The technique is based on moving atomic nuclei. Though the machines are still expensive – costing up to several million euro – there is hope that they will become cheaper in the future. Such an MRI machine, shown in Figure 90, consists essentially of a large magnetic coil, a radio transmitter and a computer. Some results of putting part of a person into the coil are shown in Figure 91. The images allow detecting problems in bones, in the spine, in the beating heart and in general tissue. Many people owe their life and health to these machines; in many cases the machines allow making precise diagnoses and thus choosing the appropriate treatment for patients.

In MRI machines, a radio transmitter emits radio waves that are absorbed because hydrogen nuclei – protons – are small spinning magnets. The magnets can be parallel or antiparallel to the magnetic field produced by the coil. The transition energy E is absorbed from a radio wave whose frequency  $\omega$  is tuned to the magnetic field B. The energy absorbed by a single hydrogen nucleus is given by

$$E = \hbar\omega = \hbar\gamma B \tag{52}$$

The material constant  $\gamma/2\pi$  has a value of 42.6 MHz/T for hydrogen nuclei; it results from the non-vanishing spin of the proton. The absorption of the radio wave is a pure quantum effect, as shown by the appearance of the quantum of action  $\hbar$ . Using some cleverly ap-

#### 5 THE STRUCTURE OF THE NUCLEUS



FIGURE 90 A commercial MRI machine (© Royal Philips Electronics).

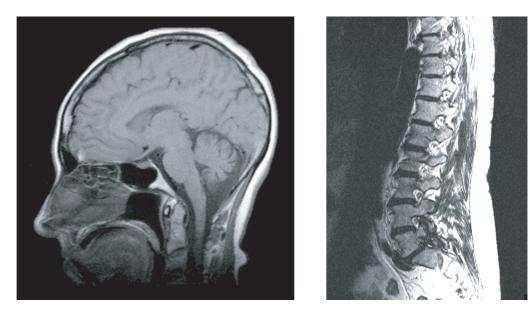


FIGURE 91 Sagittal images of the head and the spine (used with permission from Joseph P. Hornak, *The Basics of MRI*, www.cis.rit.edu/htbooks/mri, Copyright 2003).

plied magnetic fields, typically with a strength between 0.3 and 7 T for commercial and up to 21 T for experimental machines, the absorption for each volume element can be measured separately. Interestingly, the precise absorption *level* depends on the chemical compound the nucleus is built into. Thus the absorption value will depend on the chemical substance. When the intensity of the absorption is plotted as grey scale, an image is formed that retraces the different chemical compositions. Figure 91 shows two examples. Using additional tricks, modern machines can picture blood flow in the heart or air flow

#### **5 THE DENSEST CLOUDS**

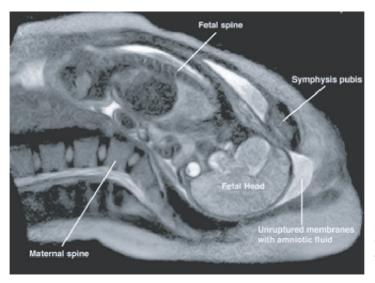


FIGURE 92 An image of the first magnetic resonance video of a human birth (© C. Bamberg).

- Ref. 155 in lungs; they now routinely make films of the heart beat. Other techniques show how the location of sugar metabolism in the brain depends on what you are thinking about.\* Magnetic resonance imaging can even image the great wonders of nature. The first
   Ref. 156 video of a human birth, taken in 2010 and published in 2012, is shown in Figure 92. MRI scans are loud, but otherwise harmless for unborn children. The first scan of a married
   Ref. 157 couple making love has been taken by Willibrord Weijmar Schultz and his group in 1999. It is shown on page 400. Every magnetic resonance image thus proves that
  - ▷ Many but not all atoms have nuclei that spin.

Like any other object, nuclei have size, shape, colour, composition and interactions. Let us explore them.

# The size of nuclei and the discovery of radioactivity

The magnetic resonance signal shows that hydrogen nuclei spin with high speed. Thus they must be small. Indeed, the *g*-factor of protons, defined using the magnetic moment  $\mu$ , their mass *m* and charge *e*, is found to be

$$g = \mu 4 \frac{m}{e\hbar} \approx 5.6 . \tag{53}$$

Vol. IV, page 107 This is a small value. Using the expression that relates the g-factor and the radius of a composite object, we deduce that the radius of the proton is about 0.9 fm; this value

<sup>\*</sup> The website www.cis.rit.edu/htbooks/mri by Joseph P. Hornak gives an excellent introduction to magnetic resonance imaging, both in English and Russian, including the physical basis, the working of the machines, and numerous beautiful pictures. The method of studying nuclei by putting them at the same time into magnetic and radio fields is also called *nuclear magnetic resonance*.

#### **5 THE STRUCTURE OF THE NUCLEUS**



FIGURE 93 Henri Becquerel (1852–1908)



FIGURE 94 Marie Curie (1867–1934)

is confirmed by many experiments and other measurement methods. Protons are thus about 30 000 times smaller than hydrogen atoms, whose radius is about 30 pm. The proton is the smallest of all nuclei; the largest known nuclei have radii about 7 times as large.

The small size of nuclei is no news. It is known since the beginning of the twentieth century. The story starts on the first of March in 1896, when Henri Becquerel\* discovered a puzzling phenomenon: minerals of uranium potassium sulphate blacken photographic plates. Becquerel had heard that the material is strongly fluorescent; he conjectured that fluorescence might have some connection to the X-rays discovered by Conrad Röntgen the year before. His conjecture was wrong; nevertheless it led him to an important new discovery. Investigating the reason for the effect of uranium on photographic plates, Becquerel found that these minerals emit an undiscovered type of radiation, different from anything known at that time; in addition, the radiation is emitted by any substance containing uranium. In 1898, Gustave Bémont named the property of these minerals *radioactivity*.

Radioactive rays are also emitted from many elements other than uranium. This radiation can be 'seen': it can be detected by the tiny flashes of light that appear when the rays hit a scintillation screen. The light flashes are tiny even at a distance of several metres from the source; thus the rays must be emitted from point-like sources. In short, radio-

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<sup>\*</sup> Henri Becquerel (b. 1852 Paris, d. 1908 Le Croisic), important physicist; his primary research topic was the study of radioactivity. He was the thesis adviser of Marie Curie, the wife of Pierre Curie, and was central to bringing her to fame. The SI unit for radioactivity is named after Becquerel. For his discovery of radioactivity he received the 1903 Nobel Prize in Physics; he shared it with the Curies.

#### 5 THE DENSEST CLOUDS

Түре	Part -	EXAMPLE	R a n g e	Dan-	Shield	U s e
α rays 3 to 10 MeV	I C L E helium nuclei	<sup>235</sup> U, <sup>238</sup> U, <sup>238</sup> Pu, <sup>238</sup> Pu, <sup>241</sup> Am	a few cm in air	G E R when eaten, inhaled, touched	any material, e.g. paper	thickness measurement
<b>β rays</b> 0 to 5 MeV	electrons and antineu- trinos	<sup>14</sup> C, <sup>40</sup> K, <sup>3</sup> H, <sup>101</sup> Tc	< 1 mm in metal light years	serious none	metals none	cancer treatment research
$oldsymbol{eta}^+$ rays	positrons and neutrinos	<sup>40</sup> K, <sup>11</sup> C, <sup>11</sup> C, <sup>13</sup> N, <sup>15</sup> O	less than β light years	medium none	any material none	tomography research
γ rays	high energy photons	<sup>110</sup> Ag	several m in air			preservation of herbs, disinfection
n reactions c. 1 MeV	neutrons	<sup>252</sup> Cf, Po-Li (α,n), <sup>38</sup> Cl-Be (γ,n)	many m in air	high	0.3 m of paraffin	nuclear power, quantum gravity experiments
n emission typ. 40 MeV	neutrons	<sup>9</sup> He, <sup>24</sup> N, <sup>254</sup> Cf	many m in air	high	0.3 m of paraffin	research experiments
<b>p emission</b> typ. 20 MeV	protons	<sup>5</sup> Be, <sup>161</sup> Re	like a rays	small	solids	
spontaneous fission typ. 100 MeV	nuclei	<sup>232</sup> Cm, <sup>263</sup> Rf	like a rays	small	solids	detection of new elements

TABLE 11 The main types of radioactivity and rays emitted by matter.

activity has to be emitted from single atoms. Thus radioactivity confirmed unambiguously that atoms do exist. In fact, radioactivity even allows *counting* atoms: in a diluted radioactive substance, the flashes can be counted, either with the help of a photographic film or with a photon counting system.

The intensity of radioactivity cannot be influenced by magnetic or electric fields; and it does not depend on temperature or light irradiation. In short, radioactivity does not depend on electromagnetism and is not related to it. Also the high energy of the emitted radiation cannot be explained by electromagnetic effects. Radioactivity must thus be due to another, new type of force. In fact, it took 30 years and a dozen of Nobel Prizes to fully understand the details. It turns out that several types of radioactivity exist; the types of emitted radiation behave differently when they fly through a magnetic field or when they encounter matter. The types of radiation are listed in Table 11. In the meantime, all

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ion Mountain – The Adventure of Physics 🛛 copyright © Christoph Schiller June 1990–May 2020 🛛 free pdf file available at www.motionmounta

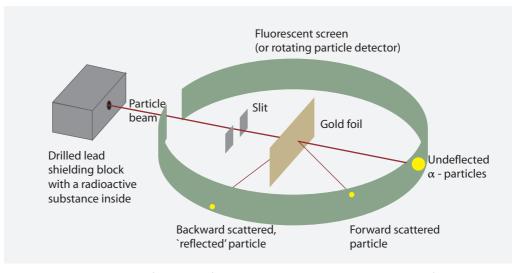


FIGURE 95 The schematics of the Rutherford–Geiger scattering experiment. The gold foil is about a square centimetre in size.

these rays have been studied in great detail, with the aim to understand the nature of the emitted entity and its interaction with matter.

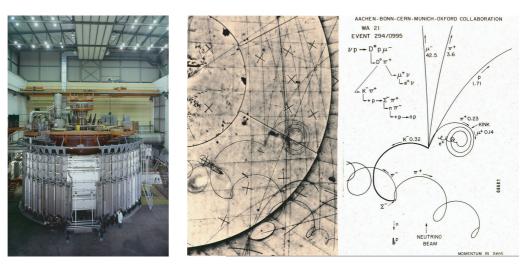
In 1909, radioactivity inspired the 37 year old physicist Ernest Rutherford,\* who had won the Nobel Prize just the year before, to another of his smart experiments. He asked his collaborator Hans Geiger to take an emitter of  $\alpha$  radiation – a type of radioactivity which Rutherford had identified and named 10 years earlier – and to point the radiation at a thin metal foil. The quest was to find out where the  $\alpha$  rays would end up. The experiment is shown in Figure 95. The research group followed the path of the particles by using scintillation screens; later on they used an invention by Charles Wilson: the cloud chamber. A *cloud chamber*, like its successor, the bubble chamber, produces white traces along the path of charged particles; the mechanism is the same as the one than leads to the white lines in the sky when an aeroplane flies by. Both cloud chambers and bubble chambers thus allow *seeing* radioactivity, as shown in the examples of Figure 96.

The radiation detectors around the thin gold foil give a consistent, but strange result: most a particles pass through the foil undisturbed, whereas a few are scattered and a few are reflected. In addition, those few which are reflected are not reflected by the surface, but in the inside of the foil. (Can you imagine how to show this?) Rutherford and Geiger deduced from their scattering experiment that first of all, the atoms in the metal foil are mainly transparent. Only transparency of atoms explains why most a particles pass the

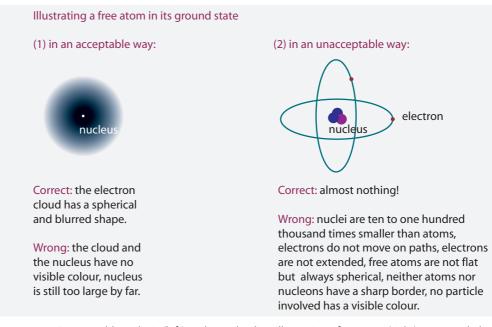
Challenge 123 s

<sup>\*</sup> Ernest Rutherford (b. 1871 Brightwater, d. 1937 Cambridge), important physicist. He emigrated to Britain and became professor at the University of Manchester. He coined the terms  $\alpha$  particle,  $\beta$  particle, proton and neutron. A gifted experimentalist, he discovered that radioactivity transmutes the elements, explained the nature of  $\alpha$  rays, discovered the nucleus, measured its size and performed the first nuclear reactions. Ironically, in 1908 he received the Nobel Prize in Chemistry, much to the amusement of himself and of the world-wide physics community; this was necessary as it was impossible to give enough physics prizes to the numerous discoverers of the time. He founded a successful research school of nuclear physics and many famous physicists spent some time at his institute. Ever an experimentalist, Rutherford deeply disliked quantum theory, even though it was and is the only possible explanation for his discoveries.

#### **5 THE DENSEST CLOUDS**



**FIGURE 96** The 'Big European Bubble Chamber' – the biggest bubble chamber ever built – and an example of tracks of relativistic particles it produced, with the momentum values deduced from the photograph (© CERN).



**FIGURE 97** A reasonably realistic (left) and a misleading illustration of an atom (right) as is regularly found in school books. *Atoms in the ground state are spherical electron clouds with a tiny nucleus, itself a cloud, at its centre.* Interacting atoms, chemically bound atoms and some, but not all excited atoms have electron clouds of different shapes.

foil without disturbance, even though it was over 2000 atoms thick. But some particles were scattered by large angles or even reflected. Rutherford showed that the reflections must be due to a single scattering point. By counting the particles that were reflected (about 1 in 20000 for his  $0.4 \,\mu\text{m}$  gold foil), Rutherford was also able to deduce the *size* 

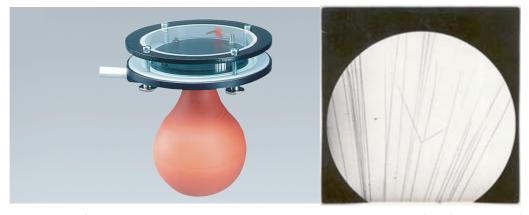


FIGURE 98 Left: a modern Wilson cloud chamber, diameter c. 100 mm. Right: one of the first pictures of α rays taken with a cloud chamber in the 1920s by Patrick Blackett, showing also a collision with an atom in the chamber (© Wiemann Lehrmittel, Royal Society)

of the reflecting entity and to estimate its *mass*. (This calculation is now a standard exercise in the study of physics at universities.) He found that the reflecting entity contains practically all of the mass of the atom in a diameter of a few fm. Rutherford named this concentrated mass the atomic *nucleus*.

Using the knowledge that atoms contain electrons, Rutherford then deduced from this experiment that atoms consist of an electron cloud that determines the size of atoms – of the order of 0.1 nm – and of a tiny but heavy nucleus at the centre. If an atom had the size of a basketball, its nucleus would have the size of a dust particle, yet contain 99.9 % of the basketball's mass. Thus

▷ Atoms resemble candy floss around a heavy dust particle.

Even though the candy floss – the electron cloud – around the nucleus is extremely thin and light, it is strong enough to avoid that two atoms interpenetrate. In solids, the candy floss, i.e., the electron cloud, keeps the neighbouring nuclei at constant distance. Figure 97 shows the more and less correct ways to picture an atom. Candy floss explains the Rutherford–Geiger experiment: for the tiny and massive  $\alpha$  particles however, the candy floss is essentially empty space, so that they simply fly through the electron clouds until they either exit on the other side of the foil or hit a nucleus.

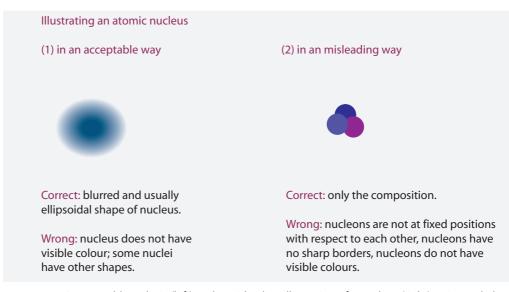
The density of the nucleus is impressive: about  $5.5 \cdot 10^{17} \text{ kg/m}^3$ . At that density, the mass of the Earth would fit in a sphere of 137 m radius and a grain of sand would have a mass larger than the largest oil tanker. (Can you confirm this?)

**C** I now know how an atom looks like! Ernest Rutherford

# NUCLEI ARE COMPOSED

Challenge 124 e

Magnetic resonance images also show that nuclei are *composed*. Indeed, images can also be taken using heavier nuclei instead of hydrogen, such as certain fluorine or oxygen



**FIGURE 99** A reasonably realistic (left) and a misleading illustration of a nucleus (right) as is regularly found in school books. *Nuclei are spherical nucleon clouds*.

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nuclei. Also the *g*-factors of these nuclei depart from the value 2 characteristic of point particles; the more massive the nuclei are, the bigger the departure. Therefore, all nuclei have a finite size. The size of nuclei can actually be measured; the Rutherford–Geiger experiment and many other scattering experiments allow to do so. The measured values confirm the values predicted by the *g*-factor. In short, both the values of the *g*-factor and the non-vanishing sizes show that *nuclei are composed*.

Interestingly, the idea that nuclei are composed is older than the concept of nucleus itself. Already in 1815, after the first mass measurements of atoms by John Dalton and others, researchers noted that the mass of the various chemical elements seem to be almost perfect multiples of the weight of the hydrogen atom. William Prout then formulated the hypothesis that all elements are composed of hydrogen. When the nucleus was discovered, knowing that it contains almost all mass of the atom, it was therefore first thought that all nuclei are made of hydrogen nuclei. Being at the origin of the list of constituents, the hydrogen nucleus was named *proton*, from the greek term for 'first' and reminding the name of Prout at the same time. Protons carry a positive unit of electric charge, just the opposite of that of electrons, but are about 1836 times as heavy. More details on the proton are listed in Table 12.

However, the charge multiples and the mass multiples for the heavier nuclei do not match. On average, a nucleus that has n times the charge of a proton, has a mass that is about 2.6 n times than of the proton. Additional experiments confirmed an idea formulated by Werner Heisenberg: all nuclei heavier than hydrogen nuclei are made of positively charged *protons* and of neutral *neutrons*. Neutrons are particles a tiny bit more massive than protons (the difference is less than a part in 700, as shown in Table 12), but without any electrical charge. Since the mass is almost the same, the mass of nuclei – and thus that of atoms – is still an (almost perfect) integer multiple of the proton mass. But since neutrons are neutral, the mass and the charge number of nuclei differ. Being

Property	P r o t o n	Neutron	
Mass	$1.672621777(74)\cdot 10^{-27}\mathrm{kg}$	$1.674927351(74)\cdot 10^{-27}\mathrm{kg}$	
	0.150 327 7484(66) nJ	0.150 534 9631(66) nJ	
	938, 272 046(21) MeV	939, 565 379(21) MeV	
	1.007 276 466 812(90) u	1.008 664 916 00(43) u	
	1836.152 6675(39)∙ m <sub>e</sub>	1838.683 6605(11)∙ m <sub>e</sub>	
Spin	1/2	1/2	
P parity	+1	+1	
Antiparticle	antiproton <del>p</del>	antineutron n	
Quark content	uud	udd	
Electric charge	1 e	0	
Charge radius	0.88(1) fm	$0.12(1)\mathrm{fm}^2$	
Electric dipole moment	$< 5.4 \cdot 10^{-26} \mathrm{e} \cdot \mathrm{m}$	$<2.9\cdot10^{-28}~\mathrm{e}\cdot\mathrm{m}$	
Electric polarizability	$1.20(6) \cdot 10^{-3}  \mathrm{fm}^3$	$1.16(15) \cdot 10^{-3}  \mathrm{fm}^3$	
Magnetic moment	1.410 606 743(33) · 10 <sup>-26</sup> J/T	-0.966 236 47(23) · 10 <sup>-26</sup> J/T	
g-factor	5.585 694 713(46)	-3.826 085 45(90)	
c	$2.792847356(23)\cdot\mu_{ m N}$	$-1.91304272(45) \cdot \mu_N$	
Gyromagnetic ratio	0.267 522 2005(63) 1/nsT		
Magnetic polarizability	$1.9(5) \cdot 10^{-4}  \mathrm{fm}^3$	$3.7(2.0) \cdot 10^{-4}  \mathrm{fm}^3$	
Mean life (free particle)	$> 2.1 \cdot 10^{29}$ a	880.1(1.1) s	
Shape (quadrupole moment)	oblate	oblate	
Excited states	more than ten	more than ten	

TABLE 12 The properties of the nucleons: proton and neutron (source: pdg.web.cern.ch).

neutral, neutrons do not leave tracks in clouds chambers and are more difficult to detect than protons, charged hadrons or charged leptons. For this reason, the neutron was discovered later than several other, more exotic subatomic particles.

Today, it is possible to keep single neutrons suspended between suitably shaped coils, with the aid of teflon 'windows'. Such traps were proposed in 1951 by Wolfgang Paul. They work because neutrons, though they have no charge, do have a small magnetic moment. (By the way, this implies that neutrons are themselves composed of charged particles.) With a suitable arrangement of magnetic fields, neutrons can be kept in place, in other words, they can be levitated. Obviously, a trap only makes sense if the trapped particle can be observed. In case of neutrons, this is achieved by the radio waves absorbed

when the magnetic moment switches direction with respect to an applied magnetic field. The result of these experiments is simple: the lifetime of free neutrons is 885.7(8) s. Nevertheless, we all know that inside most nuclei we are made of, neutrons do not decay for millions of years, because the decay products do not lead to a state of lower energy. (Why not?)

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Magnetic resonance images also show that most elements have different types of atoms. These elements have atoms with the same number of protons, but with different numbers of neutrons. One says that these elements have several *isotopes*.\* This result also explains why some elements radiate with a mixture of different decay times. Though chemically isotopes are (almost) indistinguishable, they can differ strongly in their nuclear properties. Some elements, such as tin, caesium, or polonium, have over thirty isotopes each. Together, the 118 known elements have over 2000 isotopes. They are shown in Figure 100. (Isotopes without electrons, i.e., specific nuclei with a given number of neutrons and protons, are called *nuclides*.)

Because nuclei are so extremely dense despite containing numerous positively charged protons, there must be a force that keeps everything together against the electrostatic repulsion. We saw that the force is not influenced by electromagnetic or gravitational fields; it must be something different. The force must be short range; otherwise nuclei would not decay by emitting high energy  $\alpha$  rays. The additional force is called the *strong nuclear interaction*. We shall study it in detail shortly.

The strong nuclear interaction binds protons and neutrons in the nucleus. It is essential to recall that inside a nucleus, the protons and neutrons – they are often collectively called *nucleons* – move in a similar way to the electrons moving in atoms. Figure 99 illustrates this. The motion of protons and neutrons inside nuclei allows us to understand the shape, the spin and the magnetic moment of nuclei.

## NUCLEI CAN MOVE ALONE - COSMIC RAYS

In everyday life, nuclei are mostly found inside atoms. But in some situations, they move all by themselves, without surrounding electron clouds. The first to discover an example was Rutherford; with a clever experiment he showed that the  $\alpha$  particles emitted by many radioactive substance are helium nuclei. Like all nuclei,  $\alpha$  particles are small, so that they are quite useful as projectiles.

Then, in 1912, Viktor Heß<sup>\*\*</sup> made a completely unexpected discovery. Heß was intrigued by electroscopes (also called electrometers). These are the simplest possible detectors of electric charge. They mainly consist of two hanging, thin metal foils, such as two strips of aluminium foil taken from a chocolate bar. When the electroscope is

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<sup>\*</sup> The name is derived from the Greek words for 'same' and 'spot', as the atoms are on the same spot in the periodic table of the elements.

<sup>\*\*</sup> Viktor Franz Heß, (b. 1883 Waldstein, d. 1964 Mount Vernon), nuclear physicist, received the Nobel Prize in Physics in 1936 for his discovery of cosmic radiation. Heß was one of the pioneers of research into radioactivity. Heß' discovery also explained why the atmosphere is always somewhat charged, a result important for the formation and behaviour of clouds. Twenty years after the discovery of cosmic radiation, in 1932 Carl Anderson discovered the first antiparticle, the positron, in cosmic radiation; in 1937 Seth Neddermeyer and Carl Anderson discovered the muon; in 1947 a team led by Cecil Powell discovered the pion; in 1951, the  $\Lambda^0$  and the kaon  $K^0$  are discovered. All discoveries used cosmic rays and most of these discoveries led to Nobel Prizes.

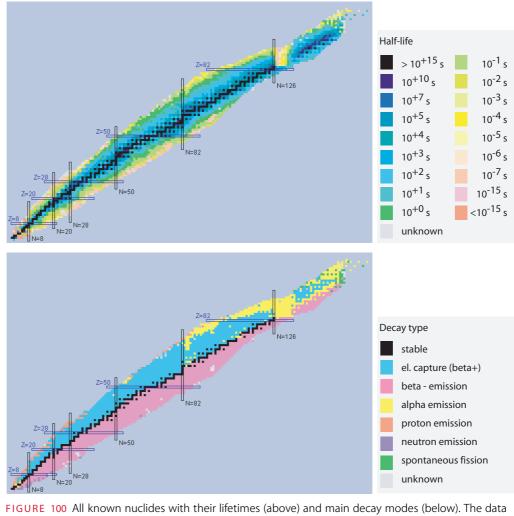
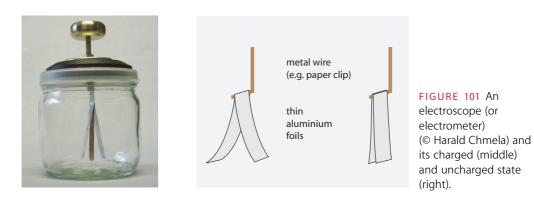


FIGURE 100 All known nuclides with their lifetimes (above) and main decay modes (below). The data are from www.nndc.bnl.gov/nudat2.



charged, the strips repel each other and move apart, as shown in Figure 101. (You can

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FIGURE 102 Viktor Heß (1883–1964)

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build one easily yourself by covering an empty glass with some transparent cellophane foil and suspending a paper clip and the aluminium strips from the foil. You can charge the electroscope with the help of a rubber balloon and a woollen pullover.) An electroscope thus measures electrical charge. Like many before him, Heß noted that even for a completely isolated electroscope, the charge disappears after a while. He asked: why? By careful study he eliminated one explanation after the other. Heß (and others) were left with only one possibility: that the discharge could be due to charged rays, such as those of the recently discovered radioactivity, emitted from the environment. To increase the distance to the environment, Heß prepared a sensitive electrometer and took it with him on a balloon flight.

As expected, the balloon flight showed that the discharge effect diminished with height, due to the larger distance from the radioactive substances on the Earth's surface. But above about 1000 m of height, the discharge effect increased again, and the higher he flew, the stronger it became. Risking his health and life, he continued upwards to more than 5000 m; there the discharge was several times faster than on the surface of the Earth. This result is exactly what is expected from a radiation coming from outer space and absorbed by the atmosphere. In one of his most important flights, performed during an (almost total) solar eclipse, Heß showed that most of the 'height radiation' did not come from the Sun, but from further away. He thus called the radiation *cosmic rays*. One also speaks of *cosmic radiation*. During the last few centuries, many people have drunk from a glass and eaten chocolate covered by aluminium foil; but only Heß combined these activities with such careful observation and deduction that he earned a Nobel Prize.\*

Today, the most common detectors for cosmic rays are *Geiger–Müller counters* and *spark chambers*. Both share the same idea; a high voltage is applied between two metal parts kept in a thin and suitably chosen gas (a wire and a cylindrical mesh for the Geiger-Müller counter, two plates or wire meshes in the spark chambers). When a high energy ionizing particle crosses the counter, a spark is generated, which can either be observed through the generated spark (as you can do yourself by watching the spark chamber in the entrance hall of the CERN main building), or detected by the sudden current flow. Historically, the current was first amplified and sent to a loudspeaker, so that the particles can be heard by a 'click' noise. In short, with a Geiger counter one cannot see ions or particles, but one can hear them. Later on, with the advances in electronics, ionized

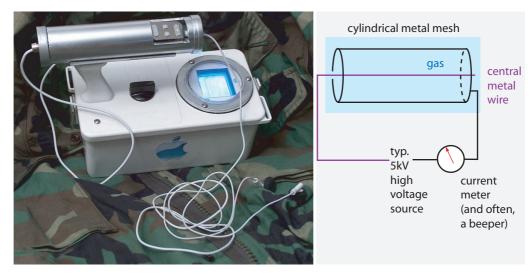
<sup>\*</sup> In fact, Hess used gold foils in his electrometer, not aluminium foils.

PARTICLE	E n e r g y	Origin	Detector	Shield
At high altitude, th	e primary particle	25:		
Protons (90 %)	10 <sup>9</sup> to 10 <sup>22</sup> eV	stars, supernovae, extragalactic, unknown	scintillator	in mines
a rays (9%)	typ. $5 \cdot 10^6 \text{ eV}$	stars, galaxy	ZnS, counters	1 mm of any material
Other nuclei, such as Le, Be, B, Fe (1 %)	10 <sup>9</sup> to 10 <sup>19</sup> eV	stars, novae	counters, films	1 mm of any material
Neutrinos	MeV, GeV	Sun, stars	chlorine, gallium, water	none
Electrons (0.1 %)	$10^{6}$ to > $10^{12}$ eV	supernova remnants		
Gammas (10 <sup>-6</sup> )	1 eV to 50 TeV	stars, pulsars, galactic, extragalactic	semiconductor detectors	in mines
At sea level, second	ary particles are j	produced in the atmosphe	ere:	
Muons	3 GeV, 150/ m <sup>2</sup> s	protons hit atmosphere, produce pions which decay into muons	drift chamber, bubble chamber, scintillation detector	15 m of water or 2.5 m of soil
Oxygen, radiocarbon and other nuclei	varies	e.g., $n + {}^{16}\text{O} \to p + {}^{14}\text{C}$	counters	soil
Positrons	varies		counters	soil
Neutrons	varies	reaction product when proton hits <sup>16</sup> O nucleus	counters	soil
Pions	varies	reaction product when proton hits <sup>16</sup> O nucleus	counters	soil
In addition, there as	re slowed down p	rimary beam particles.		

 TABLE 13 The main types of cosmic radiation.

atoms or particles could be counted.

Finding the right gas mixture for a Geiger–Müller counter is tricky; it is the reason that the counter has a double name. One needs a gas that extinguishes the spark after a while, to make the detector ready for the next particle. Müller was Geiger's assistant; he made the best counters by adding the right percentage of alcohol to the gas in the chamber. Nasty rumours maintained that this was discovered when another assistant tried,



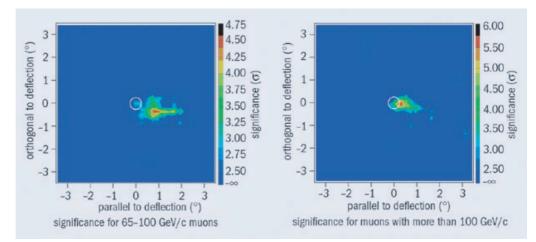
**FIGURE 103** A Geiger–Müller counter with the detachable detection tube, the connection cable to the counter electronics, and, for this model, the built-in music player (© Joseph Reinhardt).



FIGURE 104 A modern spark chamber showing the cosmic rays that constantly arrive on Earth (QuickTime film © Wolfgang Rueckner).

without success, to build counters while Müller was absent. When Müller, supposedly a heavy drinker, came back, everything worked again. However, the story is apocryphal. Today, Geiger-Müller counters are used around the world to detect radioactivity; the

#### **5 THE STRUCTURE OF THE NUCLEUS**



**FIGURE 105** The cosmic ray moon shadow, observed with the L3 detector at CERN. The shadow is shifted with respect of the position of the moon, indicated by a white circle, because the Earth's magnetic field deflects the charged particles making up cosmic rays (© CERN Courier).

smallest versions fit in mobile phones and inside wrist watches. An example is shown in Figure 103.

If you can ever watch a working spark chamber, do so. The one in the CERN entrance hall is about  $0.5 \text{ m}^3$  in size. A few times per minute, you can see the pink sparks showing the traces of cosmic rays. The rays appear in groups, called *showers*. And they hit us all the time.

Various particle detectors also allow measuring the energy of particles. The particle energy in cosmic rays spans a range between  $10^3$  eV and at least  $10^{20}$  eV; the latter is the same energy as a tennis ball after serve, but for a single ion. This is a huge range in energy. Understanding the origin of cosmic rays is a research field on its own. Some cosmic rays are galactic in origin, some are extragalactic. For most energies, supernova remnants – pulsars and the like – seem the best candidates. However, the source of the highest energy particles is still unknown; black holes might be involved in their formation.

Cosmic rays are probably the only type of radiation discovered without the help of shadows. But in the meantime, such shadows have been found. In a beautiful experiment performed in 1994, the shadow thrown by the Moon on high energy cosmic rays (about 10 TeV) was measured, as shown in Figure 105. When the position of the shadow is compared with the actual position of the Moon, a shift is found. And indeed, due to the magnetic field of the Earth, the cosmic ray Moon shadow is expected to be shifted westwards for protons and eastwards for antiprotons. The data are consistent with a ratio of antiprotons in cosmic rays between 0 % and 30 %. By studying the shadow's position, the experiment thus showed that high energy cosmic rays are mainly positively charged and thus consist mainly of matter, and only in small part, if at all, of antimatter.

Ref. 158

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Detailed observations showed that cosmic rays arrive on the surface of the Earth as a mixture of many types of particles, as shown in Table 13. They arrive from outside the atmosphere as a mixture of which the largest fraction are protons, followed by  $\alpha$  particles, iron and other nuclei. And, as mentioned above, most rays do not originate from the Sun. In other words, nuclei can thus travel alone over large distances. In fact,

#### **5 THE DENSEST CLOUDS**



FIGURE 106 An aurora borealis, produced by charged particles in the night sky (© Jan Curtis).

the distribution of the incoming direction of cosmic rays shows that many rays must be extragalactic in origin. Indeed, the typical nuclei of cosmic radiation are ejected from stars and accelerated by supernova explosions. When they arrive on Earth, they interact with the atmosphere before they reach the surface of the Earth. The detailed acceleration mechanisms at the origin of cosmic rays are still a topic of research.

The flux of *charged* cosmic rays arriving at the surface of the Earth depends on their energy. At the lowest energies, charged cosmic rays hit the human body many times a second. Measurements also show that the rays arrive in irregular groups, called *showers*. In fact, the *neutrino* flux is many orders of magnitude higher than the flux of charged rays, but does not have any effect on human bodies.

Cosmic rays have several effects on everyday life. Through the charges they pro-

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duce in the atmosphere, they are probably responsible for the start and for the jagged, non-straight propagation of lightning. (Lightning advances in pulses, alternating fast propagation for about 30 m with slow propagation, until they hit connect. The direction they take at the slow spots depends on the wind and the charge distribution in the atmosphere.) Cosmic rays are also important in the creation of rain drops and ice particles inside clouds, and thus indirectly in the charging of the clouds. Cosmic rays, together
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If the magnetic field of the Earth would not exist, we might get sick from cosmic rays. The magnetic field diverts most rays towards the magnetic poles. Also both the upper and lower atmosphere help animal life to survive, by shielding life from the harmful effects of cosmic rays. Indeed, aeroplane pilots and airline employees have a strong radiation exposure that is not favourable to their health. Cosmic rays are also one of several reasons that long space travel, such as a trip to Mars, is not an option for humans. When cosmonauts get too much radiation exposure, the body weakens and eventually they die. Space heroes, including those of science fiction, would not survive much longer than two or three years.

#### 5 THE STRUCTURE OF THE NUCLEUS

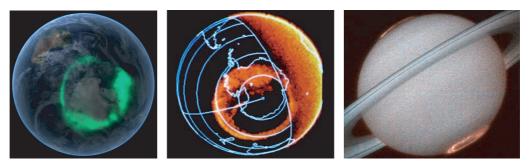


FIGURE 107 Two aurorae australes on Earth, seen from space (a composed image with superimposed UV intensity, and a view in the X-ray domain) and a double aurora on Saturn (all NASA).

Cosmic rays also produce beautifully coloured flashes inside the eyes of cosmonauts; they regularly enjoy these events in their trips. (And they all develop cataracts as a consequence.) But cosmic rays are not only dangerous and beautiful. They are also useful. If cosmic rays would not exist, we would not exist either. Cosmic rays are responsible for mutations of life forms and thus are one of the causes of biological evolution. Today, this effect is even used artificially; putting cells into a radioactive environment yields new strains. Breeders regularly derive new mutants in this way.

Cosmic rays cannot be seen directly, but their cousins, the 'solar' rays, can. This is most spectacular when they arrive in high numbers. In such cases, the particles are inevitably deviated to the poles by the magnetic field of the Earth and form a so-called *aurora borealis* (at the North Pole) or an *aurora australis* (at the South pole). These slowly moving and variously coloured curtains of light belong to the most spectacular effects in the night sky. (See Figure 106 or www.nasa.gov/mov/105423main\_FUV\_2005-01\_v01. mov.) Visible light and X-rays are emitted at altitudes between 60 and 1000 km. Seen from space, the aurora curtains typically form a circle with a few thousand kilometres diameter around the magnetic poles. Aurorae are also seen in the rest of the solar system. Aurorae due to core magnetic fields have been observed on Jupiter, Saturn, Uranus, Neptune, Earth, Io and Ganymede. For an example, see Figure 107. Aurorae due to other mechanisms have been seen on Venus and Mars.

Cosmic rays are mainly free nuclei. With time, researchers found that nuclei appear without electron clouds also in other situations. In fact, the vast majority of nuclei in the universe have no electron clouds at all: in the inside of stars, no nucleus is surrounded by bound electrons; similarly, a large part of intergalactic matter is made of protons. It is known today that most of the matter in the universe is found as protons or a particles inside stars and as thin gas between the galaxies. In other words, in contrast to what the Greeks said, matter is not usually made of atoms; it is mostly made of bare nuclei. Our everyday environment is an exception when seen on cosmic scales. In nature, atoms are rare, bare nuclei are common.

Incidentally, nuclei are in no way forced to move; nuclei can also be stored with almost no motion. There are methods – now commonly used in research groups – to superpose electric and magnetic fields in such a way that a single nucleus can be kept floating in mid-air; we discussed this possibility in the section on levitation earlier on.

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# NUCLEI DECAY – MORE ON RADIOACTIVITY

Not all nuclei are stable over time. The first measurement that provided a hint was the decrease of radioactivity with time. It is observed that the number N of emitted rays *decreases*. More precisely, radioactivity follows an exponential decay with time t:

$$N(t) = N(0) e^{-t/\tau} . (54)$$

The parameter  $\tau$ , the so-called *life time* or *decay time*, depends on the type of nucleus emitting the rays. Life times can vary from far less than a microsecond to millions of millions of years. The expression has been checked for as long as 34 multiples of the duration  $\tau$ ; its validity and precision is well-established by experiments. Obviously, formula (54) is an approximation for large numbers of atoms, as it assumes that N(t) is a continuous variable. Despite this approximation, deriving this expression from quantum theory is not a simple exercise, as we saw above. Though in principle, the quantum Zeno effect could appear for small times t, for the case of radioactivity it has not yet been observed.

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Instead of the life-time, often the half-life is used. The *half-life* is the time during which radioactivity decreases to *half* the starting value. Can you deduce how the two times are related?

*Radioactivity* is the decay of unstable nuclei. Most of all, radioactivity allows us to count the number of atoms in a given mass of material. Imagine to have measured the mass of radioactive material at the beginning of your experiment; you have chosen an element that has a lifetime of about a day. Then you put the material inside a scintillation box. After a few weeks the number of flashes has become so low that you can count them; using expression (54) you can then determine how many atoms have been in the mass to begin with. Radioactivity thus allows us to determine the number of atoms, and thus their size, in addition to the size of nuclei.

The exponential decay (54) and the release of energy is typical of *metastable* systems. In 1903, Rutherford and Soddy discovered what the state of lower energy is for  $\alpha$  and  $\beta$  emitters. In these cases, radioactivity changes the emitting atom; it is a spontaneous transmutation of the atom. An atom emitting  $\alpha$  or  $\beta$  rays changes its chemical nature. Radioactivity thus implies, for the case of nuclei, the same result that statistical mechanics of gases implies for the case of atoms: they are quantum particles with a structure that can change over time.

- In α decay or alpha decay the radiating nucleus emits a (doubly charged) helium nucleus, also called an α particle. The kinetic energy is typically a handful of MeV. After the emission, the nucleus has changed to a nucleus situated two places earlier in the periodic system of the elements. α decay occurs mainly for nuclei that are rich in protons. An example of α decay is the decay of the  $^{238}$ U isotope of uranium.
- In β decay or beta decay a neutron transforms itself into a proton, emitting an electron also called a β particle and an antineutrino. Also β decay changes the chemical nature of the atom, but to the place following the original atom in the periodic table of the elements. Example of β emitters are radiocarbon, <sup>14</sup>C, <sup>38</sup>Cl, and <sup>137</sup>Cs, the isotope expelled by damaged nuclear reactors. We will explore β decay below. A variant is the β<sup>+</sup> decay, in which a proton changes into a neutron and emits a neutrino and

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a positron. It occurs in proton-rich nuclei. An example is <sup>22</sup>Na. Another variant is electron capture; a nucleus sometimes captures an orbital electron, a proton is transformed into a neutron and a neutrino is emitted. This happens in <sup>7</sup>Be. Also bound  $\beta$ decay, as seen in  $^{187}$ Re, is a variant of  $\beta$  decay.

- In *y decay* or *gamma decay* the nucleus changes from an excited to a lower energy state by emitting a high energy photon, or *y particle*. In this case, the chemical nature is not changed. Typical energies are in the MeV range. Due to the high energy, y rays ionize the material they encounter; since they are not charged, they are not well absorbed by matter and penetrate deep into materials. y radiation is thus by far the most dangerous type of (environmental) radioactivity. An example of y decay is  $^{99m}$ Tc. A variant of  $\gamma$  decay is *isomeric transition*. Still another variant is *internal conversion*, observed, for example, in  $^{137m}$ Ba.
- In neutron emission the nucleus emits a neutron. The decay is rare on Earth, but occurs in the stellar explosions. Most neutron emitters have half-lives below a few seconds. Examples of neutron emitters are <sup>5</sup>He and <sup>17</sup>N.
- The process of spontaneous fission was discovered in 1940. The decay products vary, even for the same starting nucleus. But <sup>239</sup>Pu and <sup>235</sup>U can decay through spontaneous fission, though with a small probability.
- In proton emission the nucleus emits a proton. This decay is comparatively rare, and occurs only for about a hundred nuclides, for example for <sup>53m</sup>Co and <sup>4</sup>Li. The first example was discovered only in 1970. Around 2000, the simultaneous emission of two protons was also observed for the first time.
- In 1984, cluster emission or heavy ion emission was discovered. A small fraction of <sup>223</sup>Ra nuclei decay by emitting a <sup>14</sup>C nucleus. This decay occurs for half a dozen nuclides. Emission of <sup>18</sup>O has also been observed.
- Many combined and mixed decays also exist. These decays are studied by nuclear phys-Ref. 159 icists. Radioactivity is a common process. As an example, in every human body about nine thousand radioactive decays take place every second, mainly 4.5 kBq (0.2 mSv/a) from  ${}^{40}$ K and 4 kBq from  ${}^{14}$ C (0.01 mSv/a). Why is this not dangerous?

All radioactivity is accompanied by emission of energy. The energy emitted by an atom through radioactive decay or reactions is regularly a million times larger than that emitted by a chemical process. More than a decay, a radioactive process is thus a microscopic explosion. A highly radioactive material thus emits a large amount of energy. That is the reason for the danger of nuclear weapons.

What distinguishes those atoms that decay from those which do not? An exponential decay law implies that the probability of decay is independent of the age of the atom. Age or time plays no role. We also know from thermodynamics, that all atoms have exactly identical properties. So how is the decaying atom singled out? It took around 30 years to discover that radioactive decays, like all decays, are quantum effects. All decays are triggered by the statistical fluctuations of the vacuum, more precisely, by the quantum fluctuations of the vacuum. Indeed, radioactivity is one of the clearest observations that classical physics is not sufficient to describe nature.

Radioactivity, like all decays, is a pure quantum effect. Only a finite quantum of action makes it possible that a system remains unchanged until it suddenly decays. Indeed, in 1928 George Gamow explained  $\alpha$  decay with the tunnelling effect. He found that the

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<image>

FIGURE 108 A modern accelerator mass spectrometer for radiocarbon dating, at the Hungarian Academy of Sciences (© HAS).

tunnelling effect explains the relation between the lifetime and the range of the rays, as well as the measured variation of lifetimes – between 10 ns and  $10^{17}$  years – as the consequence of the varying potentials to be overcome in different nuclei.

# RADIOMETRIC DATING

As a result of the chemical effects of radioactivity, the composition ratio of certain elements in minerals allows us to determine the *age* of the mineral. Using radioactive decay to deduce the age of a sample is called *radiometric dating*. With this technique, geologists determined the age of mountains, the age of sediments and the age of the continents. They determined the time that continents moved apart, the time that mountains formed when the continents collided and the time when igneous rocks were formed. Where there surprises? No. The times found with radiometric dating are consistent with the relative time scale that geologists had defined independently for centuries before the technique appeared. Radiometric dating confirmed what had been deduced before.

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Ref. 160

Radiometric dating is a science of its own. An overview of the isotopes used, together with their specific applications in dating of specimen, is given in Table 14. The table shows how the technique of radiometric dating has deeply impacted astronomy, geology, evolutionary biology, archaeology and history. (And it has reduced the number of violent believers.) Radioactive life times can usually be measured to within one or two per cent

Ізоторе	D E C A Y P R O D U C T	H a l f - l i f e	METHOD USING IT	EXAMPLES
<sup>147</sup> Sm	<sup>143</sup> Nd	106 Ga	samarium–neodymium method	rocks, lunar soil, meteorites
<sup>87</sup> Rb	<sup>87</sup> Sr	48.8 Ga	rubidium–strontium method	rocks, lunar soil, meteorites
<sup>187</sup> Re	<sup>187</sup> Os	42 Ga	rhenium–osmium method	rocks, lunar soil, meteorites
<sup>176</sup> Lu	<sup>176</sup> Hf	37 Ga	lutetium–hafnium method	rocks, lunar soil, meteorites
<sup>40</sup> K	<sup>40</sup> Ar	1.25 Ga	potassium-argon & argon-argon method	rocks, lunar soil, meteorites
<sup>40</sup> K	<sup>40</sup> Ca	1.25 Ga	potassium-calcium method	granite dating, not precise
<sup>232</sup> Th	<sup>208</sup> Pb	14 Ga	thorium–lead method, lead–lead method	rocks, lunar soil, meteorites
<sup>238</sup> U	<sup>206</sup> Pb	4.5 Ga	uranium–lead method, lead–lead method	rocks, lunar soil, meteorites
<sup>235</sup> U	<sup>207</sup> Pb	0.7 Ga	uranium–lead method, lead–lead method	rocks, lunar soil, meteorites
<sup>234</sup> U	<sup>230</sup> Th	248 ka	uranium–thorium method	corals, stalagmites, bones, teeth
<sup>230</sup> Th	<sup>226</sup> Ra	75.4 ka	thorium-radon method	plant dating
<sup>26</sup> Al	<sup>26</sup> Mg	0.72 Ma	supernova debris dating, cosmogenic	checking that nucleosynthesis still takes place in the galaxy
<sup>10</sup> Be	<sup>10</sup> B	1.52 Ma	cosmogenic radiometric dating	ice cores
<sup>60</sup> Fe	<sup>60</sup> Ni	2.6 Ma (not 1.5 Ma)	supernova debris dating	deep sea crust
<sup>36</sup> Cl	<sup>36</sup> Ar	0.3 Ma	cosmogenic radiometric dating	ice cores
<sup>53</sup> Mn	<sup>53</sup> Cr	3.7 Ma	cosmogenic radiometric dating	meteorites, K/T boundary
<sup>182</sup> Hf	<sup>182</sup> W	9 Ma	cosmogenic radiometric dating	meteorites, sediments
<sup>14</sup> C	<sup>14</sup> N	5730 a	radiocarbon method, cosmogenic	wood, clothing, bones, organic material, wine
<sup>137</sup> Cs	<sup>137</sup> Ba	30 a	γ-ray counting	dating food and wine after nuclear accidents
<sup>210</sup> Pb		22 a	γ-ray counting	dating wine
<sup>3</sup> H	<sup>3</sup> He	12.3 a	γ-ray counting	dating wine

 TABLE 14 The main natural isotopes used in radiometric dating.

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of accuracy, and they are known both experimentally and theoretically not to change over geological time scales. As a result, radiometric dating methods can be surprisingly precise. Can you imagine how to measure half-lives of thousands of millions of years to high precision?

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Radiometric dating was even more successful in the field of ancient history. With the *radiocarbon dating method* historians determined the age of civilizations and the age of human artefacts.\* Many false beliefs were shattered. In some belief communities the shock is still not over, even though over hundred years have passed since these results became known.

Ref. 160

*Radiocarbon dating* uses the  $\beta$  decay of the radioactive carbon isotope <sup>14</sup>C, which has a decay time of 5730 a. This isotope is continually created in the atmosphere through the influence of cosmic rays. This happens through the reaction  ${}^{14}N + n \rightarrow p + {}^{14}C$ . As a result, the concentration of radiocarbon in air is relatively constant over time. Inside living plants, the metabolism thus (unknowingly) maintains the same concentration. In dead plants, the decay sets in. The life time value of a few thousand years is particularly useful to date historic material. Therefore, radiocarbon dating has been used to determine the age of mummies, the age of prehistoric tools and the age of religious relics. The original version of the technique measured the radiocarbon content through its radioactive decay and the scintillations it produced. A quality jump was achieved when accelerator mass spectroscopy became commonplace. It was not necessary any more to wait for decays: it is now possible to determine the <sup>14</sup>C content directly. As a result, only a tiny amount of carbon, as low as 0.2 mg, is necessary for a precise dating. Such small amounts can be detached from most specimen without big damage. Accelerator mass spectroscopy showed that numerous religious relics are forgeries, such as a cloth in Turin, and that, in addition, several of their wardens are crooks.

Researchers have even developed an additional method to date stones that uses radioactivity. Whenever an  $\alpha$  ray is emitted, the emitting atom gets a recoil. If the atom is part of a crystal, the crystal is damaged by the recoil. In many materials, the damage can be seen under the microscope. By counting the damaged regions it is possible to date the time at which rocks have been crystallized. In this way it has been possible to determine when the liquid material from volcanic eruptions has become rock.

With the advent of radiometric dating, for the first time it became possible to reliably date the age of rocks, to compare it with the age of meteorites and, when space travel became fashionable, with the age of the Moon. The result was beyond all previous estimates and expectations: the oldest rocks and the oldest meteorites, studied independently using different dating methods, are 4570(10) million years old. From this data, the age of the Earth is estimated to be 4540(50) million years. The Earth is indeed *old*.

Ref. 162

But if the Earth is so old, why did it not cool down in its core in the meantime?

# WHY IS HELL HOT?

The lava seas and streams found in and around volcanoes are the origin of the imagery that many cultures ascribe to hell: fire and suffering. Because of the high temperature of lava, hell is inevitably depicted as a hot place located at the centre of the Earth. A striking

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<sup>\*</sup> In 1960, the developer of the radiocarbon dating technique, Willard Libby, received the Nobel Prize in Chemistry.



FIGURE 109 The lava sea in the volcano Erta Ale in Ethiopia (© Marco Fulle).

example is the volcano Erta Ale, shown in Figure 109. But why is lava still hot, after so many million years?

A straightforward calculation shows that if the Earth had been a hot sphere in the beginning, it should have cooled down and solidified already long time ago. The Earth should be a solid object, like the moon: the Earth should not contain any magma nor eject any lava; hell would not be hot.

The solution to the riddle is provided by radioactivity: the centre of the Earth contains an oven that is fuelled with an estimated 8 to 10 TW by radioactive uranium <sup>235</sup>U and <sup>238</sup>U, with 8 to 10 TW by radioactive thorium <sup>232</sup>Th and with around 4 TW by radioactive potassium <sup>40</sup>K. The radioactivity of these elements, and a few others to a minor degree, keeps the centre of the Earth glowing. More precise investigations, taking into account the decay times and measured material concentrations, show that this mechanism indeed explains the internal heat of the Earth. (In addition, the decay of radioactive potassium is the origin for the 1% of argon found in the Earth's atmosphere.)

In short, radioactivity keeps lava hot. Radioactivity is the reason that we depict hell as hot. This brings up a challenge: why is the radioactivity of lava and of the Earth in general not dangerous to humans?

# NUCLEI CAN FORM COMPOSITES

Nuclei are highly unstable when they contain more than about 280 nucleons. Nuclei with higher number of nucleons inevitably decay into smaller fragments. In short, heavy nuclei are unstable. But when the mass is above  $10^{57}$  nucleons, they are stable again: such sys-

Challenge 131 ny

Ref. 163

Page 184

Challenge 132 s

#### **5 THE DENSEST CLOUDS**

tems are called *neutron stars*. This is the most extreme example of pure nuclear matter found in nature. Neutron stars are left overs of (type II) supernova explosions. They do not run any fusion reactions any more, as other stars do; in first approximation neutron stars are simply large nuclei.

Neutron stars are made of degenerate matter. Their density of  $10^{18}$  kg/m<sup>3</sup> is a few times that of a nucleus, as gravity compresses the star. This density value means that a tea spoon of such a star has a mass of several hundred million tons. Neutron stars are about 10 km in diameter. They are never much smaller, as such smaller stars are unstable. They are never much larger, because much larger neutron stars turn into black holes.

# NUCLEI HAVE COLOURS AND SHAPES

In everyday life, the colour of objects is determined by the wavelength of light that is least absorbed, or, if they shine, by the wavelength that is emitted. Also nuclei can absorb photons of suitably tuned energies and get into an excited state. In this case, the photon energy is converted into a higher energy of one or several of the nucleons whirling around inside the nucleus. Many radioactive nuclei also emit high energy photons, which then are called  $\gamma$  rays, in the range between 1 keV (or 0.2 fJ) and more than 20 MeV (or 3.3 pJ). The emission of  $\gamma$  rays by nuclei is similar to the emission of light by electrons in atoms. From the energy, the number and the lifetime of the excited states – they range from 1 ps to 300 d – researchers can deduce how the nucleons move inside the nucleus.

In short, the energies of the emitted and absorbed  $\gamma$  ray photons define the 'colour' of the nucleus. The  $\gamma$  ray spectrum can be used, like all colours, to distinguish nuclei from each other and to study their motion. In particular, the spectrum of the  $\gamma$  rays emitted by excited nuclei can be used to determine the chemical composition of a piece of matter. Some of these transition lines are so narrow that they can been used to study the change due to the chemical environment of the nucleus, to measure nuclear motion inside solids or to detect the gravitational Doppler effect.

The study of  $\gamma$ -rays also allows us to determine the *shape* of nuclei. Many nuclei are spherical; but many are prolate or oblate ellipsoids. Ellipsoids are favoured if the reduction in average electrostatic repulsion is larger than the increase in surface energy. All nuclei – except the lightest ones such as helium, lithium and beryllium – have a constant mass density at their centre, given by about 0.17 nucleons per fm<sup>3</sup>, and a skin thickness of about 2.4 fm, where their density decreases. Nuclei are thus small clouds, as illustrated in Figure 110.

We know that molecules can be of extremely involved shape. In contrast, nuclei are mostly spheres, ellipsoids or small variations of these. The reason is the short range, or better, the fast spatial decay of nuclear interactions. To get interesting shapes like in molecules, one needs, apart from nearest neighbour interactions, also next neighbour interactions and next next neighbour interactions. The strong nuclear interaction is too short ranged to make this possible. Or does it? It might be that future studies will discover that some nuclei are of more unusual shape, such as smoothed pyramids. Some predictions have been made in this direction; however, the experiments have not been performed yet.

Ref. 164

The shape of nuclei does not have to be fixed; nuclei can also *oscillate* in shape. Such oscillations have been studied in great detail. The two simplest cases, the quadrupole and

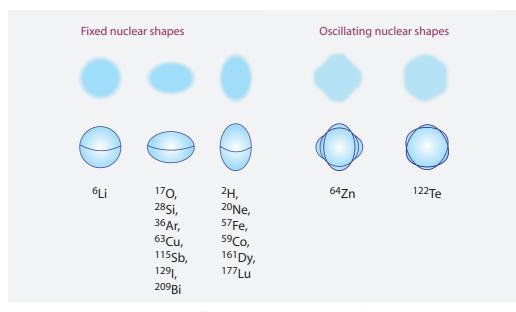


FIGURE 110 Various nuclear shapes – fixed: spherical, oblate, prolate (left) and oscillating (right), shown realistically as clouds (above) and simplified as geometric shapes (below).

octupole oscillations, are shown in Figure 110. In addition, non-spherical nuclei can also rotate. Several rapidly spinning nuclei, with a spin of up to  $60\hbar$  and more, are known. They usually slow down step by step, emitting a photon and reducing their angular momentum at each step. Recently it was even discovered that nuclei can also have bulges that rotate around a fixed core, a bit like the tides that rotate around the Earth.

Ref. 165

# The four types of motion in the nuclear domain

Nuclei are small because the nuclear interactions are short-ranged. Due to this short range, nuclear interactions play a role only in four types of motion:

- scattering,
- *bound motion,*
- *decay* and
- a combination of these three called *nuclear reactions*.

The history of nuclear physics has shown that the whole range of observed phenomena can be reduced to these four fundamental processes. Each process is a type of motion. And in each process, the main interest is the comparison of the start and the end situations; the intermediate situations are less interesting. Nuclear interactions thus lack the complex types of motion which characterize everyday life. That is also the main reason for the shortness of this chapter.

*Scattering* is performed in all accelerator experiments. Such experiments repeat for nuclei what we do when we look at an object. Eye observation, or seeing something, is a scattering experiment, as eye observation is the detection of scattered light. Scattering of X-rays was used to see atoms for the first time; scattering of high energy alpha particles

was used to discover and study the nucleus, and later the scattering of electrons with even higher energy was used to discover and study the components of the proton.

*Bound motion* is the motion of protons and neutrons inside nuclei or the motion of quarks inside mesons and baryons. In particular, bound motion determines shape and changes of shape of compounds: hadrons and nuclei.

*Decay* is obviously the basis of radioactivity. Nuclear decay can be due to the electromagnetic, the strong or the weak nuclear interaction. Decay allows studying the conserved quantities of nuclear interactions.

*Nuclear reactions* are combinations of scattering, decay and possibly bound motion. Nuclear reactions are for nuclei what the touching of objects is in everyday life. Touching an object we can take it apart, break it, solder two objects together, throw it away, and much more. The same can be done with nuclei. In particular, nuclear reactions are responsible for the burning of the Sun and the other stars; they also tell the history of the nuclei inside our bodies.

Quantum theory showed that all four types of nuclear motion can be described in the same way. Each type of motion is due to *the exchange of virtual particles*. For example, scattering due to charge repulsion is due to exchange of virtual photons, the bound motion inside nuclei due to the strong nuclear interaction is due to exchange of virtual gluons,  $\beta$  decay is due to the exchange of virtual W bosons, and neutrino reactions are due to the exchange of virtual Z bosons. The rest of this chapter explains these mechanisms in more details.

# NUCLEI REACT

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The first man thought to have made transuranic elements, the physics genius Enrico Fermi, received the Nobel Prize in Physics for the discovery. Shortly afterwards, Otto Hahn and his collaborators Lise Meitner and Fritz Strassmann showed that Fermi was wrong, and that his prize was based on a mistake. Fermi was allowed to keep his prize, the Nobel committee gave Hahn and Strassmann the Nobel Prize as well, and to make the matter unclear to everybody and to women physicists in particular, the prize was not given to Lise Meitner. (After her death though, a new chemical element was named after her.)

When protons or neutrons are shot into nuclei, they usually remained stuck inside them, and usually lead to the transformation of an element into a heavier one. After having done this with all elements, Fermi used uranium; he found that bombarding it with neutrons, a new element appeared, and concluded that he had created a transuranic element. Alas, Hahn and his collaborators found that the element formed was well-known: it was barium, a nucleus with less than half the mass of uranium. Instead of remaining stuck as in the previous 91 elements, the neutrons had *split* the uranium nucleus. In short, Fermi, Hahn, Meitner and Strassmann had observed reactions such as:

$$^{235}\text{U} + n \rightarrow {}^{143}\text{Ba} + {}^{90}\text{Kr} + 3n + 170 \,\text{MeV}$$
 (55)

Meitner called the splitting process *nuclear fission*. The amount of energy liberated in fission is unusually large, millions of times larger than in a chemical interaction of an atom. In addition, several neutrons are emitted, which in turn can lead to the same pro-

cess; fission can thus start a *chain reaction*. Later, and (of course) against the will of the team, the discovery would be used to make nuclear bombs.

Nuclear reactions are typically triggered by neutrons, protons, deuterons or  $\gamma$  particles. Apart from triggering fission, neutrons are used to transform lithium into tritium, which is used as (one type of) fuel in fusion reactors; and neutrons from (secondary) cosmic rays produce radiocarbon from the nitrogen in the atmosphere. Deuterons impinging on tritium produce helium in fusion reactors. Protons can trigger the transformation of lithium into beryllium. Photons can knock alpha particles or neutrons out of nuclei.

All nuclear reactions and decays are *transformations*. In each transformation, already the ancient Greek taught us to search, first of all, for conserved quantities. Besides the well-known cases of energy, momentum, electric charge and angular momentum conservation, the results of nuclear physics lead to several new conserved quantities. The behaviour is quite constrained. Quantum field theory implies that particles and antiparticles (commonly denoted by a bar) must behave in compatible ways. Both experiment and quantum field theory show for example that every reaction of the type

 $A + \overline{C} \rightarrow \overline{B} + D$ 

$$A + B \to C + D \tag{56}$$

implies that the reactions

or

$$\overline{C} + \overline{D} \to \overline{A} + \overline{B} \tag{58}$$

or, if energy is sufficient,

$$A \to C + D + \overline{B}, \qquad (59)$$

are also possible. Particles thus behave like conserved mathematical entities.

Experiments show that antineutrinos differ from neutrinos. In fact, all reactions confirm that the so-called *lepton number* is conserved in nature. The lepton number *L* is zero for nucleons or quarks, is 1 for the electron and the neutrino, and is -1 for the positron and the antineutrino.

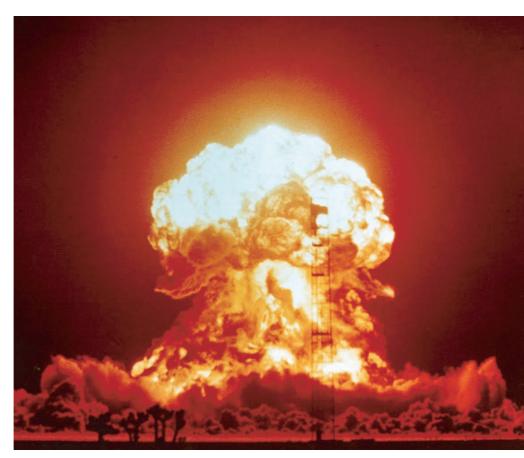
In addition, all reactions conserve the so-called *baryon number*. The baryon number *B* for protons and neutrons is 1 (and 1/3 for quarks), and -1 for antiprotons and antineutrons (and thus -1/3 for antiquarks). So far, no process with baryon number violation has ever been observed. Baryon number conservation is one reason for the danger of radioactivity, fission and fusion. The concept of baryon number was introduced by Ernst Stückelberg (b. 1905 Basel, d. 1984 Geneva), an important physicist who discovered several other concepts of particle physics, including Feynman diagrams before Feynman himself. Baryon number was renamed when Abraham Pais (b. 1918 Amsterdam, d. 2000 Copenhagen) introduced the terms 'lepton' and 'baryon'.

(57)





FIGURE 111 The destruction of four nuclear reactors in 2011 in Fukushima, in Japan, which rendered life impossible at a distance of 30 km around it (courtesy Digital Globe).



**FIGURE 112** The explosion of a nuclear bomb: an involved method of killing many children in the country where it explodes and ruining the economic future of many children in the country that built it.

# Bombs and nuclear reactors

Uranium fission is triggered by a neutron, liberates energy and produces several additional neutrons. Therefore, uranium fission can trigger a *chain reaction* that can lead either to an explosion or to a controlled generation of heat. Once upon a time, in the middle of the twentieth century, these processes were studied by quite a number of researchers. Most of them were interested in making weapons or in using nuclear energy, despite the high toll these activities place on the economy, on human health and on the environment.

Most stories around the development of nuclear weapons are almost incredibly absurd. The first such weapons were built during the Second World War, with the help of the smartest physicists that could be found. Everything was ready, including the most complex physical models, several huge factories and an organization of incredible size. There was just one little problem: there was no uranium of sufficient quality. The mighty United States thus had to go around the world to shop for good uranium. They found it in the (then) Belgian colony of Congo, in central Africa. In short, without the support of Belgium, which sold the Congolese uranium to the USA, there would have been no nuclear bomb, no early war end and no superpower status.

Congo paid a high price for this important status. It was ruled by a long chain of military dictators up to this day. But the highest price was paid by the countries that actually built nuclear weapons. Some went bankrupt, others remained underdeveloped; even the richest countries have amassed huge debts and a large underprivileged population. There is *no* exception. The price of nuclear weapons has also been that some regions of our planet became uninhabitable, such as numerous islands, deserts, rivers, lakes and marine environments. But it could have been worse. When the most violent physicist ever, Edward Teller, made his first calculations about the hydrogen bomb, he predicted that the bomb would set the atmosphere into fire. Nobel Prize winner Hans Bethe\* corrected the mistake and showed that nothing of this sort would happen. Nevertheless, the military preferred to explode the hydrogen bomb in the Bikini atoll, the most distant place from their homeland they could find. The place is so radioactive that today it is even dangerous simply to fly over that island!

Ref. 166

It was then noticed that nuclear test explosions increased ambient radioactivity in the atmosphere all over the world. Of the produced radioactive elements, <sup>3</sup>H is absorbed by humans in drinking water, <sup>14</sup>C and <sup>90</sup>Sr through food, and <sup>137</sup>Cs in both ways. Fortunately, in the meantime, all countries have agreed to perform their nuclear tests underground.

Radioactivity is dangerous to humans, because it disrupts the processes inside living cells. Details on how radioactivity is measured and what effects on health it produces are provided below.

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Not only nuclear bombs, also peaceful nuclear reactors are dangerous. The reason was

<sup>\*</sup> Hans Bethe (b. 1906 Strasbourg, d. 2005) was one of the great physicists of the twentieth century, even though he was head of the theory department that lead to the construction of the first atomic bombs. He worked on nuclear physics and astrophysics, helped Richard Feynman in developing quantum electrodynamics, and worked on solid state physics. When he got older and wiser, he became a strong advocate of arms control; he also was essential in persuading the world to stop atmospheric nuclear test explosions and saved many humans from cancer in doing so.

MATERIAL	ACTIVITY IN
	Bq/kg
Air	<i>c</i> . 10 <sup>-2</sup>
Sea water	$10^{1}$
Human body	$c. 10^2$
Cow milk	max. 10 <sup>3</sup>
Pure <sup>238</sup> U metal	$c. 10^7$
Highly radioactive α emitters	> 10 <sup>7</sup>
Radiocarbon: <sup>14</sup> C ( $\beta$ emitter)	$10^{8}$
Highly radioactive $\beta$ and $\gamma$ emitters	> 10 <sup>9</sup>
Main nuclear fallout: <sup>137</sup> Cs, <sup>90</sup> Sr (α emitter)	$2 \cdot 10^9$
Polonium, one of the most radioactive materials $\left(\alpha\right)$	$10^{24}$

TABLE 15 Some radioactivity measurements.

discovered in 1934 by Frédéric Joliot and his wife Irène, the daughter of Pierre and Marie Curie: *artificial radioactivity*. The Joliot–Curies discovered that materials irradiated by  $\alpha$  rays become radioactive in turn. They found that  $\alpha$  rays transformed aluminium into radioactive phosphorus:

$${}^{27}_{13}\text{Al} + {}^{4}_{2}\alpha \to {}^{30}_{15}\text{P} + {}^{1}_{0}\text{n} .$$
(60)

In fact, almost all materials become radioactive when irradiated with alpha particles, neutrons or  $\gamma$  rays. As a result, radioactivity itself can only be contained with difficulty. After a time span that depends on the material and the radiation, any box that contains radioactive material has itself become radioactive. The 'contagion' stops only for very small amounts of radioactive material.

The dangers of natural and artificial radioactivity are the reason for the high costs of nuclear reactors. After about thirty years of operation, reactors have to be dismantled. The radioactive pieces have to be stored in specially chosen, inaccessible places, and at the same time the workers' health must not be put in danger. The world over, many reactors now need to be dismantled. The companies performing the job sell the service at high price. All operate in a region not far from the border to criminal activity, and since radioactivity cannot be detected by the human senses, many companies cross that border.

In fact, one important nuclear reactor is (usually) not dangerous to humans: the Sun.

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We explore it shortly.

# CURIOSITIES AND CHALLENGES ON NUCLEI AND RADIOACTIVITY

Nowadays, nuclear magnetic resonance is also used to check the quality of food. For example, modern machines can detect whether orange juice is contaminated with juice from other fruit and can check whether the fruit were ripe when pressed. Other machines can check whether wine was made from the correct grapes and how it aged.

\* \*

#### **5 THE STRUCTURE OF THE NUCLEUS**



FIGURE 113 A machine to test fruit quality with the help of nuclear magnetic resonance (© Bruker).

Ref. 171

Ref. 167

Magnetic resonance machines pose no danger; but they do have some biological effects, as Peter Mansfield, one of the inventors of the technique, explains. The first effect is due to the conductivity of blood. When blood in the aorta passes through a magnetic field, a voltage is induced. This effect has been measured and it might interfere with cardiac functioning at 7 T; usual machines have 1.5 T and pose no risk. The second effect is due to the switching of the magnetic field. Some people sense the switching in the thorax and in the shoulders. Not much is known about the details of such peripheral nerve stimulation yet.

\* \*

The amount of radioactive radiation is called the *dose*. The unit for the radioactive dose is one *gray*: it is the amount of radioactivity that deposits the energy 1 J on 1 kg of matter: 1 Gy = 1 J/kg. A *sievert*, or 1 Sv, is the unit of radioactive dose *equivalent*; it is adjusted to humans by weighting each type of human tissue with a factor representing the impact of radiation deposition on it. Three to five sievert are a lethal dose to humans. In comparison, the natural radioactivity present inside human bodies leads to a dose of 0.2 mSv per year. An average X-ray image implies an irradiation of 1 mSv; a CAT scan 8 mSv. For other measurement examples, see Table 15.

The *amount of radioactive material* is measured by the number of nuclear decays per second. One decay per second is called one *becquerel*, or 1 Bq. An adult human body typically contains 9 kBq, the European limit for food, in 2011, varies between 370

#### 5 THE DENSEST CLOUDS

TABLE 16 Human exposure to radioactivity and the corresponding doses.

Exposure	Dose	
Daily human exposure:		
Average exposure to cosmic radiation in Europe		
at sea level	0.3 mSv/a	
at a height of 3 km	1.2 mSv/a	
Average (and maximum) exposure from the soil,	0.4 mSv/a (2 mSv/a)	
not counting radon effects		
Average (and maximum) inhalation of radon	1 mSv/a (100 mSv/a)	
Average exposure due to internal radionuclides	0.3 mSv/a	
natural content of <sup>40</sup> K in human muscles	$10^{-4}$ Gy and 4500 Bq	
natural content of Ra in human bones	$2 \cdot 10^{-5}$ Gy and 4000 Bq	
natural content of <sup>14</sup> C in humans	$10^{-5}  \text{Gy}$	
Total average (and maximum) human exposure	2 mSv/a (100 mSv/a)	
Common situations:		
Dental X-ray	c. 10 mSv equivalent dose	
Lung X-ray	c. 0.5 mSv equivalent dose	
Short one hour flight (see www.gsf.de/epcard)	<i>c.</i> 1 μSv	
Transatlantic flight	<i>c</i> . 0.04 mSv	
Maximum allowed dose at work	30 mSv/a	
Smoking 60 cigarettes a day	26 to 120 mSv/a	
Deadly exposures:		
Ionization	0.05 C/kg can be deadly	
Dose	100 Gy=100 J/kg is deadly in 1 to 3 days	
Equivalent dose	more than 3 Sv leads to death for 50 % of untreated patients	

and 600 Bq/kg. The amount released by the Hiroshima bomb is estimated to have been between 4 PBq and 60 PBq, the amount released by the Chernobyl disaster was between 2 and 12 EBq, thus between 200 and 500 times larger. The numbers for the various Russian radioactive disasters in the 1960s and 1970 are similarly high. The release for the Fukushima reactor disaster in March 2011 is estimated to have been 370 to 630 PBq, which would put it at somewhere between 10 and 90 Hiroshima bombs.

The SI units for radioactivity are now common around the world; in the old days, 1 sievert was called 100 rem or 'Röntgen equivalent man'; the SI unit for dose, 1 gray, replaces what used to be called 100 rd or Rad. The SI unit for exposure, 1 C/kg, replaces the older unit 'röntgen', with the relation  $1 \text{ R} = 2.58 \cdot 10^{-4} \text{ C/kg}$ . The SI unit becquerel replaces the curie (Ci), for which 1 Ci = 37 GBq.



FIGURE 114 A dated image of Lake Karachay and the nuclear plant that was filling it with radioactivity (© Unknown).

Ref. 168

Not all γ-rays are due to radioactivity. In the year 2000, an Italian group discovered that thunderstorms also emit γ rays, of energies up to 10 MeV. The mechanisms are still being investigated; they seem to be related to the formation process of lightning.

\*

*Chain reactions* are quite common in nature, and are not limited to the nuclear domain. *Fire* is a chemical chain reaction, as are exploding fireworks. In both cases, material needs heat to burn; this heat is supplied by a neighbouring region that is already burning.

Radioactivity can be extremely dangerous to humans. The best example is plutonium. Only 1  $\mu$ g of this  $\alpha$  emitter inside the human body are sufficient to cause lung cancer. Another example is polonium. Polonium 210 is present in tobacco leaves that were grown with artificial fertilizers. In addition, tobacco leaves filter other radioactive substances from the air. Polonium, lead, potassium and the other radioactive nuclei found in tobacco are the main reason that *smoking produces cancer*. Table 16 shows that the dose is considerable and that it is by far the largest dose absorbed in everyday life.

Why is nuclear power a dangerous endeavour? The best argument is Lake Karachay near Mayak, in the Urals in Russia. In less than a decade, the nuclear plants of the region have transformed it into the most radioactive place on Earth. In the 1970s, walking on the

#### 5 THE DENSEST CLOUDS

shore of the lake for an hour led to death on the shore. The radioactive material in the lake was distributed over large areas in several catastrophic explosions in the 1950s and 1960s, leading to widespread death and illness. Several of these accidents were comparable to the Chernobyl accident of 1986; they were kept secret. Today, in contrast to Figure 114, the lake is partly filled with concrete – but not covered with it, as is often assumed.

\* \*

Ref. 169

All lead is slightly radioactive, because it contains the <sup>210</sup>Pb isotope, a  $\beta$  emitter. This lead isotope is produced by the uranium and thorium contained in the rock from where the lead is extracted. For sensitive experiments, such as for neutrino experiments, one needs radioactivity shields. The best shield material is lead, but obviously it has to be lead with a low radioactivity level. Since the isotope <sup>210</sup>Pb has a half-life of 22 years, one way to do it is to use *old* lead. In a precision neutrino experiment in the Gran Sasso in Italy, the research team uses lead mined during Roman times, thus 2000 years old, in order to reduce spurious signals.

\* \*

Not all nuclear reactors are human made. The occurrence of *natural* nuclear reactors have been predicted in 1956 by Paul Kuroda. In 1972, the first such example was found. In Oklo, in the African country of Gabon, there is a now famous geological formation where uranium is so common that two thousand million years ago a *natural* nuclear reactor has formed spontaneously – albeit a small one, with an estimated power generation of 100 kW. It has been burning for over 150 000 years, during the time when the uranium 235 percentage was 3 % or more, as required for chain reaction. (Nowadays, the uranium 235 content on Earth is 0.7 %.) The water of a nearby river was periodically heated to steam during an estimated 30 minutes; then the reactor cooled down again for an estimated 2.5 hours, since water is necessary to moderate the neutrons and sustain the chain reaction. The system has been studied in great detail, from its geological history up to the statements it makes about the constancy of the 'laws' of nature. The studies showed that 2000 million years ago the mechanisms were the same as those used today.

Nuclear reactors exist in many sizes. The largest are used in power plants and can produce over 1000 MW in electrical power; the smallest are used in satellites, and usually produce around 10 kW. All work without refuelling for between one and thirty years.

\* \*

Radioactivity also has forensic uses. On many surfaces, it is hard to make finger prints visible. One method is to put the object in question in an atmosphere of radioactive iodine or radioactive sulphur dioxide. The gases react with the substances in finger prints. The fingerprints have thus become radioactive. Looking at the scintillation signals of the prints – a method called *autoradiography* – then allows imaging the fingerprint simply by laying a photographic film or an equivalent detector over the object in question.

\* \*

In contrast to massive particles, massless particles cannot decay at all. There is a simple

reason for it: massless particles do not experience time, as their paths are 'null'. A particle that does not experience time cannot have a half-life. (Can you find another argument?)

Challenge 133 s

High energy radiation is dangerous to humans. In the 1950s, when nuclear tests were still made above ground by the large armies in the world, the generals overruled the orders of the medical doctors. They positioned many soldiers nearby to watch the explosion, and worse, even ordered them to walk to the explosion site as soon as possible after the explosion. One does not need to comment on the orders of these generals. Several of these unlucky soldiers made a strange observation: during the flash of the explosion, they were able to see the bones in their own hand and arms. How can this be?

\*

Challenge 134 s

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In 1958, six nuclear bombs were made to explode in the stratosphere by a vast group of criminals. A competing criminal group performed similar experiments in 1961, followed by even more explosions by both groups in 1962. (For reports and films, see en. wikipedia.org/wiki/High\_altitude\_nuclear\_explosion.) As a result of most of these explosions, an *artificial aurora* was triggered the night following each of them. In addition, the electromagnetic pulse from the blasts destroyed satellites, destroyed electronics on Earth, disturbed radio communications, injured people on the surface of the Earth, caused problems with power plants, and distributed large amounts of radioactive material over the Earth – during at least 14 years following the blasts. The van Allen radiation belts around the Earth were strongly affected; it is expected that the lower van Allen belt will recover from the blasts only in a few hundred years. Fortunately for the human race, after 1962, this activity was stopped by international treaties.

Nuclear bombs are terrible weapons. To experience their violence but also the criminal actions of many military people during the tests, have a look at the pictures of explosions. In the 1950s and 60s, nuclear tests were performed by generals who refused to listen to doctors and scientists. Generals ordered to explode these weapons in the air, making the complete atmosphere of the world radioactive, hurting all mankind in doing so; worse, they even obliged soldiers to visit the radioactive explosion site a few minutes after the explosion, thus doing their best to let their own soldiers die from cancer and leukaemia. Generals are people to avoid.

Several radioactive dating methods are used to date wine, and more are in development. A few are included in Table 14.

\* \*

\* \*

A few rare radioactive decay times can be changed by external influence. Electron capture, as observed in beryllium-7, is one of the rare examples were the decay time can change, by up to 1.5 %, depending on the chemical environment. The decay time for the same isotope has also been found to change by a fraction of a per cent under pressures

#### **5 THE DENSEST CLOUDS**

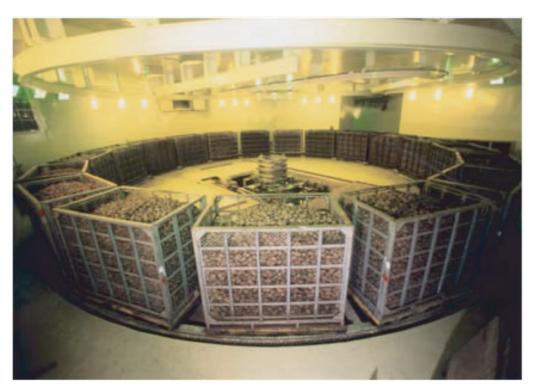


FIGURE 115 Potatoes being irradiated at the Shihorocho Agricultural Cooperative Isotope Irradiation Center in Japan. Good appetite!

of 27 GPa. On the other hand, these effects are predicted (and measured) to be negligible for nuclei of larger mass. A few additional nuclides show similar, but smaller effects.

The most interesting effect on nuclei is laser-induced fissioning of <sup>238</sup>U, which occurs for very high laser intensities.

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Ref. 159

Both  $\gamma$  radiation and neutron radiation can be used to image objects without destroying them.  $\gamma$  rays have been used to image the interior of the Tutankhamun mask. Neutron radiation, which penetrates metals as easily as other materials, has been used to image, even at film speed, the processes inside car engines.

\* \*

 $\gamma$  rays are used in Asia to irradiate food. This is forbidden other countries, such as Germany. For example,  $\gamma$  rays are used to irradiate potatoes, in order to prevent sprouting. An example is given in Figure 115. It is better not to work there. In fact, over 30 countries allowed the food industry to irradiate food. For example, almost all spice in the world are treated with  $\gamma$  rays, to increase their shelf life. However, the consumer is rarely informed about such treatments.

 $\beta$  rays with 10 MeV and  $\gamma$  rays are used in many large factories across the world to sterilize

medical equipment, medical devices, toys, furniture and also to kill moulds in books and in animal food. (See www.bgs.eu for an example.)

\* \*

The non-radioactive isotopes  ${}^{2}H$  – often written simply D – and  ${}^{18}O$  can be used for measuring energy production in humans in an easy way. Give a person a glass of doubly labelled water to drink and collect his urine samples for a few weeks. Using a mass spectrometer one can determine his energy consumption. Why? Doubly labelled water  ${}^{2}H_{2}{}^{18}O$  is processed by the body in three main ways. The oxygen isotope is expired as  $C^{18}O_{2}$  or eliminated as  $H_{2}{}^{18}O$ ; the hydrogen isotope is eliminated as  ${}^{2}H_{2}O$ . Measurements on the urine allow one to determine carbon dioxide production, therefore to determine how much has food been metabolized, and thus to determine energy production.

Human energy consumption is usually given in joule per day. Measurements showed that high altitude climbers with  $20\,000 \text{ kJ/d}$  and bicycle riders with up to  $30\,000 \text{ kJ/d}$  are the most extreme sportsmen. Average humans produce  $6\,000 \text{ kJ/d}$ .

The percentage of the <sup>18</sup>O isotope in the water of the Earth's oceans can be used to deduce where the water came from. This was told in the first volume of our adventure.

Many nuclei oscillate in shape. The calculation of these shape oscillations is a research subject in itself. For example, when a spherical nucleus oscillates, it can do so in three mutually orthogonal axes. A spherical nucleus, when oscillating at small amplitudes, thus behaves like a three-dimensional harmonic oscillator. Interestingly, the symmetry of the three-dimensional harmonic oscillator is SU(3), the same symmetry that characterizes the strong nuclear interaction. However, the two symmetries are unrelated – at least following present knowledge. A relation might appear in the future, though.

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# Summary on nuclei

Atomic nuclei are composed of protons and neutrons. Their diameter is between one and a few femtometres, and they have angular momentum. Their angular momentum, if larger than zero, allows us to produce magnetic resonance images. Nuclei can be spherical or ellipsoidal, they can be excited to higher energy states, and they can oscillate in shape. Nuclei have colours that are determined by their spectra. Nuclei can decay, can scatter, can break up and can react among each other. Nuclear reactions can be used to make bombs, power plants, generate biological mutations and to explore the human body. And as we will discover in the following, nuclear reactions are at the basis of the working of the Sun and of our own existence.



# CHAPTER 6 THE SUN, THE STARS AND THE BIRTH OF MATTER

Lernen ist Vorfreude auf sich selbst.\*\* Peter Sloterdijk

uclear physics is the most violent part of physics. But despite this bad image, uclear physics has also something fascinating to offer: by exploring uclei, we learn to understand the Sun, the stars, the early universe, the birth of matter and our own history.

Nuclei consist of protons and neutrons. Since protons are positively charged, they repel each other. Inside nuclei, protons must be bound by a force strong enough to keep them together against their electromagnetic repulsion. This is the *strong nuclear interaction*; it is needed to avoid that nuclei explode. The strong nuclear interaction is the strongest of the four interactions in nature – the others being gravitation, electromagnetism and the weak nuclear interaction. Despite its strength, we do not experience the strong nuclear interaction in everyday life, because its range is limited to distances of a few femtometres, i.e., to a few proton diameters. Despite this limitation, the strong interaction tells a good story about the burning of the Sun and about the flesh and blood we are made of.

# The Sun

At present, the Sun emits 385 YW of light. The amount was first measured by Claude Pouillet at the start of the nineteenth century. The power would be sufficient to melt away, every year, a volume of ice 500 times larger than the volume of the Earth.

Where does the huge energy emitted by the Sun come from? If it came from burning coal, the Sun would stop burning after a few thousands of years. When radioactivity was discovered, researchers tested the possibility that this process might be at the heart of the Sun's shining. However, even though radioactivity – or the process of fission that was discovered later – is able to release more energy than chemical burning, the composition of the Sun – mostly hydrogen and helium – makes this impossible.

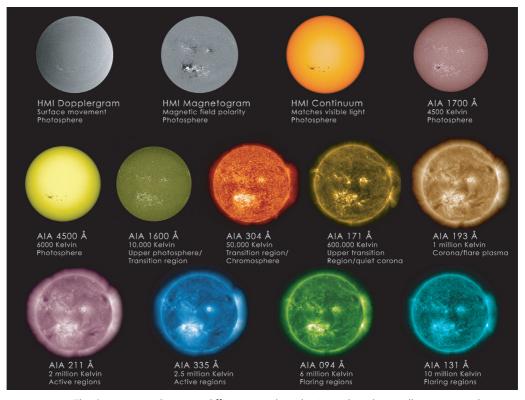
The origin of the energy radiated by the Sun was clarified in 1929 by Fritz Houtermans,
 Ref. 173 Carl Friedrich von Weiszäcker, and Hans Bethe: the Sun burns by *hydrogen fusion*. Fusion is the composition of a large nucleus from smaller ones. In the Sun, the central fusion reaction

$$4^{-1}H \to {}^{4}He + 2e^{+} + 2\nu + 4.4 \,\mathrm{pJ} \tag{61}$$

Ref. 172

<sup>\*\* &#</sup>x27;Learning is anticipated joy about yourself.'

## 6 THE SUN, THE STARS



**FIGURE 116** The Sun emits radiation at different wavelengths. Note that almost all images are shown in a single, false colour selected just for visual appeal. The collections does not show the radio wave images, which also show the solar spots, but with much lower resolution. (Courtesy NASA)

converts hydrogen nuclei into helium nuclei. The reaction is called the *hydrogen-hydrogen cycle* or p-p cycle. The hydrogen cycle is the result of a continuous cycle of three separate nuclear reactions:

$$p + p \rightarrow d + e^{+} + \nu$$
 (a weak nuclear reaction involving the deuteron)  
 $d + p \rightarrow {}^{3}\text{He} + \gamma$  (a strong nuclear reaction)  
 ${}^{3}\text{He} + {}^{3}\text{He} \rightarrow \alpha + 2 p + \gamma$ . (62)

We can also write the p-p cycle as

$${}^{1}H + {}^{1}H \rightarrow {}^{2}H + e^{+} + \nu \quad (a \text{ weak nuclear reaction})$$

$${}^{2}H + {}^{1}H \rightarrow {}^{3}He + \gamma \quad (a \text{ strong nuclear reaction})$$

$${}^{3}He + {}^{3}He \rightarrow {}^{4}He + 2 {}^{1}H + \gamma . \qquad (63)$$

In total, four protons are thus fused to one helium nucleus, or alpha particle; if we include the electrons, we can say that four hydrogen atoms are fused to one helium atom. The fusion process emits neutrinos and light with a total energy of 4.4 pJ (26.7 MeV). This is

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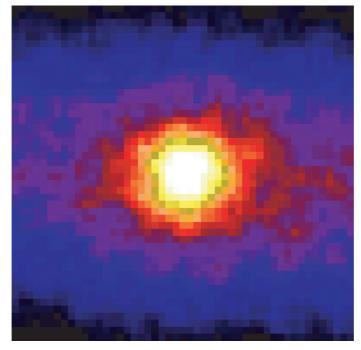


FIGURE 117 The Sun also emits neutrinos. Their intensities are shown here in a false colour image, taken through the whole Earth from an underground experiment, with a 503-day exposure, at energies from 7 to 25 MeV. However, due to scattering processes, the bright spot is several times the size of the Sun. (© Robert Svoboda)

the energy that makes the Sun shine. Most of the energy is emitted as light; around 10 % is carried away by neutrinos. The latter part is illustrated in Figure 117.

The first of the three reactions of equation (62) is due to the weak nuclear interaction. This transmutation and the normal  $\beta$  decay have the same first-order Feynman diagram. The weak interaction avoids that fusion happens too rapidly and ensures that the Sun will shine still for some time. Indeed, in the Sun, with a luminosity of 385 YW, there are thus only 10<sup>38</sup> fusions per second. This allows us to deduce that the Sun will last another handful of Ga (Gigayears) before it runs out of fuel.

The simplicity of the hydrogen-hydrogen cycle does not fully purvey the fascination of the process. On average, protons in the Sun's centre move with 600 km/s. Only if they hit each other precisely head-on can a nuclear reaction occur; in all other cases, the electrostatic repulsion between the protons keeps them apart. For an average proton, a head-on collision happens once every 7 thousand million years! Nevertheless, there are so many proton collisions in the Sun that every second four million tons of hydrogen are burned to helium. The second reaction of the proton cycle takes a few seconds and the third about one million years.

The fusion reaction (62) takes place in the centre of the Sun, in the so-called *core*. Fortunately for us, the high energy  $\gamma$  photons generated in the Sun's centre are 'slowed' down by the outer layers of the Sun, namely the *radiation zone*, the *convection zone* with its involved internal motion, and the so-called *photosphere*, the thin layer we actually see. The last layer, the atmosphere, is not visible during a day, but only during an eclipse, as shown in Figure 120. More precisely, the solar atmosphere consists of the *temperature minimum*, the *chromosphere*, the *transition region*, the *corona* and the *heliosphere*.

During the elaborate slowing-down process inside the Sun, the y photons are pro-

#### Challenge 136 e

Ref. 174

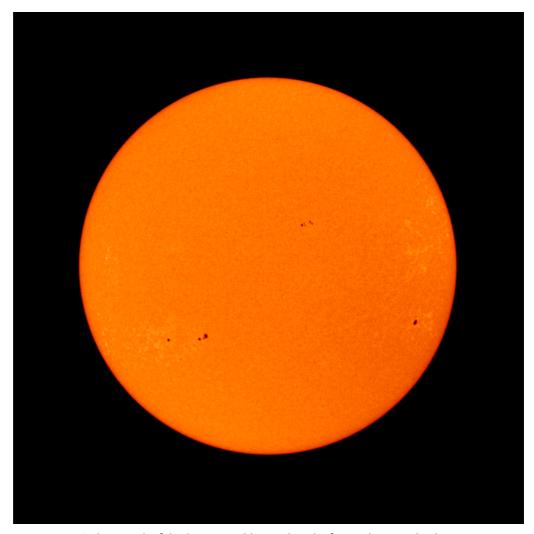


FIGURE 118 A photograph of the Sun at a visible wavelength of around 677 nm, by the SOHO space probe, showing a few sunspots (ESA and NASA).

Ref. 175

gressively converted to visible photons, mainly through scattering. Scattering takes time. In the Sun, it takes along time: the sunlight of today was in fact generated at the time of the Neandertals: a typical estimate is about 170 000 years ago. In other words, the average effective speed of light inside the Sun is estimated to be around 300 km/year! After these one hundred and seventy thousand years, the photons take another 8.3 minutes to reach the Earth and to sustain the life of all plants and animals.

# Motion in and on the Sun

Vol. III, page 148 Challenge 137 e In its core, the Sun has a temperature of around 15 MK. At its surface, the temperature is around 5.8 kK. (Why is it cooler?) Since the Sun is cooler on its surface than in its centre, the Sun is not a homogeneous ball, but an inhomogeneous structure. If you want to experience the majestic beauty of the Sun, watch the stunning video www.youtube.

#### AND THE BIRTH OF MATTER

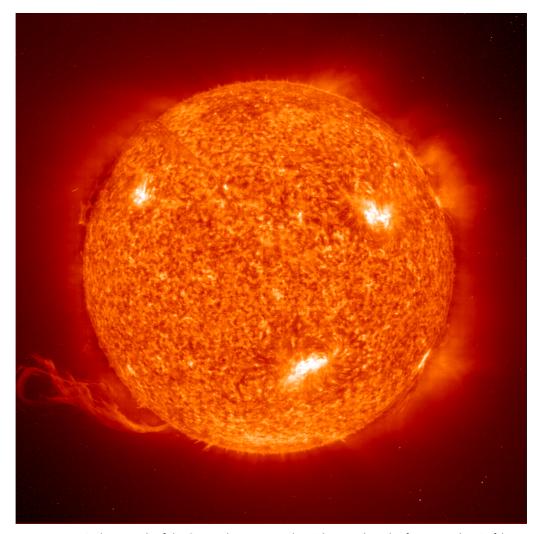


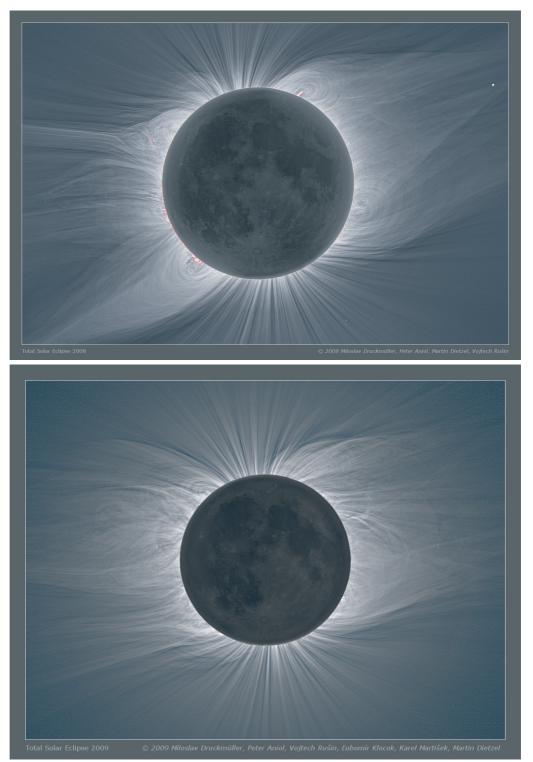
FIGURE 119 A photograph of the Sun at the extreme ultraviolet wavelength of 30.4 nm, thus in false colour, again by the SOHO space probe, showing solar prominences (ESA and NASA).

com/watch?v=ipvfwPqh3V4 that shows the Sun's surface over a two-week period. The inhomogeneity of the Sun's structure and surface is due to the convection processes induced by the temperature gradient. The convection, together with the rotation of the Sun around its axis, leads to fascinating structures that are shown in Figure 119 and the following ones: *solar eruptions*, including flares and coronal mass ejections, and *solar spots*.

In short, the Sun is not a static object. The matter in the Sun is in constant motion. An impressive way to experience the violent processes it contains is to watch the film shown in Figure 122, which shows the evolution of a so-called *solar flare*. Many solar eruptions, such as those shown in the lower left corner in Figure 119 or in Figure 123, eject matter far into space. When this matter reaches the Earth,\* after being diluted by the journey, it affects our everyday environment. Such *solar storms* can deplete the higher atmosphere

<sup>\*</sup> It might also be that the planets affect the solar wind; the issue is not settled and is still under study.

# 6 THE SUN, THE STARS



**FIGURE 120** The complex details of the corona of the Sun during the 2008 eclipse in Bor Udzuur in Mongolia and the 2009 eclipse on the Marshall Islands. The images are digital compositions of several dozen photographs chosen to reproduce the experience of looking at the eclipse through a small telescope. The structures also allow to locate the solar poles. The top image includes protuberances. (Top image © Miloslav Druckmüller, Martin Dietzel, Peter Aniol, Vojtech Rušin; bottom image © Miloslav Druckmüller, Peter Aniol, Vojtech Rušin, Ľubomír Klocok, Karel Martišek and Martin Dietzel)

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#### AND THE BIRTH OF MATTER

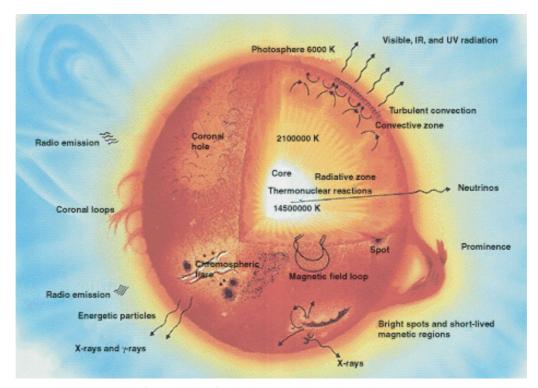
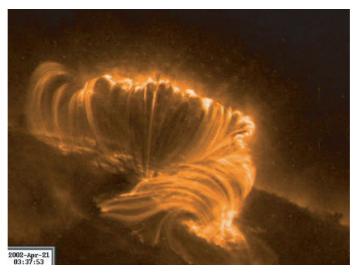


FIGURE 121 A drawing of the interior of the Sun (courtesy NASA).



**FIGURE 122** The evolution of a solar flare observed by the TRACE satellite (QuickTime film courtesy NASA).

and can thus possibly even trigger usual Earth storms. Other effects of solar storms are the formation of auroras and the loss of orientation of birds during their migration; this happens during exceptionally strong solar storms, because the magnetic field of the Earth

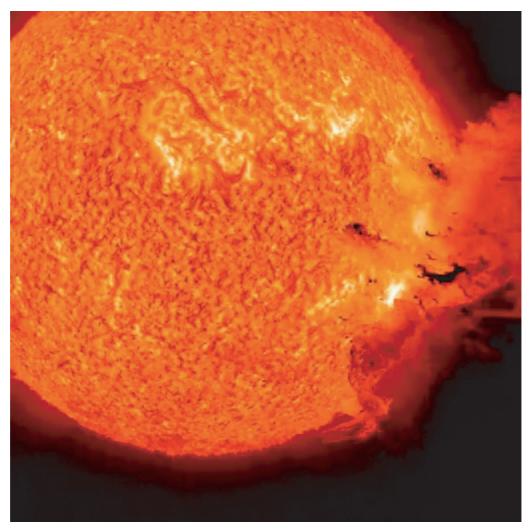


FIGURE 123 A spectacular coronal mass ejection observed on June 7, 2011 by the Solar Dynamic Observatory satellite (QuickTime film courtesy NASA).

is disturbed in these situations. A famous effect of a solar storm was the loss of electricity in large parts of Canada in March of 1989. The flow of charged solar particles triggered large induced currents in the power lines, blew fuses and destroyed parts of the network, shutting down the power system. Millions of Canadians had no electricity, and in the most remote places it took two weeks to restore the electricity supply. Due to the coldness of the winter and a train accident resulting from the power loss, over 80 people died. In the meantime, the power network has been redesigned to withstand such events.

How can the Sun's surface have a temperature of 6 kK, whereas the Sun's *corona* – the thin gas emanating from and surrounding the Sun that is visible during a total solar eclipse, as shown in Figure 120 – reaches one to three million Kelvin on average, with localized peaks inside a flare of up to 100 MK? In the latter part of the twentieth century it was shown, using satellites, that the magnetic field of the Sun is the cause; through the violent flows in the Sun's matter, magnetic energy is transferred to the corona in those places were flux tubes form knots, above the bright spots in the left of Figure 119 or above the dark spots in Figure 118. As a result, the particles of the corona are accelerated and heat the corona to temperatures that are a thousand times higher than those at the surface of the Sun.

#### WHY DO THE STARS SHINE?

Don't the stars shine beautifully? I am the only person in the world who knows why they do. Friedrich (Fritz) Houtermans \*

All stars shine because of fusion. When two light nuclei are fused to a heavier one, some energy is set free, as the average nucleon is bound more strongly. This energy gain is possible until nuclei of iron <sup>56</sup>Fe are produced. For nuclei beyond this nucleus, as shown in Figure 124, the binding energies per nucleon then decrease again; thus fusion is not energetically possible. It turns out that the heavier nuclei found on Earth and across the universe were formed through *neutron capture*. In short, nuclei below iron are made through fusion, nuclei above iron are made through neutron capture. And for the same reason, nuclei release energy through *fusion* when the result is lighter than iron, and release energy through *fission* when the starting point is above iron.

The different stars observed in the sky<sup>\*\*</sup> can be distinguished by the type of fusion nuclear reaction that dominates them. Most stars, in particular young or light stars, run hydrogen fusion. But that is not all. There are several types of hydrogen fusion: the direct hydrogen–hydrogen (p–p) cycle, as found in the Sun and in many other stars, and the various CNO cycle(s) or Bethe-Weizsäcker cycle(s).

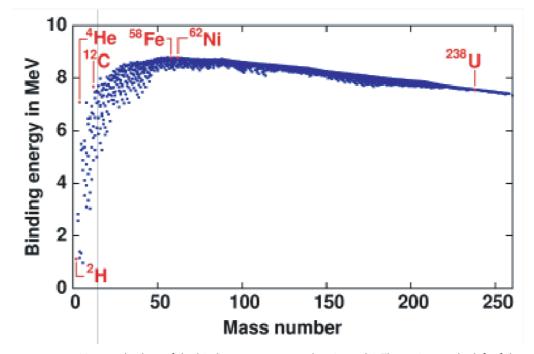
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The hydrogen cycle was described above and can be summarized as

$$4^{1}H \rightarrow {}^{4}He + 2e^{+} + 2\nu + 4.4 \,\mathrm{pJ}$$
(64)

<sup>\*</sup> Friedrich Houtermans (1903–1966) was one of the most colourful physicists of his time. He lived in Austria, England, the Soviet Union, Germany and the United States. He was analyzed by Sigmund Freud, imprisoned and tortured by the NKWD in Russia, then imprisoned by the Gestapo in Germany, then worked on nuclear fission. He worked with George Gamow and Robert Atkinson.

<sup>\*\*</sup> To find out which stars are in the sky above you at present, see the www.surveyor.in-berlin.de/himmel website.



**FIGURE 124** Measured values of the binding energy *per nucleon* in nuclei. The region on the left of the maximum, located at <sup>58</sup>Fe, is the region where *fusion* is energetically possible; the right region is where *fission* is possible (© Max Planck Institute for Gravitational Physics).

or, equivalently,

$$4 p \to \alpha + 2 e^{+} + 2 v + 26.7 \,\text{MeV} \,. \tag{65}$$

But this is not the only way for a star to burn. If a star has heavier elements inside it, the hydrogen fusion uses these elements as catalysts. This happens through the so-called Bethe-Weizsäcker cycle or CNO cycle, which runs as

$${}^{12}C + {}^{1}H \rightarrow {}^{13}N + \gamma$$

$${}^{13}N \rightarrow {}^{13}C + e^{+} + \nu$$

$${}^{13}C + {}^{1}H \rightarrow {}^{14}N + \gamma$$

$${}^{14}N + {}^{1}H \rightarrow {}^{15}O + \gamma$$

$${}^{15}O \rightarrow {}^{15}N + e^{+} + \nu$$

$${}^{15}N + {}^{1}H \rightarrow {}^{12}C + {}^{4}He$$
(66)

The end result of the cycle is the *same* as that of the hydrogen cycle, both in nuclei and in energy. The Bethe-Weizsäcker cycle is faster than hydrogen fusion, but requires higher temperatures, as the protons must overcome a higher energy barrier before reacting with carbon or nitrogen than when they react with another proton. (Why?) Inside the Sun, due to the comparatively low temperature of a few tens of million kelvin, the Bethe-Weizsäcker cycle (and its variations) is not as important as the hydrogen cycle.

Challenge 138 s

AND THE BIRTH OF MATTER

The proton cycle and the Bethe-Weizsäcker cycle are not the only options for the burning of stars. Heavier and older stars than the Sun can also shine through other fusion reactions. In particular, when no hydrogen is available any more, stars run *helium burning*:

$$3^{4}\text{He} \rightarrow {}^{12}\text{C} . \tag{67}$$

This fusion reaction, also called the *triple-a process*, is of low probability, since it depends on three particles being at the same point in space at the same time. In addition, small amounts of carbon disappear rapidly via the reaction  $\alpha + {}^{12}C \rightarrow {}^{16}O$ . Nevertheless, since <sup>8</sup>Be is unstable, the reaction with 3 alpha particles is the only way for the universe to produce carbon. All these negative odds are countered only by one feature: carbon has an excited state at 7.65 MeV, which is 0.3 MeV above the sum of the alpha particle masses; the excited state *resonantly enhances* the low probability of the three particle reaction. Only in this way the universe is able to produce the atoms necessary for apes, pigs and people. The prediction of this resonance by Fred Hoyle is one of the few predictions in physics made from the simple experimental observation that humans exist. The story has lead to a huge outflow of metaphysical speculations, most of which are unworthy of being even mentioned.

The studies of star burning processes also explain why the Sun and the stars do not collapse. In fact, the Sun and most stars are balls of hot gas, and the *gas pressure* due to the high temperature of its constituents prevents their concentration into a small volume. For other types of stars – especially those of high mass such as red giants – the *radiation pressure* of the emitted photons prevents collapse; for still other stars, such as neutron stars, the role is taken by the *Pauli pressure*.

The nuclear reaction rates at the interior of a star are extremely sensitive to its temperature *T*. The carbon cycle reaction rate is proportional to between  $T^{13}$  for hot massive O stars and  $T^{20}$  for stars like the Sun. In red giants and supergiants, the triple- $\alpha$  reaction rate is proportional to  $T^{40}$ ; these strong dependencies imply that stars usually shine with constancy over long times, often thousands and millions of years, because any change in temperature would be damped by a very efficient feedback mechanism. Of course, there are exceptions: variable stars get brighter and darker with periods of a few days; some stars change in brightness every few years. And even the Sun shows such effects. In the 1960s, it was discovered that the Sun pulsates with a frequency of 5 minutes. The amplitude is small, only 3 kilometres out of 1.4 million; nevertheless, it is measurable. In the meantime, helioseismologists have discovered numerous additional oscillations of the Sun, and in 1993, even on other stars. Such oscillations allow studying what is happening inside stars, even separately in each of the layers they consist of.

By the way, it is still not clear how much the radiation of the Sun changes over long time scales. There is an 11 year periodicity, the famous *solar cycle*, but the long term trend is still unknown. Precise measurements cover only the years from 1978 onwards, which makes only about 3 cycles. A possible variation of the intensity of the Suns, the so-called *solar constant* might have important consequences for climate research; however, the issue is still open.

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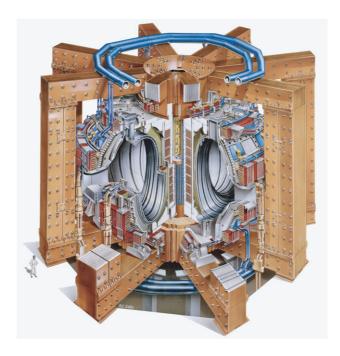


FIGURE 125 A simplified drawing of the Joint European Torus in operation at Culham, showing the large toroidal chamber and the magnets for the plasma confinement (© EFDA-JET).

# Why are fusion reactors not common yet?

Across the world, for over 50 years, a large number of physicists and engineers have tried to build fusion reactors. Fusion reactors try to copy the mechanism of energy release used by the Sun. The first machine that realized macroscopic energy production through fusion was, in 1991, the Joint European Torus<sup>\*</sup> (JET for short) located in Culham in the United Kingdom. Despite this success, the produced power was still somewhat smaller than the power needed for heating.

Ref. 176

The idea of JET is to produce an extremely hot plasma that is as dense as possible. At high enough temperature and density, fusion takes place; the energy is released as a particle flux that is transformed (like in a fission reactor) into heat and then into electricity. To achieve ignition, JET used the fusion between deuterium and tritium, because this reaction has the largest cross section and energy gain:

$$D + T \to He^4 + n + 17.6 \,\text{MeV}$$
 (68)

Because tritium is radioactive, most research experiments are performed with the far less efficient deuterium–deuterium reactions, which have a lower cross section and a lower energy gain:

$$D + D \rightarrow T + H + 4 \text{ MeV}$$
  
$$D + D \rightarrow He^{3} + n + 3.3 \text{ MeV}.$$
 (69)

<sup>\*</sup> See www.jet.edfa.org.

Fusion takes place when deuterium and tritium (or deuterium) collide at high energy. The high energy is necessary to overcome the electrostatic repulsion of the nuclei. In other words, the material has to be hot. To release energy from deuterium and tritium, one therefore first needs energy to heat it up. This is akin to the ignition of wood: in order to use wood as a fuel, one first has to heat it with a match.

Ref. 177

Following the so-called *Lawson criterion*, rediscovered in 1957 by the English engineer John Lawson, after its discovery by Russian researchers, a fusion reaction releases energy only if the triple product of density *n*, reaction (or containment) time  $\tau$  and temperature *T* exceeds a certain value. Nowadays this criterion is written as

$$n\tau T > 3 \cdot 10^{28} \,\mathrm{s\,K/m^3}$$
 (70)

In order to realize the Lawson criterion, JET uses temperatures of 100 to 200 MK, particle densities of 2 to  $3 \cdot 10^{20} \text{ m}^{-3}$ , and confinement times of 1 s. The temperature in JET is thus much higher than the 15 MK at the centre of the Sun, because the densities and the confinement times are much lower.

Matter at these temperatures is in form of a plasma: nuclei and electrons are completely separated. Obviously, it is impossible to pour a 100 MK plasma into a container: the walls would instantaneously evaporate. The only option is to make the plasma float in a vacuum, and to avoid that the plasma touches the container wall. The main challenge of fusion research in the past has been to find a way to keep a hot gas mixture of deuterium and tritium suspended in a chamber so that the gas never touches the chamber walls. The best way is to suspend the gas using a magnetic field. This works because in the fusion plasma, charges are separated, so that they react to magnetic fields. The most successful geometric arrangement was invented by the famous Russian physicists Igor Tamm and Andrei Sakharov: the tokamak. Of the numerous tokamaks around the world, JET is the largest and most successful. Its concrete realization is shown in Figure 125. JET manages to keep the plasma from touching the walls for about a second; then the situation becomes unstable: the plasma touches the wall and is absorbed there. After such a disruption, the cycle consisting of gas injection, plasma heating and fusion has to be restarted. As mentioned, JET has already achieved ignition, that is the state were more energy is released than is added for plasma heating. However, so far, no sustained commercial energy production is planned or possible, because JET has no attached electrical power generator.

The successor project, *ITER*, an international tokamak built with European, Japanese, US-American and Russian funding, aims to pave the way for commercial energy generation. Its linear reactor size will be twice that of JET; more importantly, ITER plans to achieve 30 s containment time. ITER will use superconducting magnets, so that it will have extremely cold matter at 4 K only a few metres from extremely hot matter at 100 MK. In other words, ITER will be a high point of engineering. The facility is being built in Cadarache in France. Due to its lack of economic sense, ITER has a good chance to be a modern version of the tower of Babylon; but maybe one day, it will start operation.

Like many large projects, fusion started with a dream: scientists spread the idea that fusion energy is safe, clean and inexhaustible. These three statements are still found on every fusion website across the world. In particular, it is stated that fusion reactors are not dangerous, produce much lower radioactive contamination than fission reactors, and use water as basic fuel. 'Solar fusion energy would be as clean, safe and limitless as the Sun.' In reality, the only reason that we do not feel the radioactivity of the Sun is that we are far away from it. Fusion reactors, like the Sun, are highly radioactive. The management of radioactive fusion reactors is much more complex than the management of radioactive fission reactors.

It is true that fusion fuels are almost inexhaustible: deuterium is extracted from water and the tritium – a short-lived radioactive element not found in nature in large quantities – is produced from *lithium*. The lithium must be enriched, but since material is not radioactive, this is not problematic. However, the production of tritium from lithium is a dirty process that produces large amounts of radioactivity. Fusion energy is thus inexhaustible, but not safe and clean.

In summary, of all technical projects ever started by mankind, fusion is by far the most challenging and ambitious. Whether fusion will ever be successful – or whether it ever should be successful – is another issue.

# Where do our atoms come from?

The elements were made in less time than you could cook a dish of duck and roast potatoes. George Gamow

Ref. 178

People consist of electrons and various nuclei. Where did the nucleosynthesis take place? Many researchers contributed to answering this question.

About three minutes after the big bang, when temperature was around 0.1 MeV, protons and neutrons formed. About seven times as many protons as neutrons were formed, mainly due to their mass difference. Due to the high densities, the neutrons were captured, through the intermediate step of deuterium nuclei, in  $\alpha$  particles. The process stopped around 20 minutes after the big bang, when temperatures became too low to allow fusion. After these seventeen minutes, the mass of the universe was split into 75 % of hydrogen, 25 % of helium (both percentages result from the factor 7 between the number of protons and neutrons), and traces of deuterium, lithium and beryllium. This process is called *primordial nucleosynthesis*. No heavier elements were formed, because the temperature fall prevented their accumulation in measurable quantities, and because there are no stable nuclei with 5 or 8 nucleons.

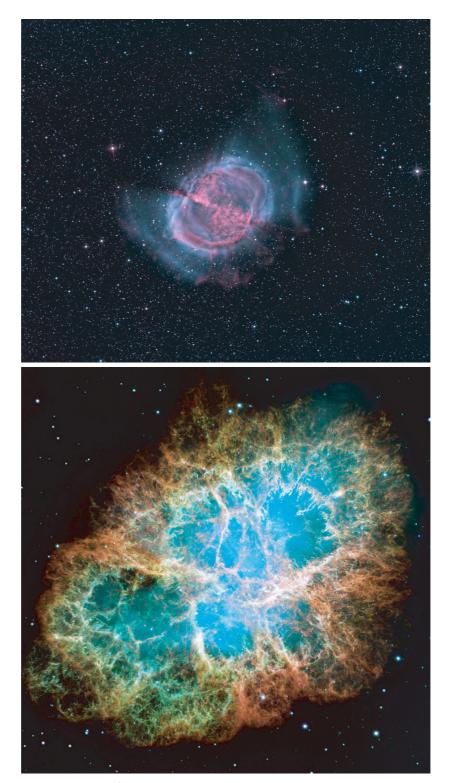
Simulations of primordial nucleosynthesis agree well with the element abundances found in extremely distant, thus extremely old stars. The abundances are deduced from the spectra of these stars. In short, *hydrogen, helium, lithium and beryllium nuclei are formed shortly after ('during') the big bang.* These are the so-called *primordial elements.* 

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Ref. 179

All other nuclei are formed many millions of years after the big bang. In particular, *other light nuclei are formed in stars*. Young stars run hydrogen burning or helium burning; heavier and older stars run neon-burning or even silicon-burning. These latter processes require high temperatures and pressures, which are found only in stars with a mass at least eight times that of the Sun. All these fusion processes are limited by photodissociation and thus will only lead to nuclei up to  $^{56}$ Fe.

*Nuclei heavier than iron can only be made by* neutron capture. There are *two* main neutron capture processes. The first process is the so-called *s-process* – for 'slow'. The process occurs inside stars, and gradually builds up heavy elements – including the most



**FIGURE 126** Two examples of how exploding stars shoot matter into interstellar space: the Crab nebula M1 and the Dumbbell nebula M27 (courtesy NASA and ESA, © Bill Snyder).

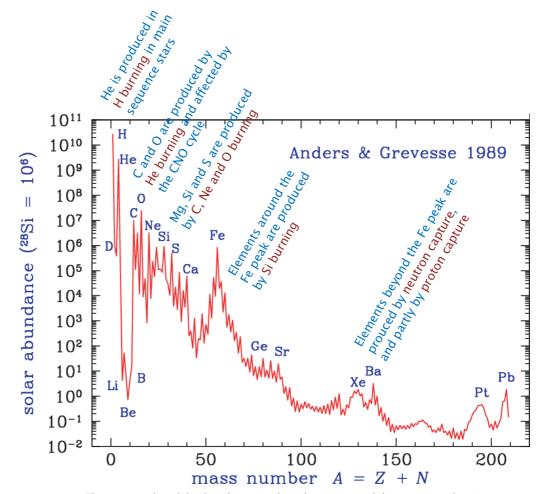


FIGURE 127 The measured nuclide abundances in the solar system and their main production processes (from Ref. 180).

Ref. 181

heavy stable nucleus, lead – from neutrons flying around. The second neutron capture process is the rapid *r-process*. For a long time, its was unknown where it occurred; for many decades, it was thought that it takes place in stellar explosions. Recent research points to *neutron star mergers* as the more likely place for the r-process. Such collisions emit material into space. The high neutron flux produces heavy elements. For example, it seems that most *gold* nuclei are synthesized in this way. (The first clear neutron star merger was observed in 2013 with the Hubble space telescope, after it had been detected as a gamma ray burst with the name GRB 130603B. Such an event is also called a *kilonova*, because the emitted energy is between that of a *nova* and of a *supernova*. In October 2017, a further, well-publicized neutron star merger was observed with the help of gravitational wave detectors, of gamma ray burst detectors and of over 70 optical telescopes. It took place at a distance of 130 million light years.) The abundances of the heavy elements in the solar system can be measured with precision, a shown in Figure 127. These data points correspond well with what is expected from the material synthesized by neutron star

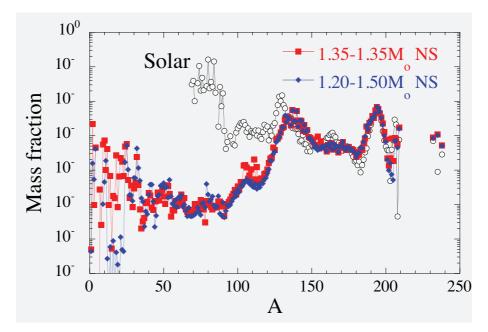


FIGURE 128 The comparison between measured nuclide abundances (dotted circles) in the solar system and the calculated values (red squares, blue diamonds) predicted by neutron star mergers (from reference Ref. 181).

mergers, the most likely candidate for the r-process at present, as illustrated by Figure 128.

A number of other processes, such as *proton capture* and the so-called *equilibrium process*, contributed to the formation of the elements.

In summary, the electrons and protons in our body were made during the big bang; the lighter nuclei, such as carbon or oxygen, in stars; the heavier nuclei in star explosions and neutron star mergers. But how did those nuclei arrive on Earth?

At a certain stage of their life, many stars explode. An exploding star is called a *supernova*. Such a supernova has an important effect: it distributes most of the matter of the star, such as carbon, nitrogen or oxygen, into space. This happens mostly in the form of neutral atoms. (Some elements are also synthesized during the explosion.) Exploding supernovae are thus essential for distributing material into space.

The Sun is a second generation star – as so-called 'population I' star. and the solar system formed from the remnants of a supernova, as did, somewhat later, life on Earth. We all are made of recycled atoms.

We are recycled stardust. This is the short summary of the extended study by astrophysicists of all the types of stars found in the universe, including their birth, growth, mergers and explosions. The exploration of how stars evolve and then move in galaxies is a fascinating research field, and many aspects are still unknown.

CURIOSITIES ABOUT THE SUN AND THE STARS

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What would happen if the Sun suddenly stopped shining? Obviously, temperatures would fall by several tens of degrees within a few hours. It would rain, and then all water would freeze. After four or five days, all animal life would stop. After a few weeks, the

oceans would freeze; after a few months, air would liquefy. Fortunately, this will never happen.

\* \*

Not everything about the Sun is known. For example, the neutrino flux from the Sun oscillates with a period of 28.4 days. That is the same period with which the magnetic field of the Sun oscillates. The connection is still being explored.

\* \*

The Sun is a fusion reactor. But its effects are numerous. If the Sun were less brighter than it is, evolution would have taken a different course. We would not have eyelids, we would still have more hair, and would have a brighter skin. Can you find more examples?

Challenge 139 e

Some stars shine like a police siren: their luminosity increases and decreases regularly. Such stars, called *Cepheids*, are important because their period depends on their average (absolute) brightness. Therefore, measuring their period and their brightness on Earth thus allows astronomers to determine their distance.

\* \*

\* \*

The first human-made hydrogen bomb explosion took place the Bikini atoll. Fortunately, none has ever been used on people.

But nature is much better at building bombs. The most powerful nuclear explosions known take place on the surface of neutron stars in X-ray binaries. The matter falling into such a neutron star from the companion star, mostly hydrogen, will heat up until the temperature allows fusion. The resulting explosions can be observed in telescopes as light or X-ray flashes of about 10 s duration; the explosions are millions of times more powerful that those of human-made hydrogen bombs.

In the 1960s, it was discovered that surface of the Sun oscillates. The surface is covered with standing waves. The amplitude is a few hundred kilometres, the wavelength can be hundred times larger; the typical frequency of the famous p-modes, or trapped acoustic waves, is between 2 and 4 mHz, thus roughly between 8 and 3 minutes. The oscillations are also visible as diameter oscillations of the Sun. This research field is now called *helioseismology*.

\* \*

Lithium, beryllium and boron are rare inside stars, because they like to capture protons, and thus change identity. For the same reason, these elements are rare on Earth.

\* \*

By chance, the composition ratios between carbon, nitrogen and oxygen inside the Sun are the same as inside the human body.

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\* \*

Nucleosynthesis is mainly regulated by the strong interaction. However, if the electromagnetic interaction would be much stronger or much weaker, stars would either produce too little oxygen or too little carbon, and we would not exist. This famous argument is due to Fred Hoyle. Can you fill in the details?

Challenge 140 d

## SUMMARY ON STARS AND NUCLEOSYNTHESIS

All humans are brothers. We came from the same supernova.

Stars and the Sun burn because of nuclear fusion. The energy liberated in nuclear fusion is due to the strong nuclear interaction that acts between nucleons. When stars have used up their nuclear fuel, they usually explode. In such a supernova explosion, they distribute nuclei into space in the form of dust. Already in the distant past, such dust recollected because of gravity and then formed the Sun, the Earth and, later on, humans.

The nuclear reaction processes behind nucleosynthesis have been studied in great detail. Nucleosynthesis during the big bang formed hydrogen and helium, nucleosynthesis in stars formed the light nuclei, and nucleosynthesis in neutron star mergers and supernovae explosions formed the heavy nuclei.



# Chapter 7 THE STRONG INTERACTION – INSIDE NUCLEI AND NUCLEONS

B oth radioactivity and medical images show that nuclei are composed systems. Ut quantum theory predicts even more: also protons and neutrons must e composed. There are two reasons: first, nucleons have a finite size, and second, their magnetic moments do not match the value predicted for point particles.

Ref. 182

Ref. 183

The prediction of components inside protons was confirmed in the late 1960s when Kendall, Friedman and Taylor shot high energy electrons into hydrogen atoms. They found that a proton contains *three* constituents with spin 1/2. The experiment was able to 'see' the constituents through large angle scattering of electrons, in the same way that we see objects through large angle scattering of photons. These constituents correspond in number and (most) properties to the so-called *quarks* predicted in 1964 by George Zweig and also by Murray Gell-Mann.\*\*

Why are there three quarks inside a proton? And how do they interact? The answers are deep and fascinating.

## The feeble side of the strong interaction

The mentioned deep inelastic scattering experiments show that the interaction keeping the protons together in a nucleus, which was first described by Yukawa Hideki,\*\*\* is

Ref. 184

Gell-Mann was the central figure of particle physics in the 20th century; he introduced the concept of strangeness, the renormalization group, the flavour SU(3) symmetry and quantum chromodynamics itself. A disturbing story is that he took the idea, the data, the knowledge, the concepts and even the name of the V–A theory of the weak interaction from the bright physics student George Sudarshan and published it, together with Richard Feynman, as his own. The wrong attribution is still found in many textbooks.

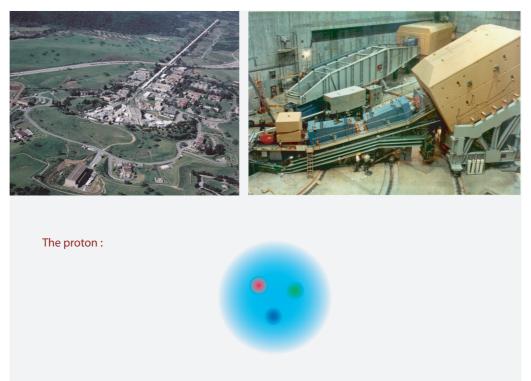
<sup>\*\*</sup> The physicist George Zweig (b. 1937 Moscow) proposed the quark idea – he called them *aces* – in 1963, with more clarity than Gell-Mann. Zweig stressed the reality of aces, whereas Gell-Mann, in the beginning, did not believe in the existence of quarks. Zweig later moved on to a more difficult field: neurobiology.

Murray Gell-Mann (b. 1929 New York ) received the Nobel Prize in Physics in 1969. He is the originator of the term 'quark'. The term has two origins: officially, it is said to be taken from *Finnegans Wake*, a novel by James Joyce; in reality, Gell-Mann took it from a Yiddish and German term meaning 'lean soft cheese' and used figuratively in those languages to mean 'silly idea'.

Gell-Mann is also known for his constant battle with Feynman about who deserved to be called the most arrogant physicist of their university. A famous anecdote is the following. Newton's once used a common saying of his time in a letter to Hooke: 'If I have seen further than you and Descartes, it is by standing upon the shoulders of giants.' Gell-Mann is known for saying: 'If I have seen further than others, it is because I am surrounded by dwarfs.'

<sup>\*\*\*</sup> Yukawa Hideki (b. 1907 Azabu, d. 1981 Kyoto), important physicist specialized in nuclear and particle physics. He received the 1949 Nobel Prize in Physics for his theory of mesons. Yukawa founded the journal

#### 7 INSIDE NUCLEI AND NUCLEONS



**FIGURE 129** Top: SLAC, the electron linear collider, and the detectors used for the deep inelastic electron scattering experiment. Bottom: an artistic illustration of the final result, showing the three scattering centres observed inside the proton.

only a feeble shadow of the interaction that keeps quarks together in a proton. Both interactions are called by the same name. The two cases correspond somewhat to the two cases of electromagnetism found in atomic matter. The clearest example is provided by neon atoms: the strongest and 'purest' aspect of electromagnetism is responsible for the attraction of the electrons to the neon nuclei; its feeble 'shadow', the Van-der-Waals interaction, is responsible for the attraction of neon atoms in liquid neon and for processes like its evaporation and condensation. Both attractions are electromagnetic, but the strengths differ markedly. Similarly, the strongest and 'purest' aspect of the strong interaction leads to the formation of the proton and the neutron through the binding of quarks; the feeble, 'shadow' aspect leads to the formation of nuclei and to a decay. Obviously, most information can be gathered by studying the strongest and 'purest' aspect.

#### BOUND MOTION, THE PARTICLE ZOO AND THE QUARK MODEL

Deep electron scattering showed that protons are made of interacting constituents. How can one study these constituents?

Physicists are simple people. To understand the constituents of matter, and of protons in particular, they had no better idea than to take all particles they could get hold of and

*Progress of Theoretical Physics* and together with his class mate Tomonaga Shin'ichiro, who also won the prize, he was an example to many scientists in Japan.



FIGURE 130 A typical experiment used to study the quark model: the Proton Synchroton at CERN in Geneva (© CERN).

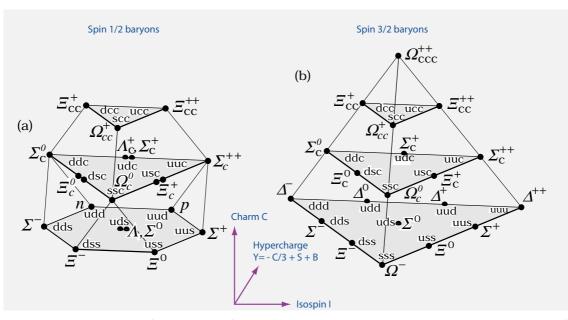


FIGURE 131 The family diagrams for the least massive baryons that can be built as qqq composites of the first four quark types (from Ref. 186).

Ref. 185 to smash them into each other. Many researchers played this game for decades. Obviously, this is a facetious comment; in fact, quantum theory forbids any other method. Challenge 141 s Can you explain why?

> Understanding the structure of particles by smashing them into each other is not simple. Imagine that you want to study how cars are built just by crashing them into

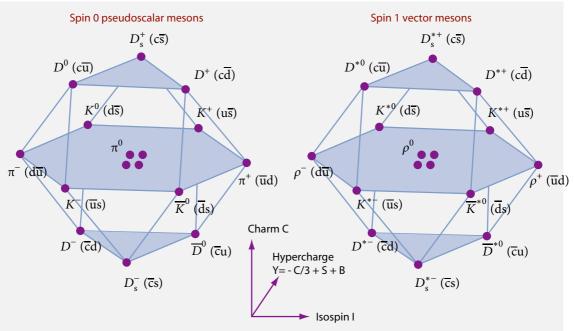


FIGURE 132 The family diagram for the least massive pseudoscalar and vector mesons that can be built as  $q\bar{q}$  composites of the first four quark flavours.

each other. Before you get a list of all components, you must perform and study a nonnegligible number of crashes. Most give the same result, and if you are looking for a particular part, you might have to wait for a long time. If the part is tightly attached to others, the crashes have to be especially energetic. In addition, the part most likely will be deformed. Compared to car crashes, quantum theory adds the possibility for debris to transform, to react, to bind and to get excited. Therefore the required diligence and patience is even greater for particle crashes than for car crashes. Despite these difficulties, for many decades, researchers have collected an ever increasing number of proton debris, also called *hadrons*. The list, a small part of which is given in Appendix B, is overwhelmingly long; the official full list, several hundred pages of fine print, is found at pdg.web. cern.ch and contains hundreds of hadrons. Hadrons come in two main types: integer spin hadrons are called *mesons*, half-integer spin hadrons are called *baryons*. The proton and the neutron themselves are thus baryons.

and the neutron themselves are thus baryons. Then came the quark model. Using the ingenuity of many experimentalists and theoreticians, the quark model explained the whole meson and baryon catalogue as a consequence of only 6 types of bound quarks. Typically, a large part of the catalogue can be structured in graphs such as the ones given in Figure 132 and Figure 131. These graphs were the beginning of the end of high energy physics. The quark model explained all quantum numbers of the debris, and allowed understanding their mass ratios as well as their decays.

The quark model explained why debris come into two types: all *mesons* consist of a quark and an antiquark and thus have integer spin; all *baryons* consist of three quarks, and thus have half-integer spin. In particular, the proton and the neutron are seen as

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QUARK	Mass m (see text)	Spin J parity P	Possible colours; possible weak be- haviour	CHARGE Q, ISOSPIN $I$ , STRANGENESS S, CHARM C, BEAUTY B', TOPNESS $T$	L E PT O N N U M B E R L, B A R Y O N N U M B E R B
Down d	4.5 to 5.5 $MeV/c^2$	$\frac{1}{2}^{+}$	red, green, blue; singlet, doublet	$-\frac{1}{3}, -\frac{1}{2}, 0, 0, 0, 0$	$0, \frac{1}{3}$
Up u	1.8 to 3.0 MeV/ $c^2$	$\frac{1}{2}^{+}$	red, green, blue; singlet, doublet	$+\frac{2}{3}, +\frac{1}{2}, 0, 0, 0, 0$	$0, \frac{1}{3}$
Strange s	$95(5)\mathrm{MeV}/c^2$	$\frac{1}{2}^{+}$	red, green, blue; singlet, doublet	$-\frac{1}{3}, 0, -1, 0, 0, 0$	$0, \frac{1}{3}$
Charm <i>c</i>	$1.275(25) \mathrm{GeV}/c^2$	$\frac{1}{2}^{+}$	red, green, blue; singlet, doublet	$+\frac{2}{3}, 0, 0, +1, 0, 0$	$0, \frac{1}{3}$
Bottom b	$4.18(3) \mathrm{GeV}/c^2$	$\frac{1}{2}^{+}$	red, green, blue; singlet, doublet	$-\frac{1}{3}, 0, 0, 0, -1, 0$	$0, \frac{1}{3}$
Top t	$173.5(1.4) \mathrm{GeV}/c^2$	$\frac{1}{2}^{+}$	red, green, blue; singlet, doublet	$+\frac{2}{3}, 0, 0, 0, 0, +1$	$0, \frac{1}{3}$

TABLE	17	The quarks.
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combinations of two quark types, called up (u) and down (d): the proton is a *uud* state, the neutron a *udd* state. The discovery of other hadrons lead to the addition of four additional types of quarks. The quark names are somewhat confusing: they are called *strange* (s), *charm* (c), *bottom* (b) – also called 'beauty' in the old days – and *top* (t) – called 'truth' in the past. The quark types are called *flavours*; in total, there are thus 6 quark flavours in nature.

All quarks have spin one half; they are fermions. Their electric charges are multiples of 1/3 of the electron charge. In addition, quarks carry a strong charge, called, again confusingly, *colour*. In contrast to electromagnetism, which has only positive, negative, and neutral charges, the strong interaction has red, blue, green quarks on one side, and anti-red, anti-blue and anti-green on the other. The neutral state is called 'white'. All baryons, including proton and neutrons, and all mesons are white, in the same way that all atoms are neutral.

## The essence of quantum chromodynamics

Ref. 187

The theory describing the bound states of quarks is called *quantum chromodynamics*, or QCD. It was formulated in its final form in 1973 by Fritzsch, Gell-Mann and Leutwyler. In the same way that in atoms, electrons and protons are held together by the exchange of

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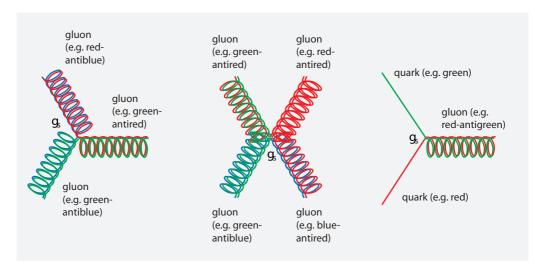


FIGURE 133 The essence of the QCD Lagrangian: the Feynman diagrams of the strong interaction.

virtual photons, in protons, quarks are held together by the exchange of virtual gluons. *Gluons* are the quanta of the strong interaction, and correspond to photons, the quanta of the electromagnetic interactions.

Ref. 188

Quantum chromodynamics describes all motion due to the strong interaction with the three fundamental processes shown in Figure 133: two gluons can scatter, a gluon can emit or absorb another, and a quark can emit or absorb a gluon. In electrodynamics, only the last diagram is possible; in the strong interaction, the first two appear as well. Among others, the first two diagrams are responsible for the confinement of quarks, and thus for the lack of free quarks in nature.

QCD is a *gauge* theory: the fields of the strong interaction show gauge invariance under the Lie group SU(3). We recall that in the case of electrodynamics, the gauge group is U(1), and Abelian, or commutative. In contrast, SU(3) is non-Abelian; QCD is a non-Abelian gauge theory. Non-Abelian gauge theory was invented and popularized by Wolfgang Pauli. It is often incorrectly called *Yang–Mills theory* after the first two physicists who wrote down Pauli's ideas.

Due to the SU(3) gauge symmetry, there are 8 gluons; they are called red-antigreen, blue-antired, etc. Since SU(3) is non-Abelian, gluons interact among themselves, as shown in the first two processes in Figure 133. Out of the three combinations red-antired, blue-antiblue and green-antigreen, only two gluons are linearly independent, thus giving a total of  $3^2 - 1 = 8$  gluons.

The coupling strength of the strong interaction, its three fundamental processes in Figure 133, together with its SU(3) gauge symmetry and the observed number of six quarks, completely determine the behaviour of the strong interaction. In particular, they completely determine its Lagrangian density.

#### THE LAGRANGIAN OF QUANTUM CHROMODYNAMICS\*

The Lagrangian density of the strong interaction can be seen as a complicated formulation of the Feynman diagrams of Figure 133. Indeed, the Lagrangian density of quantum chromodynamics is

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} F^{(a)}_{\mu\nu} F^{(a)\mu\nu} - c^2 \sum_q m_q \overline{\psi}^k_q \psi_{qk} + i\hbar c \sum_q \overline{\psi}^k_q \gamma^\mu (D_\mu)_{kl} \psi^l_q$$
(71)

where the gluon field strength and the gauge covariant derivative are

$$\begin{split} F^{(a)}_{\mu\nu} &= \partial_{\mu}A^{a}_{\nu} - \partial_{\nu}A^{a}_{\mu} + g_{\rm s}f_{abc}A^{b}_{\mu}A^{b}_{\nu} \\ (D_{\mu})_{kl} &= \delta_{kl}\partial_{\mu} - i\frac{g_{\rm s}}{2}\sum_{a}\lambda^{a}_{k,l}A^{a}_{\mu} \; . \end{split}$$

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We remember from the section on the principle of least action that Lagrangians are always sums of scalar products; this is clearly seen in expression (71). The index a = 1...8numbers the eight types of gluons and the index k = 1, 2, 3 numbers the three colours, all due to SU(3). The index q = 1...6 numbers the six quark flavours. The fields  $A_{\mu}^{a}(x)$  are the eight gluon fields, represented by the coiled lines in Figure 133. The fields  $\psi_{q}^{k}(x)$  are those of the quarks of flavour q and colour k, represented by the straight line in the figure. The six times three quark fields, like those of any elementary fermion, are 4-component Dirac spinors with masses  $m_{q}$ .\*\*

The Lagrangian (71) is that of a *local* field theory: observables are functions of position. In other words, QCD is similar to quantum electrodynamics and can be compared to experiment in the same way.

The first term of the Lagrangian (71) represents the kinetic energy of the radiation (the gluons), the second or mass term the kinetic energy of the matter particles (the quarks) and the third term the interaction between the two.

The mass term in the Lagrangian is the only term that spoils or *breaks flavour symmetry*, i.e., the symmetry under exchange of quark types. (In particle physics, this symmetry is also called *chiral symmetry*, for historical reasons.) Obviously, the mass term also breaks space-time conformal symmetry.

The interaction term in the Lagrangian thus corresponds to the third diagram in Figure 133. The strength of the strong interaction is described by the *strong coupling constant*  $g_s$ . The constant is independent of flavour and colour, as observed in experiment. The Interaction term does not mix different quarks; as observed in experiments, flavour is conserved in the strong interaction, as is baryon number. The strong interaction also conserves spatial parity P and charge conjugation parity C. The strong interaction does not transform matter.

Yo

$$= \begin{pmatrix} I & 0\\ 0 & -I \end{pmatrix} \text{ and } \gamma_n = \begin{pmatrix} 0 & \sigma^i\\ -\sigma^i & 0 \end{pmatrix} \text{ for } n = 1, 2, 3$$
(72)

Vol. IV, page 231 where the  $\sigma^i$  are the Pauli spin matrices.

<sup>\*</sup> This section can be skipped at first reading.

<sup>\*\*</sup> In their simplest form, the matrices  $\gamma_{\mu}$  can be written as

#### **7 INSIDE NUCLEI AND NUCLEONS**

Challenge 142 ny

Page 362

In QCD, the eight gluons are massless; also this property is taken from experiment. Therefore no gluon mass term appears in the Lagrangian. It is easy to see that massive gluons would spoil gauge invariance. As mentioned above, in contrast to electromagnetism, where the gauge group U(1) is Abelian, the gauge group SU(3) of the strong interactions is non-Abelian. As a consequence, the colour field itself is charged, i.e., carries colour, and thus the index *a* appears on the fields *A* and *F*. As a result, gluons can interact with each other, in contrast to photons, which pass each other undisturbed. The first two diagrams of Figure 133 are thus reflected in the somewhat complicated definition of the field  $F_{\mu\nu}^{(a)}$ . In contrast to electrodynamics, the definition has an extra term that is *quadratic* in the fields *A*; it is described by the so-called structure constants  $f_{abc}$  and the interaction strength  $g_s$ . The numbers  $f_{abc}$  are the structure constants of the SU(3).

The behaviour of the gauge transformations and of the gluon field is described by the eight matrices  $\lambda_{k,l}^a$ . They are a fundamental, 3-dimensional representation of the *generators* of the SU(3) algebra and correspond to the eight gluon types. The matrices  $\lambda_a$ , a = 1...8, and the structure constants  $f_{abc}$  obey the relations

$$[\lambda_a, \lambda_b] = 2if_{abc}\lambda_c$$
  
$$\{\lambda_a, \lambda_b\} = 4/3\delta_{ab}I + 2d_{abc}\lambda_c$$
(73)

where *I* is the unit matrix. The structure constants  $f_{abc}$  of SU(3), which are odd under permutation of any pair of indices, and  $d_{abc}$ , which are even, have the values

abc	$f_{abc}$	abc	d <sub>abc</sub>	abc	$d_{abc}$	
123	1	118	$1/\sqrt{3}$	355	1/2	
147	1/2	146	1/2	366	-1/2	
156	-1/2	157	1/2	377	-1/2	
246	1/2	228	$1/\sqrt{3}$	448	$-1/(2\sqrt{3})$	(74)
257	1/2	247	-1/2	558	$-1/(2\sqrt{3})$	
345	1/2	256	1/2	668	$-1/(2\sqrt{3})$	
367	-1/2	338	$1/\sqrt{3}$	778	$-1/(2\sqrt{3})$	
458	$\sqrt{3}/2$	344	1/2	888	$-1/\sqrt{3}$	
678	$\sqrt{3}/2$					

All other elements vanish. Physically, the structure constants of SU(3) describe the details of the interaction between quarks and gluons and of the interaction between the gluons themselves.

A fundamental 3-dimensional representation of the eight generators  $\lambda_a$  – correspond-

ing to the eight gluon types - is given, for example, by the set of the Gell-Mann matrices

$$\begin{split} \lambda_{1} &= \begin{pmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \lambda_{2} = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \lambda_{3} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \\ \lambda_{4} &= \begin{pmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 1 & 0 & 0 \end{pmatrix} \lambda_{5} = \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & 0 \\ i & 0 & 0 \end{pmatrix} \lambda_{6} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \\ \lambda_{7} &= \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix} \lambda_{8} = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix} . \quad (75)$$

There are eight matrices, one for each gluon type, with  $3 \times 3$  elements, due to the 3 colours of the strong interaction. There is no ninth gluon, because that gluon would be colourless, or 'white'.

The Lagrangian is complete only when the 6 quark masses and the coupling constant  $g_s$  are included. These values, like the symmetry group SU(3), are not explained by QCD, of course.

Only quarks and gluons appear in the Lagrangian of QCD, because only quarks and gluons interact via the strong force. This can be also expressed by saying that only quarks and gluons carry colour; *colour* is the source of the strong force in the same way that electric charge is the source of the electromagnetic field. In the same way as electric charge, colour charge is *conserved* in all interactions. Electric charge comes in two types, positive and negative; in contrast, colour comes in three types, called *red*, *green* and *blue*. The neutral state, with no colour charge, is called *white*. Protons and neutrons, but also electrons or neutrinos, are thus 'white', thus *neutral* for the strong interaction.

In summary, the six quark types interact by exchanging eight gluon types. The interaction is described by the Feynman diagrams of Figure 133, or, equivalently, by the Lagrangian (71). Both descriptions follow from the requirements that the gauge group is SU(3) and that the masses and coupling constants are given. It was a huge amount of work to confirm that all experiments indeed agree with the QCD Lagrangian; various competing descriptions were discarded.

## Experimental consequences of the quark model

How can we pretend that quarks and gluons exist, even though they are never found alone? There are a number of arguments in favour.

\* \*

The quark model explains the non-vanishing magnetic moment of the neutron and explains the magnetic moments  $\mu$  of the baryons. By describing the proton as a *uud* state and the neutron a *udd* state with no orbital angular momentum and using the precise wave functions, we get

$$\mu_u = \frac{1}{5}(4\mu_p + \mu_n)$$
 and  $\mu_d = \frac{1}{5}(4\mu_n + \mu_p)$ . (76)

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Assuming that  $m_u = m_d$  and that the quark magnetic moment is proportional to their charge, the quark model predicts a ratio of the magnetic moments of the proton and the neutron of

$$\frac{\mu_p}{\mu_n} = -\frac{3}{2} \,. \tag{77}$$

This prediction differs from measurements only by 3 %. Furthermore, using the same values for the magnetic moment of the quarks, magnetic moment values of over half a dozen of other baryons can be predicted. The results typically deviate from measurements only by around 10 %. In particular, the sign of the resulting baryon magnetic moment is always correctly calculated.

\* \*

The quark model describes all *quantum numbers* of mesons and baryons. P-parity, Cparity, and the absence of certain meson parities are all reproduced. The observed conservation of electric charge, baryon number, isospin, strangeness etc. is reproduced. Hadron family diagrams such as those shown in Figure 131 and in Figure 132 describe all existing hadron states (of lowest angular momentum) *completely*; the states not listed are not observed. The quark model thus produces a complete and correct classification of all hadrons as bound states of quarks.

The quark model also explains the *mass spectrum* of hadrons. The best predictions are made by QCD lattice calculations. With months of computer time, researchers were able to reproduce the masses of proton and neutron to within a few per cent. Interestingly, if one sets the u and d quark masses to zero, the resulting proton and neutron mass differ from experimental values only by 10%. The mass of protons and neutrons is almost completely due to the binding, not to the constituents. More details are given below.

\* \*

The number of colours of quarks must be taken into account to get correspondence of theory and calculation. For example, the measured decay time of the neutral pion is 83 as. The calculation without colour gives 750 as; if each quark is assumed to appear in 3 colours the value must be divided by 9, and then matches the measurement.

In particle colliders, collisions of electrons and positrons sometimes lead to the production of hadrons. The calculated production rates also fit experiments only if quarks have three colours. In more detail, if one compares the ratio of muon–antimuon production and of hadron production, a simple estimate relates them to their charges:

$$R = \frac{\sum q_{\text{hadrons}}}{\sum q_{\text{muons}}}$$
(78)

Between 2 and 4 GeV, when only three quarks can appear, this argument thus predicts R = 2 if colours exist, or R = 2/3 if they don't. Experiments yield a value of R = 2.2, thus

Ref. 189 Ref. 190 Page 234

Challenge 144 s

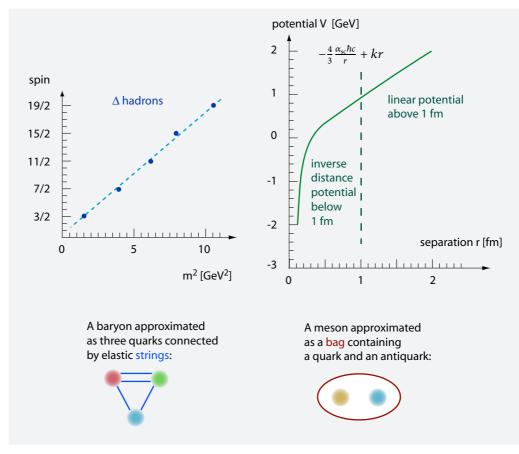


FIGURE 134 Top left: a Regge trajectory, or Chew–Frautschi plot, due to the confinement of quarks. Top right: the quark confinement potential. Bottom: two approximate ways to describe quark confinement: the string model and the bag model of hadrons.

confirming the number of colours. Many other such *branching ratios* can be calculated in this way. They agree with experiments only if the number of colours is three.

### CONFINEMENT OF QUARKS - AND ELEPHANTS

Many of the observed hadrons are not part of the diagrams of Figure 131 and Figure 132; these additional hadrons can be explained as *rotational excitations* of the fundamental mesons from those diagrams. As shown by Tullio Regge in 1957, the idea of rotational excitations leads to quantitative predictions. Regge assumed that mesons and baryons are quarks connected by strings, like rubber bands – illustrated in Figure 134 and Figure 135 – and that the force or tension k between the quarks is thus constant over distance.

We assume that the strings, whose length we call  $2r_0$ , rotate around their centre of mass as rapidly as possible, as shown in Figure 135. Then we have

$$v(r) = c \frac{r}{r_0} . \tag{79}$$

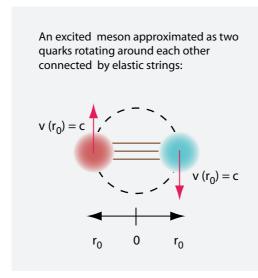


FIGURE 135 Calculating masses of excited hadrons.

The quark masses are assumed negligible. For the total energy this implies the relation

$$E = c^{2}m = 2 \int_{0}^{r_{0}} \frac{k}{\sqrt{1 - v(r)/c^{2}}} dr = kr_{0}\pi$$
(80)

and for angular momentum the relation

$$J = \frac{2}{\hbar c^2} \int_0^{r_0} \frac{k r v(r)}{\sqrt{1 - v(r)/c^2}} dr = \frac{k r_0^2}{2\hbar c} .$$
(81)

Including the spin of the quarks, we thus get

$$J = \alpha_0 + \alpha' m^2$$
 where  $\alpha' = \frac{c^3}{2\pi k\hbar}$ . (82)

Regge thus deduced a simple expression that relates the mass *m* of excited hadrons to their total spin *J*. For bizarre historical reasons, this relation is called a *Regge trajectory*.

The value of the constant  $\alpha'$  is predicted to be independent of the quark–antiquark pairing. A few years later, as shown in Figure 134, such linear relations were found in experiments: the *Chew-Frautschi plots*. For example, the three lowest lying states of  $\Delta$  are the spin 3/2  $\Delta(1232)$  with  $m^2$  of 1.5 GeV<sup>2</sup>, the spin 7/2  $\Delta(1950)$  with  $m^2$  of 3.8 GeV<sup>2</sup>, and the spin 11/2  $\Delta(2420)$  with  $m^2$  of 5.9 GeV<sup>2</sup>. The value of the constant  $\alpha'$  is found experimentally to be around 0.93 GeV<sup>-2</sup> for almost all mesons and baryons, whereas the value for  $\alpha_0$  varies from particle to particle. The quark string tension is thus found to be

Ref. 188

$$k = 0.87 \,\text{GeV/fm} = 0.14 \,\text{MN}$$
 (83)

In other words, two quarks in a hadron attract each other with a force equal to the weight of two elephants: about 14 tons.

Experiments are thus clear: the observed Chew-Frautschi plots, as well as several other observations not discussed here, are best described by a quark-quark potential that grows, above 1 fm, *linearly* with distance. The slope of the linear potential, the force, has a value equal to the force with which the Earth attracts two elephants. As a result, quarks *never* appear as free particles: quarks are always *confined* in hadrons. This situation is in contrast with QED, where the force between charges goes to zero for large distances; electric charges are thus not confined, but can exist as free particles. At large distances, the electric potential *decreases* in the well-known way, with the inverse of the distance. In contrast, for the strong interaction, experiments lead to a quark potential given by

Ref. 185

$$V = -\frac{4}{3}\frac{\alpha_{\rm sc}\hbar c}{r} + kr \tag{84}$$

where k is the mentioned 0.87 GeV/fm,  $\alpha_{sc}$  is 0.2, and  $\hbar c$  is 0.1975 GeV/fm. The quark potential is illustrated in Figure 134.

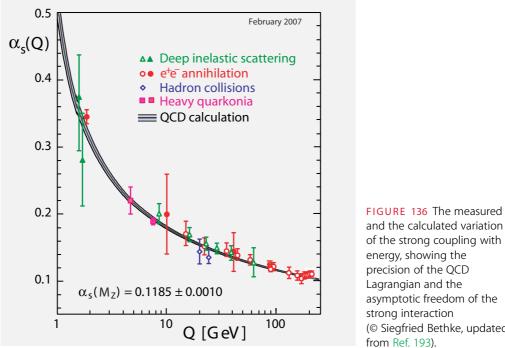
Even though experiments are clear, theoreticians face a problem. So far, neither the quark-quark potential nor the quark bound states can be deduced from the QCD Lagrangian with a simple approximation method. Nevertheless, complicated nonperturbative calculations show that the QCD Lagrangian does predict a force between two coloured particles that levels off at a constant value (corresponding to a linearly increasing potential). These calculations show that the old empirical approximations of hadrons as quarks connected by strings or a quarks in bags, shown in Figure 134, can indeed be deduced from the QCD Lagrangian. However, the calculations are too complex to be summarized in a few lines. Independently, the constant force value has also been reproduced in computer calculations in which one simplifies space-time to a lattice and then approximates QCD by so-called *lattice QCD* or *lattice gauge theory*. Lattice calculations have further reproduced the masses of most mesons and baryons with reasonable accuracy. Using the most powerful computers available, these calculations have given predictions of the mass of the proton and other baryons within a few per cent. Discussing these complex and fascinating calculations lies outside the scope of this text, however.

Ref. 192

In fact, the challenge of explaining confinement in simple terms is so difficult that the brightest minds have been unable to solve it yet. This is not a surprise, as its solution probably requires the unification of the interactions and, most probably, also the unification with gravity. We therefore leave this issue for the last part of our adventure.

### Asymptotic freedom

QCD has another property that sets it apart form QED: the behaviour of its coupling with energy. In fact, there are three equivalent ways to describe the strong coupling strength. The first way is the quantity appearing in the QCD Lagrangian,  $g_s$ . The second way is often used to define the equivalent quantity  $\alpha_s = g_s^2/4\pi$ . Both  $\alpha_s$  and  $g_s$  depend on the energy Q of the experiment. If they are known for one energy, they are known for all of them. Presently, the best experimental value is  $\alpha_s(M_Z) = 0.1185 \pm 0.0010$ .



of the strong coupling with energy, showing the precision of the QCD Lagrangian and the asymptotic freedom of the strong interaction (© Siegfried Bethke, updated

Ref. 186, Ref. 188

The energy dependence of the strong coupling can be calculated with the standard renormalization procedures and is expected to be

$$\alpha_s(Q^2) = \frac{12\pi}{33 - 2n_f} \frac{1}{L} \left( 1 - \frac{(918 - 114n_f)\ln L}{(33 - 2n_f)^2 L} + \dots \right) \quad \text{where} \quad L = \ln \frac{Q^2}{\Lambda^2(n_f)} \tag{85}$$

where  $n_f$  is the number of quarks with mass below the energy scale Q, thus a number between 3 and 6. (The expression has been expanded to many additional terms with the help of computer algebra.)

The third way to describe the strong coupling is thus the energy parameter  $\Lambda(n_f)$ . Experiments yield  $\Lambda(3) = 230(60) \text{ GeV}$ ,  $\Lambda(4) = 180(50) \text{ GeV}$  and  $\Lambda(5) = 120(30) \text{ GeV}$ .

The accelerator experiments that measure the coupling are extremely involved, and hundreds of people across the world have worked for many years to gather the relevant data. The comparison of QCD and experiment, shown in Figure 136, does not show any contradiction between the two.

Figure 136 and expression (85) illustrate what is called *asymptotic freedom*:  $\alpha_s$  decreases at high energies. In other words, at high energies quarks are *freed* from the strong interaction; they behave as free particles.\* As a result of asymptotic freedom, in QCD, a perturbation expansion can be used only at energies much larger than  $\Lambda$ . Historically,

<sup>\*</sup> Asymptotic freedom was discovered in 1972 by Gerard 't Hooft; since he had received the Nobel Prize already, the 2004 Prize was then given to the next people who highlighted it: David Gross, David Politzer and Frank Wilczek, who studied it extensively in 1973.

the discovery of asymptotic freedom was essential to establish QCD as a theory of the strong interaction.

Asymptotic freedom can be understood qualitatively if the situation is compared to QED. The electron coupling increases at small distances, because the screening due to the virtual electron-positron pairs has less and less effect. In QCD, the effective colour coupling also changes at small distances, due to the smaller number of virtual quark-antiquark pairs. However, the gluon properties lead to the opposite effect, an *antiscreening* that is even stronger: in total, the effective strong coupling decreases at small distances.

# THE SIZES AND MASSES OF QUARKS

The size of quarks, like that of all elementary particles, is predicted to vanish by QCD, as in all quantum field theory. So far, no experiment has found any effect due to a finite quark size. Measurements show that quarks are surely smaller than  $10^{-19}$  m. No size conjecture has been given by any hypothetical theory. Quarks are assumed point-like, or at most Planck-sized, in all descriptions so far.

We noted in several places that a neutral compound of charged particles is always less massive than its components. But if you look up the mass values for quarks in most tables, the masses of u and d quarks are only of the order of a few MeV/ $c^2$ , whereas the proton's mass is 938 MeV/ $c^2$ . What is the story here?

It turns out that the definition of the mass is more involved for quarks than for other particles. Quarks are never found as free particles, but only in bound states. As a result, the concept of quark mass depends on the calculation framework one is using.

Due to *asymptotic freedom*, quarks behave almost like free particles only at high energies. The mass of such a 'free' quark is called the *current quark mass*; for the light quarks it is only a few MeV/ $c^2$ , as shown in Table 17.

At low energy, for example inside a proton, quarks are *not* free, but must carry along a large amount of energy due to the confinement process. As a result, bound quarks have a much larger effective, so-called *constituent quark mass*, which takes into account this confinement energy. To give an idea of the values, take a proton; the indeterminacy relation for a particle inside a sphere of radius 0.9 fm gives a momentum indeterminacy of around 190 MeV/c. In three dimensions this gives an energy of  $\sqrt{3}$  times that value, or an effective, constituent quark mass of about 330 MeV/c<sup>2</sup>. Three confined quarks are thus heavier than a proton, whose mass is 938 MeV/c<sup>2</sup>; we can thus still say that a compound proton is less massive than its constituents.

Ref. 195

Ref. 186

Ref 194

In short, the mass of the proton and the neutron is (almost exclusively) the kinetic energy of the quarks inside them, as their rest mass is almost negligible. As Frank Wilczek says, some people put on weight even though they never eat anything heavy.

But also the small current quark mass values for the up, down, strange and charmed quarks that appear in the QCD Lagrangian depend on the calculation framework that is used. The values of Table 17 are those for a renormalization scale of 2 GeV. For half that energy, the mass values increase by 35 %. The heavy quark masses are those used in the so-called  $\overline{MS}$  scheme, a particular way to perform perturbation expansions.

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## 7 INSIDE NUCLEI AND NUCLEONS

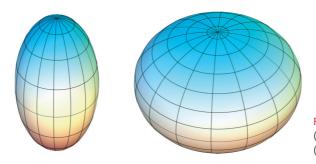


FIGURE 137 An illustration of a prolate (left) and an oblate (right) ellipsoidal shape (© Sam Derbyshire).

## THE MASS, SHAPE AND COLOUR OF PROTONS

- Ref. 195
- Frank Wilczek mentions that one of the main results of QCD, the theory of strong interactions, is to explain mass relations such as

$$m_{\text{proton}} \sim e^{-k/\alpha} m_{\text{Planck}}$$
 and  $k = 11/2\pi$ ,  $\alpha_{\text{unif}} = 1/25$ . (86)

Here, the value of the coupling constant  $\alpha_{unif}$  is taken at the grand unifying energy, a factor of 1000 below the Planck energy. (See the section of grand unification below.) In other words, a general understanding of masses of bound states of the strong interaction, such as the proton, requires almost purely a knowledge of the unification energy and the coupling constant at that energy. The approximate value  $\alpha_{unif} = 1/25$  is an extrapolation from the low energy value, using experimental data. The proportionality factor k in expression (86) is not easy to calculate. It is usually determined on computers using lattice QCD.

But the mass is not the only property of the proton. Being a cloud of quarks and gluons, it also has a shape. Surprisingly, it took a long time before people started to become interested in this aspect. The proton, being made of two up quarks and one down quark, resembles a ionized  $H_2^+$  molecule, where one electron forms a cloud around two protons. Obviously, the  $H_2^+$  molecule is elongated, or *prolate*, as shown in Figure 137.

Ref. 196

Ref. 197

Is the proton prolate? There is no spectroscopically measurable asphericity – or quadrupole moment – of the proton. However, the proton has an *intrinsic* quadrupole moment. The quadrupole moments of the proton and of the neutron are predicted to be positive in all known calculation methods, implying an *prolate* shape. Recent measurements at Jefferson Laboratories confirm this prediction. A prolate shape is predicted for all J = 1/2 baryons, in contrast to the oblate shape predicted for the J = 3/2 baryons. The spin 0 pseudoscalar mesons are predicted to be prolate, whereas the spin 1 vector mesons are expected to be oblate.

The shape of any molecule will depend on whether other molecules surround it. Recent research showed that similarly, both the size and the shape of the proton in nuclei is slightly variable; both seem to depend on the nucleus in which the proton is built-in.

Apart from shapes, molecules also have a colour. The colour of a molecule, like that of any object, is due to the energy absorbed when it is irradiated. For example, the  $H_2^+$ molecule can absorb certain light frequencies by changing to an excited state. Molecules change mass when they absorb light; the excited state is heavier than the ground state.

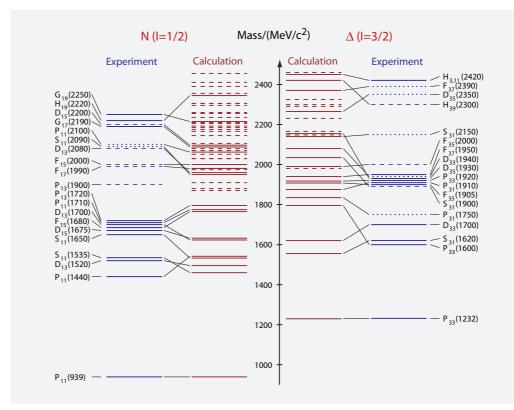


FIGURE 138 The mass spectrum of the excited states of the proton: experimental and calculated values (from Ref. 186).

Ref. 186

In the same way, protons and neutrons can be excited. In fact, their excited states have been studied in detail; a summary, also showing the limitation of the approach, is shown in Figure 138. Many excitations can be explained as excited quarks states, but many more are predicted. The calculated masses agree with observations to within 10 %. The quark model and QCD thus structure and explain a large part of the baryon spectrum; but the agreement is not yet perfect.

Obviously, in our everyday environment the energies necessary to excite nucleons do not appear – in fact, they do not even appear inside the Sun – and these excited states can be neglected. They only appear in particle accelerators and in cosmic rays. In a sense, we can say that in our corner of the universe, the colour of protons usually is not visible.

## Curiosities about the strong interaction

In a well-known analogy, QCD can be compared to superconductivity. Table 18 gives an overview of the correspondence.

\* \*

The computer calculations necessary to extract particle data from the Lagrangian of quantum chromodynamics are among the most complex calculations ever performed. They beat weather forecasts, fluid simulations and the like by orders of magnitude.

#### 7 INSIDE NUCLEI AND NUCLEONS

TABLE 18 Correspondence between QCD and superconductivity.

QCD	Superconductivity
Quark	magnetic monopole
Colour force non-linearities	Electron-lattice interaction
Chromoelectric flux tube	magnetic flux tube
Gluon-gluon attraction	electron-electron attraction
Glueballs	Cooper pairs
Instability of bare vacuum	instability of bare Fermi surface
Discrete centre symmetry	continuous U(1) symmetry
High temperature breaks symmetry	low temperature breaks symmetry

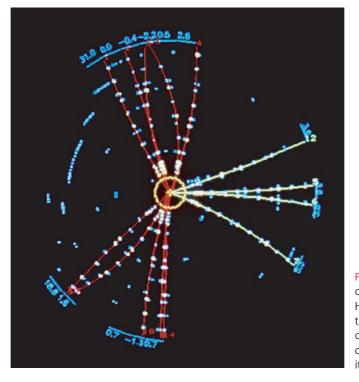


FIGURE 139 A three jet event observed at the PETRA collider in Hamburg in Germany. The event, triggered by an electron-positron collision, allowed detecting the decay of a gluon and measuring its spin (© DESY).

Nobody knows whether this will be necessary also in the future: the race for a simple approximation method for finding solutions is still open.

\* \*

Even though gluons are massless, like photons and gravitons are, there is *no* colour radiation in nature. Gluons carry colour and couple to themselves; as a result, free gluons were predicted to directly decay into quark–antiquark pairs.

In 1979, the first clear decays of *gluons* have been observed at the PETRA particle collider in Hamburg. The occurrence of certain events, called *gluon jets*, are due to the decay of high-energy gluons into narrow beams of particles. Gluon jets appear in coplanar

Ref. 191

three-jet events. The observed rate and the other properties of these events confirmed the predictions of QCD. Experiments at PETRA also determined the spin S = 1 of the gluon and the running of the strong coupling constant. The hero of those times was the project manager Gustav-Adolf Voss, who completed the accelerator on budget and six months ahead of schedule.

\*

Something similar to colour radiation, but still stranger, might have been found in 1997. It might be that a scalar meson with a mass of  $1.5 \text{ GeV/c}^2$  is a *glueball*. This is a hypothetical meson composed of gluons only. Numerical results from lattice gauge theory seem to confirm the possibility of a glueball in that mass range. The existence of glueballs is hotly debated and still open.

Ref. 198

There is a growing consensus that most light scalar mesons below  $1 \text{ GeV}/c^2$ , are *tetraquarks*. In 2003, experiments provided also candidates for heavier tetraquarks, namely the X(3872), Ds(2317) and Ds(2460). The coming years will show whether this interpretation is correct.

\* \*

Do particles made of five quarks, so-called *pentaquarks*, exist? So far, they seem to exist only in a few laboratories in Japan, whereas in other laboratories across the world they are not seen. Most researchers do not believe the results any more.

\* \*

Whenever we look at a periodic table of the elements, we look at a manifestation of the strong interaction. The Lagrangian of the strong interaction describes the origin and properties of the presently known 115 elements.

Nevertheless one central aspect of nuclei is determined by the electromagnetic interaction. Why are there around 115 different elements? Because the electromagnetic coupling constant  $\alpha$  is around 1/137.036. In more detail, the answer is the following. If the charge of a nucleus were much higher than around 137, the electric field around nuclei would lead to spontaneous electron–positron pair generation; the generated electron would fall into the nucleus and transform one proton into a neutron, thus inhibiting a larger proton number. The finite number of the elements is thus due to the electromagnetic interaction.

To know more about radioactivity, its effects, its dangers and what a government can do about it, see the English and German language site of the Federal Office for Radiation Protection at www.bfs.de.

\* \*

\* \*

From the years 1990 onwards, it has regularly been claimed that extremely poor countries Challenge 145 s are building nuclear weapons. Why is this highly unlikely?

Ref. 199

Ref. 200

Historically, nuclear reactions provided the first test of the relation  $E = c^2 \gamma m$ . This was achieved in 1932 by Cockcroft and Walton. They showed that by shooting protons into lithium one gets the reaction

\* \*

$${}^{7}_{3}\text{Li} + {}^{1}_{1}\text{H} \rightarrow {}^{8}_{4}\text{Be} \rightarrow {}^{4}_{2}\text{He} + {}^{4}_{2}\text{He} + 17 \text{ MeV}$$
 (87)

The measured energy on the right is exactly the same value that is derived from the differences in total mass of the nuclei on both sides.

\* \*

A large fraction of researchers say that QCD is defined by *two* parameters. Apart from the coupling constant, they count also the strong CP parameter. Indeed, it might be that the strong interaction violates CP invariance. This violation would be described by a second term in the Lagrangian; its strength would be described by a second parameter, a phase usually called  $\theta_{CP}$ . However, many high-precision experiments have been performed to search for this effect, and no CP violation in the strong interaction has ever been detected.

## A summary of QCD and its open issues

Quantum chromodynamics, the non-Abelian gauge theory based on the Lagrangian with SU(3) symmetry, describes the properties of gluons and quarks, the properties of the proton, the neutron and all other hadrons, the properties of atomic nuclei, the working of the stars and the origin of the atoms inside us and around us. Without the strong interaction, we would not have flesh and blood. And all these aspects of nature follow from a single number, the strong coupling constant, and the SU(3) gauge symmetry.

The strong interaction acts only on quarks and gluons. It conserves particle type, colour, electric charge, weak charge, spin, as well as C, P and T parity.

QCD and experiment agree wherever comparisons have been made. QCD is a perfect description of the strong interaction. The limitations of QCD are only conceptual. Like in all of quantum field theory, also in the case of QCD the mathematical form of the Lagrangian is almost uniquely defined by requiring renormalizability, Lorentz invariance and gauge invariance – SU(3) in this case. We say 'almost', because the Lagrangian, despite describing correctly all experiments, contains a few parameters that remain unexplained:

- The number, 6, and the masses  $m_a$  of the quarks are not explained by QCD.
- The coupling constant of the strong interaction  $g_s$ , or equivalently,  $\alpha_s$  or Λ, is unexplained. QCD predicts its energy dependence, but not its absolute value.
- Experimentally, the strong interaction is found to be CP conserving. This is not obvious; the QCD Lagrangian assumes that any possible CP-violating term vanishes, even though there exist CP-violating Lagrangian terms that are Lorentz-invariant, gauge-invariant and renormalizable.
- The properties of space-time, in particular its Lorentz invariance, its continuity and the number of its dimensions are assumed from the outset and are obviously all unexplained in QCD.

 It is also not known how QCD has to be modified in strong gravity, thus in strongly curved space-time.

We will explore ways to overcome these limits in the last part of our adventure. Before we do that, we have a look at the other nuclear interaction observed in nature.



# CHAPTER 8 THE WEAK NUCLEAR INTERACTION AND THE HANDEDNESS OF NATURE

The weirdest interaction in nature is the weak interaction. The weak interaction ransforms elementary particles into each other, has radiation particles hat have mass, violates parity and treats right and left differently. Fortunately, we do not experience the weak interaction in our everyday life, as its properties violate much of what we normally experience. This contrast makes the weak interaction the most fascinating of the four interactions in nature.

#### TRANSFORMATION OF ELEMENTARY PARTICLES

Radioactivity, in particular the so-called  $\beta$  decay, is a bizarre phenomenon. Experiments in the 1910s showed that when  $\beta$  sources emit electrons, atoms are *transformed* from one chemical element to another. For example, experiments such as those of Figure 140 show that tritium, an isotope of hydrogen, decays into helium as

$${}_{1}^{3}\text{H} \rightarrow {}_{2}^{3}\text{He} + e^{-} + \overline{\nu}_{e} . \tag{88}$$

In fact, new elements appear in all  $\beta$  decays. In the 1930s it became clear that the transformation process is due to a neutron in the nucleus changing into a proton (and more):

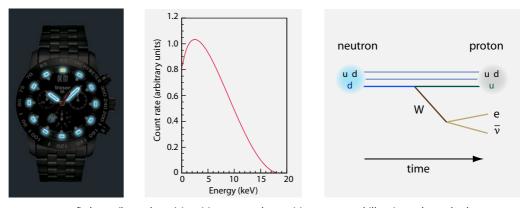
$$n \to p + e^- + \overline{\nu}_e \,. \tag{89}$$

This reaction explains all  $\beta$  decays. In the 1960s, the quark model showed that  $\beta$  decay is in fact due to a down quark changing to an up quark:

$$d \to u + e^- + \overline{\nu}_e . \tag{90}$$

This reaction explains the transformation of a neutron – a *udd* state – into a proton – a *uud* state. In short, matter particles can transform into each other. We note that this transformation differs from what occurs in other nuclear processes. In fusion, fission or a decay, even though nuclei change, every neutron and every proton retains its nature. In  $\beta$  decay, elementary particles are not immutable. The dream of Democritus and Leucippus about immutable basic building blocks is definitely *not* realized in nature.

Experiments show that quark transformations cannot be achieved with the help of electromagnetic fields, nor with the help of gluon fields, nor with the help of gravitation. There must be another type of radiation in nature, and thus another, fourth in-



**FIGURE** 140  $\beta$  decay (beta decay) in tritium: a modern, tritium-powered illuminated watch, the measured continuous energy spectrum of the emitted electrons from tritium, and the process occurring in the tritium nucleus (© Traser, Katrin collaboration).

teraction. Chemical transformations are also rare, otherwise we would not be running around with a constant chemical composition. The fourth interaction is therefore *weak*. Since the transformation processes were observed in the nucleus first, the interaction was named the *weak nuclear interaction*.

In  $\beta$  decay, the weak nuclear interaction transforms quarks into each other. In fact, the weak nuclear interaction can also transform leptons into each other, such as muons into electrons. But where does the energy released in  $\beta$  decay go to? Measurements in 1911 showed that the energy spectrum of the emitted electron is *continuous*. This is illustrated in Figure 140. How can this be? In 1930, Wolfgang Pauli had the courage and genius to explain this observation with a daring hypothesis: the energy of the decay is split between the electron and a new, truly astonishing particle, the *neutrino* – more precisely, the electron anti-neutrino  $\bar{\nu}_e$ . In order to agree with data, the neutrino must be uncharged, cannot interact strongly, and must be of very low mass. As a result, neutrinos interact with ordinary matter only extremely rarely, and usually fly through the Earth without being affected. This property makes their detection very difficult, but not impossible; the first neutrino was finally detected in 1952. Later on, it was discovered that there are three types of neutrinos, now called the electron neutrino, the muon neutrino and the tau neutrino, each with its own antiparticle. For the summary of these experimental efforts, see Table 19.

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## The weakness of the weak nuclear interaction

From the observation of  $\beta$  decay, and helped by the quark model, physicists quickly concluded that there must be an intermediate particle that carries the weak nuclear interaction, similar to the photon that carries the electromagnetic interaction. This 'weak radiation', in contrast to all other types of radiation, consists of *massive* particles.

▷ There are two types of weak radiation particles: the neutral Z boson with a mass of 91.2 GeV – that is the roughly mass of a silver atom – and the electrically charged W boson with a mass of 80.4 GeV.

TABLE 19 The leptons: the three neutrinos and the three charged leptons (antiparticles have opposite charge Q and parity P).

Neutring	DMASS M AND DECAY (SEE TEXT)	-	Colour; possible weak be- haviour	isospin I, strangeness S,	
Electron neutrino v <sub>e</sub>	$< 2 \mathrm{eV}/c^2$ , oscillates	$\frac{1}{2}^{+}$	white; singlet, doublet	0, 0, 0, 0, 0, 0, 0	1,0
Muon neutrino $v_e$	$< 2 \text{ eV}/c^2$ , oscillates	$\frac{1}{2}^{+}$	white; singlet, doublet	0, 0, 0, 0, 0, 0, 0	1,0
Tau neutrino $v_e$	$< 2 \mathrm{eV}/c^2$ , oscillates	$\frac{1}{2}^{+}$	white; singlet, doublet	0, 0, 0, 0, 0, 0, 0	1,0
Electron <i>e</i>	0.510 998 928(11) MeV/c <sup>2</sup> , stable	$\frac{1}{2}^{+}$	white; singlet, doublet	-1, 0, 0, 0, 0, 0	1,0
Muon $\mu$	105.658 3715(35) MeV/ $c^2$ , c. 99 % $e\overline{v}_e v_\mu$	$\frac{1}{2}^{+}$	white; singlet, doublet	-1,0,0,0,0,0	1,0
Tau τ	1.776 82(16) GeV/ $c^2$ , c. 17 % $\mu \overline{\nu}_{\mu} \nu_{\tau}$ , c. 18 % $e \overline{\nu}_e \nu_{\tau}$	$\frac{1}{2}^{+}$	white; singlet, doublet	-1, 0, 0, 0, 0, 0	1,0

Together, the W and Z bosons are also called the *weak vector bosons*, or the *weak intermediate bosons*.

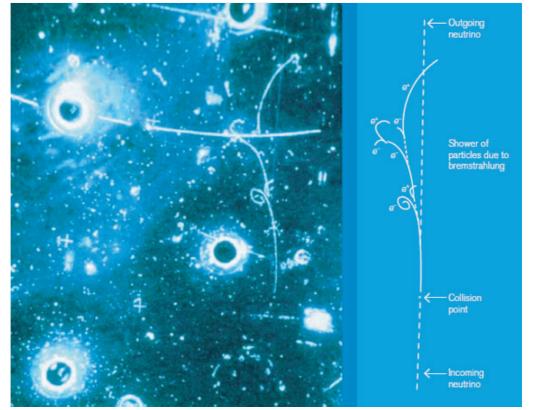
The masses of the weak vector bosons are so large that free weak radiation exists only for an extremely short time, about 0.1 ys; then the bosons decay. The large mass is the reason that the weak interaction is extremely short range and thus extremely weak. Indeed, any exchange of virtual carrier particles scales with the negative exponential of the intermediate particle's mass. A few additional properties are given in Table 20. In fact, the weak interaction is so weak that neutrinos, particles which interact *only* weakly, have a large probability to fly through the Sun without any interaction.

The existence of a massive charged intermediate vector boson, today called the W, was already deduced and predicted in the 1940s; but theoretical physicists did not accept the idea until the Dutch physicists Martin Veltman and Gerard 't Hooft proved that it was possible to have such a mass without having problems in the rest of the theory. For this proof they later received the Nobel Prize in Physics – after experiments confirmed their prediction.

The existence of an additional massive *neutral* intermediate vector boson, the Z boson, was predicted only much after the W boson, by Salam, Weinberg and Glashow. Experimentally, the Z boson was first observed as a *virtual* particle in 1973 at CERN in Geneva. The discovery was made by looking, one by one, at over 700 000 photographs made at

**TABLE 20** The intermediate vector bosons of the weak interaction (the Z boson is its own antiparticle; the W boson has an antiparticle of opposite charge).

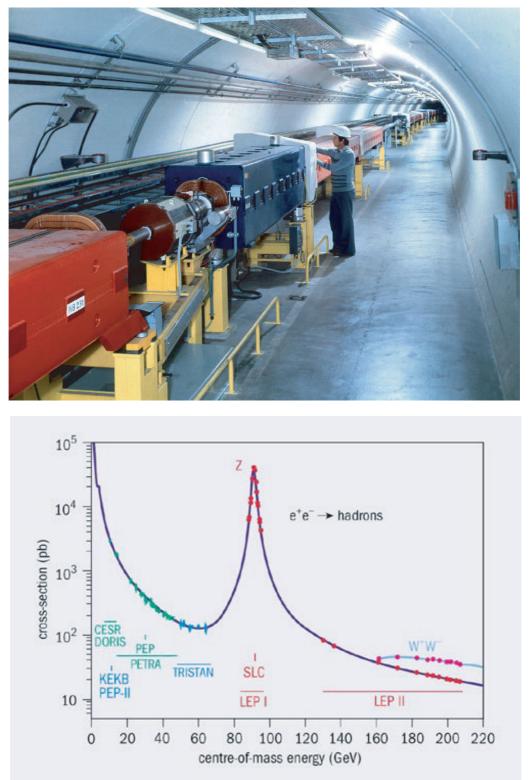
Boson	Mass m	Spin J	WEAK BE-	CHARGE Q, ISOSPIN $I$ , STRANGENESS S, CHARM C, BEAUTY B', TOPNESS $T$	Lepton number L, baryon number B
Z boson	91.1876(21) GeV/c <sup>2</sup>	1	white; 'triplet'	0, 0, 0, 0, 0, 0, 0	0,0
W boson	80.398(25) GeV/ $c^2$	1	white; 'triplet'	1, 0, 0, 0, 0, 0	0,0



**FIGURE 141** The first observation of a virtual Z boson: only neutral weak currents allow that a neutrino collides with an electron in the bubble chamber and leaves again (© CERN).

the Gargamelle bubble chamber. Only a few interesting pictures were found; the most famous one is shown in Figure 141.

In 1983, CERN groups produced and detected the first *real* W and Z bosons. This experiment was a five-year effort by thousands of people working together. The results are



**FIGURE 142** Top: the SPS, the proton–antiproton accelerator and collider at CERN, with 7 km circumference, that was used to make the first observations of real W and Z bosons. Bottom: the beautifully simple Z observation made with LEP, the successor machine (© CERN)

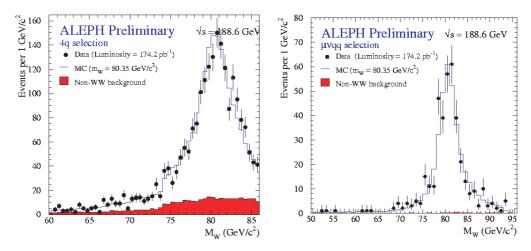


FIGURE 143 A measurement of the W boson mass at LEP (© CERN)

summarized in Table 20. The energetic manager of the project, Carlo Rubbia, whose bad temper made his secretaries leave, on average, after three weeks, and the chief technologist, Simon van der Meer, received the 1984 Nobel Prize in Physics for the discovery. This again confirmed the 'law' of nature that bosons are discovered in Europe and fermions in America. The simplest data that show the Z and W bosons is shown in Figure 142 and Figure 143; both results are deduced from the cross section of electron-positron collisions at LEP, a decade after the original discovery.

In the same way that photons are emitted by accelerated electric charges, W and Z bosons are emitted by accelerated weak charges. Due to the high mass of the W and Z bosons, the required accelerations are very high, so that they are only found in certain nuclear decays and in particle collisions. Nevertheless, the W and Z bosons are, apart from their mass and their weak charge, similar to the photon in most other aspects. In particular, the W and the Z are observed to be elementary. For example, the W gyromagnetic ratio has the value predicted for elementary particles.

Ref. 186

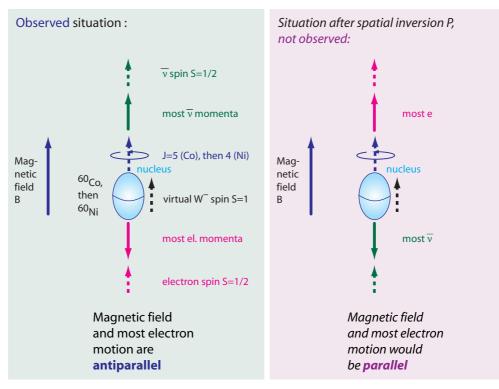
## DISTINGUISHING LEFT FROM RIGHT

Another weird characteristic of the weak interaction is the non-conservation of parity P under spatial inversion. The weak interaction distinguishes between mirror systems; this is in contrast to everyday life, to gravitation, to electromagnetism, and to the strong interaction. The non-conservation of parity by the weak interaction had been predicted by 1956 by Lee Tsung-Dao and Yang Chen Ning in order to explain the ability of  $K^0$  mesons to decay sometimes into 2 pions, which have even parity, and sometimes into 3 pions, which have odd parity.

Ref. 202

Lee and Yang suggested an experiment to Wu Chien-Shiung\* The experiment she performed with her team is shown schematically in Figure 144. A few months after the

<sup>\*</sup> Wu Chien-Shiung (b. 1912 Shanghai, d. 1997 New York) was called 'madame Wu' by her colleagues. She was a bright and driven physicist born in China. She worked also on nuclear weapons; later in life she was president of the American Physical Society.



**FIGURE** 144 The measured behaviour of  $\beta$  decay, and its imagined, but unobserved behaviour under spatial inversion P (corresponding to a mirror reflection plus subsequent rotation by  $\pi$  around an axis perpendicular to the mirror plane).

first meetings with Lee and Yang, Wu and her team found that in the  $\beta$  decay of cobalt nuclei aligned along a magnetic field, the electrons are emitted mostly *against* the spin of the nuclei. In the experiment with inversed parity, the electrons would be emitted *along* the spin direction; however, this case is not observed. Parity is violated. This earned Lee and Yang a Nobel Prize in 1957.

Parity is thus violated in the weak interaction. Parity violation does not only occur in  $\beta$  decay. Parity violation has been found in muon decay and in every other weak process studied so far. In particular, when two electrons collide, those collisions that are mediated by the weak interaction behave differently in a mirror experiment. The number of experiments showing this increases from year to year. In 2004, two polarized beams of electrons – one left-handed and one right-handed – were shot at a matter target and the reflected electrons were counted. The difference was 0.175 parts per million – small, but measurable. The experiment also confirmed the predicted weak charge of –0.046 of the electron.

Ref. 204

Ref. 203

A beautiful consequence of parity violation is its influence on the *colour* of certain atoms. This prediction was made in 1974 by Bouchiat and Bouchiat. The weak interaction is triggered by the weak charge of electrons and nuclei; therefore, electrons in atoms do not exchange only virtual photons with the nucleus, but also virtual Z particles. The chance for this latter process is extremely small, around  $10^{-11}$  times smaller than for ex-



FIGURE 145 Wu Chien-Shiung (1912 –1997) at her parity-violation experiment.

change of virtual photons. But since the weak interaction is not parity conserving, this process allows electron transitions which are impossible by purely electromagnetic effects. In 1984, measurements confirmed that certain optical transitions of caesium atoms that are impossible via the electromagnetic interaction, are allowed when the weak interaction is taken into account. Several groups have improved these results and have been able to confirm the calculations based on the weak interaction properties, including the weak charge of the nucleus, to within a few per cent.

The weak interaction thus allows one to distinguish left from right. Nature contains processes that differ from their mirror version. In short, particle physics has shown that nature is (weakly) left-handed.

The left-handedness of nature is to be taken literally. All experiments confirmed two central statements on the weak interaction that can be already guessed from Figure 144.

- ▷ The weak interaction only couples to left-handed particles and to righthanded antiparticles. Parity is *maximally violated* in the weak interaction.
- ▷ All neutrinos observed so far are left-handed, and all antineutrinos are righthanded.

This result can only hold if neutrino masses vanish or are negligibly small. These two experimental results fix several aspects of the Lagrangian of the weak interaction.

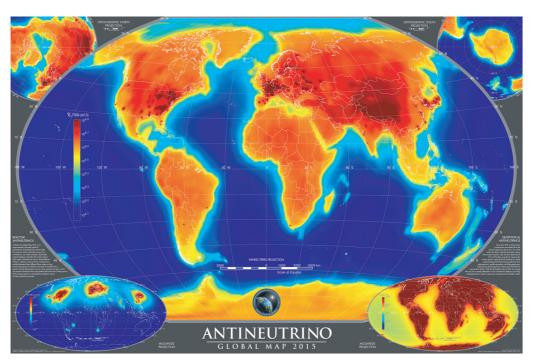
Ref. 206

Ref. 205

Challenge 146 e

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Challenge 147 e



**FIGURE 146** A map of the intensity distribution of the  $3(2) \cdot 10^{25}$  antineutrinos between 0 and 11 MeV radiated every second from the Earth. Around 99% of the flux is from natural sources and around 1% from civil and military nuclear processing plants and reactors. The map is from www.nga.mil, thus cannot be completely trusted about the human sources.

## DISTINGUISHING PARTICLES AND ANTIPARTICLES, CP VIOLATION

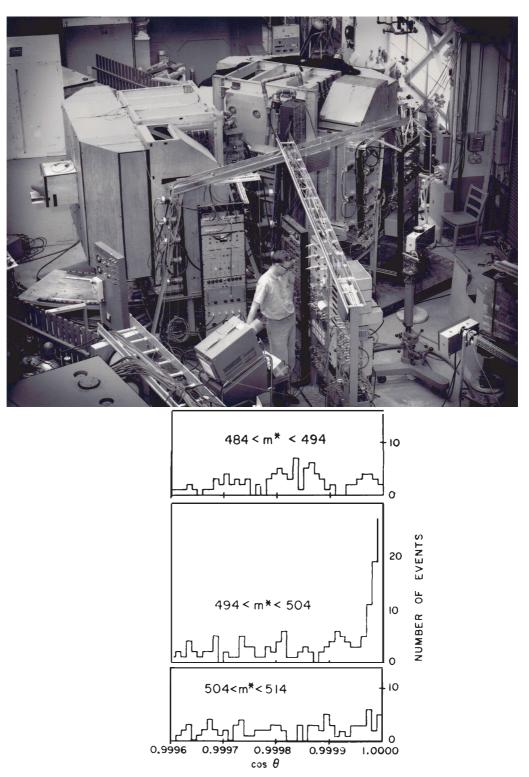
In the weak interaction, the observation that only right-handed particles and left-handed antiparticles are affected has an important consequence: it implies a violation of charge conjugation parity C. Observations of muons into electrons shows this most clearly: antimuon decay differs from muon decay. The weak interaction distinguishes particles from antiparticles.

▷ Experiments show that C parity, like P parity, is *maximally violated* in the weak interaction.

Also this effect has been confirmed in all subsequent observations ever performed on the weak interaction. But that is not all. In 1964, a now famous observation was made by Val Fitch and James Cronin in the decay of the neutral K mesons.

▷ The weak interaction also violates the combination of parity inversion with particle-antiparticle symmetry, the so-called CP invariance. In contrast to P violation and C violation, which are maximal, CP violation is a tiny effect.

The experiment, shown in Figure 147 earned them the Nobel Prize in 1980. CP violation



**FIGURE 147** Top: the experimental set-up for measuring the behaviour of neutral K meson decay. Bottom: the measured angular dependence; the middle graph shows a peak at the right side that would not appear if CP symmetry would not be violated (© Brookhaven National Laboratory, Nobel Foundation).



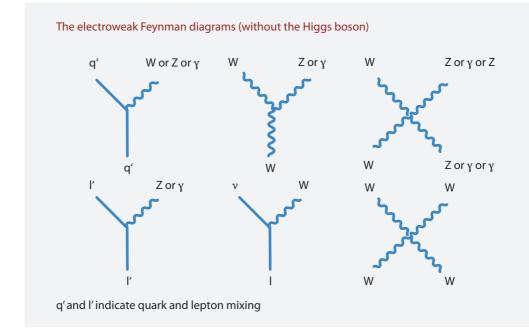


FIGURE 148 The essence of the electroweak interaction Lagrangian.

has also been observed in neutral B mesons, in several different processes and reactions. The search for other manifestations of CP violation, such as in non-vanishing electric dipole moments of elementary particles, is an intense research field. The search is not simple because CP violation is a small effect in an already very weak interaction; this tends to makes experiments large and expensive.

Since the weak interaction violates CP invariance, it also violates motion (or time) reversal T.

▷ But like all gauge theories, the weak interaction does not violate the combined CPT symmetry: it is CPT invariant.

If CPT would be violated, the masses, lifetimes and magnetic moments of particles and antiparticles would differ. That is not observed.

## WEAK CHARGE AND MIXINGS

All weak interaction processes can be described by the Feynman diagrams of Figure 148. But a few remarks are necessary. First of all, the W and Z act only on left-handed fermion and on right-handed anti-fermions. Secondly, the weak interaction conserves a so-called *weak charge*  $T_3$ , also called *weak isospin*. The three quarks u, c and t, as well as the three neutrinos, have weak isospin  $T_3 = 1/2$ ; the other three quarks and the charged leptons have weak isospin  $T_3 = -1/2$ . In an idealized, SU(2)-symmetric world, the three vector bosons  $W^+, W^0, W^-$  would have weak isospin values 1,0 and -1 and be massless. However, a few aspects complicate the issue. First of all, it turns out that the quarks appearing in Figure 148 are not those of the strong interaction: there is a slight difference, due to *quark mixing*. Secondly, also *neutrinos mix*. And thirdly, the vector bosons are massive and break the SU(2) symmetry of the imagined idealized world; the Lie group SU(2) is not an exact symmetry of the weak interaction, and the famous Higgs boson has mass. We now explore these aspects in this order.

Surprisingly, the weak interaction eigenstates of the quarks are not the same as the mass eigenstates. This discovery by Nicola Cabibbo is described by the so-called Cabibbo–Kobayashi–Maskawa or CKM mixing matrix. The matrix is defined by

$$\begin{pmatrix} d'\\s'\\b' \end{pmatrix} = (V_{ij}) \begin{pmatrix} d\\s\\b \end{pmatrix}.$$
(91)

where, by convention, the states of the +2/3 quarks (u, c, t) are unmixed. In its standard parametrization, the CKM matrix reads

$$V = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{13}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{13}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{13}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{13}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{13}} & c_{23}c_{13} \end{pmatrix}$$
(92)

where  $c_{ij} = \cos \theta_{ij}$ ,  $s_{ij} = \sin \theta_{ij}$  and *i* and *j* label the generation  $(1 \le i, j \le 3)$ . In the limit  $\theta_{23} = \theta_{13} = 0$ , i.e., when only two generations mix, the only remaining parameter is the angle  $\theta_{12}$ , called the *Cabibbo angle*, which was introduced when only the first two generations of fermions were known. The phase  $\delta_{13}$ , lying between 0 and  $2\pi$ , is different from zero in nature, and expresses the fact that CP invariance is violated in the case of the weak interactions. It appears in the third column and shows that CP violation is related to the existence of (at least) three generations.

The CP violating phase  $\delta_{13}$  is usually expressed with the *Jarlskog invariant*, defined as  $J = \sin \theta_{12} \sin \theta_{13} \sin \theta_{23}^2 \cos \theta_{12} \cos \theta_{13} \cos \theta_{23} \sin \delta_{13}$ . This expression is independent of the definition of the phase angles; it was discovered by Cecilia Jarlskog, an important Swedish particle physicist. Its measured value is  $J = 2.96(20) \cdot 10^{-5}$ .

The CKM mixing matrix is predicted to be unitary. The unitarity has been confirmed by all experiments so far. The 90 % confidence upper and lower limits for the *magnitude* of the complex CKM matrix V are given by

$$|V| = \begin{pmatrix} 0.97428(15) & 0.2253(7) & 0.00347(16) \\ 0.2252(7) & 0.97345(16) & 0.0410(11) \\ 0.00862(26) & 0.0403(11) & 0.999152(45) \end{pmatrix}.$$
 (93)

The values have been determined in dozens of experiments by thousands of physicists.

Also neutrinos mix, in the same way as the d, s and b quarks. The determination of the matrix elements is not as complete as for the quark case. This is an intense research field. Like for quarks, also for neutrinos the mass eigenstates and the flavour eigenstates differ. There is a dedicated neutrino mixing matrix, called the *Pontecorvo–Maki–Nakagawa–* 

Ref. 207

Ref. 186

Ref. 186

*Sakata mixing matrix* or *PMNS mixing matrix*, with 4 angles for massive neutrinos (it would have 6 angles if neutrinos were massless). In 2012, the measured matrix values were

$$P = \begin{pmatrix} 0.82 & 0.55 & -0.15 + 0.038i \\ -0.36 + 0.020i & 0.70 + 0.013i & 0.61 \\ 0.44 + 0.026i & -0.45 + 0.017i & 0.77 \end{pmatrix}.$$
 (94)

Many experiments are trying to measure these parameters with higher precision.

#### Symmetry breaking – and the lack of electroweak unification

The intermediate W and Z bosons are massive and their masses differ. Thus, the weak interaction does not show a SU(2) symmetry. In addition, electromagnetic and weak processes *mix*.

Beautiful research in the 1960s showed that the mixing of the electromagnetic and the weak interactions can be described by an *'electroweak' coupling constant g* and a *weak mixing angle*  $\theta_W$ . The mixing angle describes the strength of the breaking of the SU(2) symmetry.

It needs to be stressed that in contrast to what is usually said and written, the weak and the electromagnetic interactions do *not* unify. They have *never* been unified. Despite the incessant use of the term '*electroweak* unification' since several decades, the term is *wrong*. The electromagnetic and the weak interactions are two independent interactions, with two coupling constants, that *mix*. But they do not unify. Even though the Nobel Prize committee used the term 'unification', the relevant Nobel Prize winners confirm that the term is *not correct*.

The electromagnetic and the weak interaction have *not* been unified. Their mixing has been elucidated.

The usual electromagnetic coupling constant *e* is related to the 'electroweak' coupling *g* and the mixing angle  $\theta_w$  by

$$e = g\sin\theta_{\rm w} \,, \tag{95}$$

which at low four-momentum transfers is the fine structure constant with the value 1/137.036. The electroweak coupling constant g also defines the historically defined *Fermi* constant  $G_{\rm F}$  by

 $G_{\rm F} = \frac{g^2 \sqrt{2}}{8M_W^2} \,. \tag{96}$ 

The broken SU(2) symmetry implies that in the *real* world, in contrast to the *ideal* SU(2) world, the intermediate vector bosons are

- the massless, neutral photon, given as  $A = B \cos \theta_W + W^3 \sin \theta_W$ ;
- the massive neutral Z boson, given as  $Z = -B\sin\theta_W + W^3\cos\theta_W$ ;
- the massive charged W bosons, given as  $W^{\pm} = (W^1 \mp i W^2) / \sqrt{2}$ .

Together, the mixing of the electromagnetic and weak interactions as well as the breaking

of the SU(2) symmetry imply that the electromagnetic coupling e, the weak coupling g and the intermediate boson masses by the impressive relation

$$\left(\frac{m_W}{m_Z}\right)^2 + \left(\frac{e}{g}\right)^2 = 1.$$
(97)

The relation is well verified by experiments.

The mixing of the electromagnetic and weak interactions also suggests the existence of a scalar, elementary *Higgs boson*. This prediction, from the year 1963, was made by Peter Higgs and a number of other particles physicists, who borrowed ideas that Yoichiro Nambu and, above all, Philip Anderson introduced in solid state physics. The Higgs boson maintains the unitarity of longitudinal boson scattering at energies of a few TeV and influences the mass of all other elementary particles. In 2012, the Higgs boson has finally been observed in two large experiments at CERN.

#### The Lagrangian of the weak and electromagnetic interactions

If we combine the observed properties of the weak interaction mentioned above, namely its observed Feynman diagrams, its particle transforming ability, P and C violation, quark mixing, neutrino mixing and symmetry breaking, we arrive at the full Lagrangian density. It is given by:

$$\mathcal{I}_{\text{E\&W}} = \sum_{k} \overline{\psi}_{k} (i \partial - m_{k} - \frac{gm_{k}H}{2m_{W}}) \psi_{k}$$

$$-e \sum_{k} q_{k} \overline{\psi}_{k} \gamma^{\mu} \psi_{k} A_{\mu}$$

$$-\frac{g}{2\sqrt{2}} \sum_{k} \overline{\psi}_{k} \gamma^{\mu} (1 - \gamma^{5}) (T^{+} W_{\mu}^{+} + T^{-} W_{\mu}^{-}) \psi_{k}$$

$$-\frac{g}{2\sqrt{2}} \sum_{k} \overline{\psi}_{k} \gamma^{\mu} (g_{V}^{k} - g_{A}^{k} \gamma^{5}) \psi_{k} Z_{\mu}$$

$$-\frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

$$-\frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

$$-\frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

$$-\frac{1}{4} W_{\mu\nu}^{+} W^{-\mu\nu} - \frac{1}{4} Z_{\mu\nu} Z^{\mu\nu}$$

$$+m_{W}^{2} W^{+} W^{-} + \frac{1}{2} m_{Z}^{2} Z^{2}$$

$$-gWWA - gWWZ$$

$$-\frac{g^{2}}{4} (W^{4} + Z^{4} + W^{2} F^{2} + Z^{2} F^{2})$$

$$+\frac{1}{2} (\partial^{\mu} H) (\partial_{\mu} H) - \frac{1}{2} m_{H}^{2} H^{2}$$

$$-\frac{gm_{\mu}^{2}}{4m_{W}} H^{3} - \frac{g^{2} m_{\mu}^{2}}{32m_{W}^{2}} H^{4}$$

$$+ (gm_{W} H + \frac{g^{2}}{4} H^{2}) (W_{\mu}^{+} W^{-\mu} + \frac{1}{2\cos^{2} \theta_{w}} Z_{\mu} Z^{\mu})$$

$$+ (gm_{W} H + \frac{g^{2}}{4} H^{2}) (W_{\mu}^{+} W^{-\mu} + \frac{1}{2\cos^{2} \theta_{w}} Z_{\mu} Z^{\mu})$$

$$+ (gm_{W} H + \frac{g^{2}}{4} H^{2}) (W_{\mu}^{+} W^{-\mu} + \frac{1}{2\cos^{2} \theta_{w}} Z_{\mu} Z^{\mu})$$

$$+ (gm_{W} H + \frac{g^{2}}{4} H^{2}) (W_{\mu}^{+} W^{-\mu} + \frac{1}{2\cos^{2} \theta_{w}} Z_{\mu} Z^{\mu})$$

$$+ (gm_{W} H + \frac{g^{2}}{4} H^{2}) (W_{\mu}^{+} W^{-\mu} + \frac{1}{2\cos^{2} \theta_{w}} Z_{\mu} Z^{\mu})$$

$$+ (gm_{W} H + \frac{g^{2}}{4} H^{2}) (W_{\mu}^{+} W^{-\mu} + \frac{1}{2\cos^{2} \theta_{w}} Z_{\mu} Z^{\mu})$$

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$$+ (gm_{W} H + \frac{g^{2}}{4} H^{2}) (W_{\mu}^{+} W^{-\mu} + \frac{1}{2\cos^{2} \theta_{w}} Z_{\mu} Z^{\mu})$$

$$+ (gm_{W} H + \frac{g^{2}}{4} H^{2}) (W_{\mu}^{+} W^{-\mu} + \frac{1}{2\cos^{2} \theta_{w}} Z_{\mu} Z^{\mu})$$

$$+ (gm_{W} H + \frac{g^{2}}{4} H^{2}) (W_{\mu}^{+} W^{-\mu} + \frac{1}{2\cos^{2} \theta_{w}} Z_{\mu} Z^{\mu})$$

$$+ (gm_{W} H + \frac{g^{2}}{4} H^{2}) (W_{\mu}^{+} W^{-\mu} + \frac{gm_{W}}{4} Z^{\mu})$$

$$+ (gm_{W} H + \frac{gm_{W}}{4} Z^{\mu})$$

$$+$$

The terms in the Lagrangian are easily associated to the Feynman diagrams of Figure 148:
 this term describes the inertia of every object around us, yields the motion of fermions, and represents the kinetic energy of the quarks and leptons, as it appears in the usual Dirac equation, modified by the so-called *Yukawa coupling* to the Higgs field *H* and possibly by a Majorana term for the neutrinos (not shown);

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- 2. the second term describes the well-known interaction of matter and electromagnetic radiation, and explains practically all material properties and colours observed in daily life;
- 3. the term is the so-called *charged weak current interaction*, due to exchange of virtual W bosons, that is responsible for the β decay and for the fact that the Sun is shining;
- 4. this term is the *neutral weak current interaction*, the 'V A theory' of George Sudarshan, that explains the elastic scattering of neutrinos in matter;
- 5. this term represents the kinetic energy of photons and yields the evolution of the electromagnetic field in vacuum, thus the basic Maxwell equations;
- 6. this term represents the kinetic energy of the weak radiation field and gives the evolution of the intermediate W and Z bosons of the weak interaction;
- 7. this term is the kinetic energy of the vector bosons;
- 8. this term represents the triple vertex of the self-interaction of the vector boson;
- 9. this term represents the quadruple vertex of the self-interaction of the vector boson;
- 10. this term is the kinetic energy of Higgs boson;
- 11. this term is the self-interaction of the Higgs boson;
- 12. the last term is expected to represent the interaction of the vector bosons with the Higgs boson that restore unitarity at high energies.

Let us look into the formal details. The quantities appearing in the Lagrangian are:

d

- The wave functions  $\psi_k = (v'_k l^-_k)$  for leptons and  $(u_k d'_k)$  for quarks are the left-handed fermion fields of the *k*-th fermion generation; every component is a spinor. The index k = 1, 2, 3 numbers the generation: the value 1 corresponds to (u d  $v_e e^-$ ), the second generation is (c s  $v_\mu \mu^-$ ) and the third (t b  $v_\tau \tau^-$ ). The  $\psi_k$  transform as doublets under SU(2); the right handed fields are SU(2) singlets.

In the doublets, one has

$$V_{k}' = \sum_{l} V_{kl} d_{l} , \qquad (99)$$

where  $V_{kl}$  is the Cabibbo–Kobayashi–Maskawa mixing matrix,  $d'_k$  are the quark flavour eigenstates and  $d_k$  are the quark mass eigenstates. A similar expression holds for the mixing of the neutrinos:

$$\nu_k' = \sum_l P_{kl} \nu_l , \qquad (100)$$

where  $P_{kl}$  is the Pontecorvo–Maki–Nakagawa–Sakata mixing matrix,  $v'_l$  the neutrino flavour eigenstates and  $v_l$  the neutrino mass eigenstates.

- For radiation,  $A^{\mu}$  and  $F^{\mu\nu}$  is the field of the massless vector boson of the electromagnetic field, the *photon*  $\gamma$ .
  - $W^{\pm}_{\mu}$  are the massive charged gauge vector bosons of the weak interaction; the corresponding particles,  $W^{+}$  and  $W^{-}$ , are each other's antiparticles.

 $Z_{\mu}$  is the field of the massive neutral gauge vector boson of the weak interactions; the neutral vector boson itself is usually called Z<sup>0</sup>.

- H is the field of the neutral scalar Higgs boson H<sup>0</sup>, the only elementary scalar particle in the standard model.
- Two charges appear, one for each interaction. The number  $q_k$  is the well-known *elec*-

*tric charge* of the particle  $\psi_k$  in units of the positron charge. The number  $t_{3L}(k)$  is the *weak isospin*, or *weak charge*, of fermion *k*, whose value is +1/2 for  $u_k$  and  $v_k$  and is -1/2 for  $d_k$  and  $l_k$ . These two charges together define the so-called *vector coupling* 

$$g_V^k = t_{3L}(k) - 2q_k \sin^2 \theta_W \tag{101}$$

and the axial coupling

$$g_A^k = t_{3L}(k) . (102)$$

The combination  $g_V^k - g_A^k$ , or V - A for short, expresses the maximal violation of P and C parity in the weak interaction.

- The operators  $T^+$  and  $T^-$  are the weak isospin raising and lowering operators. Their action on a field is given e.g. by  $T^+l_k^- = v_k$  and  $T^-u_k = d_k$ .

We see that the Lagrangian indeed contains all the ideas developed above. The electroweak Lagrangian is essentially *unique*: it could not have a different mathematical form, because both the electromagnetic terms and the weak terms are fixed by the requirements of Lorentz invariance, U(1) and broken SU(2) gauge invariance, permutation symmetry and renormalizability.

The Lagrangian of the weak interaction has been checked and confirmed by thousands of experiments. Many experiments have been designed specifically to probe it to the highest precision possible. In all these cases, no contradictions between observation

Ref. 186

and theory has ever been found. Even though the last three terms of the Lagrangian are not fully confirmed, this is – most probably – the exact Lagrangian of the weak interaction.

#### Curiosities about the weak interaction

The weak interaction, with its breaking of parity and its elusive neutrino, exerts a deep fascination on all those who have explored it. Let us explore this fascination a bit more.

\* \*

The weak interaction is required to have an excess of matter over antimatter. Without the parity violation of the weak interactions, there would be no matter at all in the universe, because all matter and antimatter that appeared in the big bang would have annihilated. The weak interaction prevents the symmetry between matter and antimatter, which is required to have an excess of one over the other in the universe. In short, the parity violation of the weak interaction is a necessary condition for our own existence.

\* \*

The weak interaction is also responsible for the heat produced inside the Earth. This heat keeps the magma liquid. As a result, the weak interaction, despite its weakness, is responsible for most earthquakes, tsunamis and volcanic eruptions.

\* \*

The Lagrangian of the weak interaction was clarified by Steven Weinberg, Sheldon

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Glashow and Abdus Salam. They received the 1979 Nobel Prize in physics for their work.

Abdus Salam (b. 1926 Santokdas, d. 1996 Oxford) was a physics genius, the greatest Pakistani scientist by far, an example to many scientists across the world, the first muslim science Nobel-Prize winner, and a deeply spiritual man. In his Nobel banquet speech he explained: 'This, in effect, is the faith of all physicists: the deeper we seek, the more is our wonder excited, the more is the dazzlement for our gaze.' Salam often connected his research to the spiritual aspects of Islam. Once he was asked in Pakistani television why he believed in unification of physics. He answered: 'Because god is one!' When the parliament of Pakistan, in one of the great injustices of the twentieth century, declared Ahmadi Muslims to be non-Muslims and thus effectively started a religious persecution, Salam left Pakistan and never returned. The religious persecution continues to this day: on his tombstone in Pakistan, the word 'muslim' has been hammered away, and the internet is full of offensive comments about him by other muslims, even on Wikipedia. Salam was also an important science manager. With support of UNESCO, Salam founded the International Centre for Theoretical Physics and the Third World Academy of Sciences, both in Trieste, in Italy, and attracted there the best scientists from developing countries.

 $\beta$  decay, due to the weak interaction, separates electrons and protons. Finally, in 2005, people have proposed to use this effect to build long-life batteries that could be used in satellites. Future will tell whether the proposals will be successful.

\*

Ref. 211 Every second around  $10^{16}$  neutrinos fly through our body. They have five sources:

- Solar neutrinos arrive on Earth at  $6 \cdot 10^{14}$  /m<sup>2</sup>s, with an energy from 0 to 0.42 MeV; they are due to the p-p reaction in the sun; a tiny is due to the <sup>8</sup>B reaction and has energies up to 15 MeV.
- Atmospheric neutrinos are products of cosmic rays hitting the atmosphere, consist of 2/3 of muon neutrinos and one third of electron neutrinos, and have energies mainly between 100 MeV and 5 GeV.
- *Earth neutrinos* from the radioactivity that keeps the Earth warm form a flux of  $6 \cdot 10^{10} / \text{m}^2 \text{s}$ .
- Fossil neutrinos from the big bang, with a temperature of 1.95 K are found in the universe with a density of  $300 \text{ cm}^{-3}$ , corresponding to a flux of  $10^{15} / \text{m}^2 \text{s}$ .
- Man-made neutrinos are produced in nuclear reactors (at 4 MeV) and as neutrino beams in accelerators, using pion and kaon decay. A standard nuclear plant produces  $5 \cdot 10^{20}$  neutrinos per second. Neutrino beams are produced, for example, at the CERN in Geneva. They are routinely sent 700 km across the Earth to the Gran Sasso laboratory in central Italy, where they are detected. (In 2011, a famous measurement error led some people to believe, incorrectly, that these neutrinos travelled faster than light.)

Neutrinos are mainly created in the atmosphere by cosmic radiation, but also coming directly from the background radiation and from the centre of the Sun. Nevertheless, during our own life – around 3 thousand million seconds – we have only a 10% chance that one of these neutrinos interacts with one of the  $3 \cdot 10^{27}$  atoms of

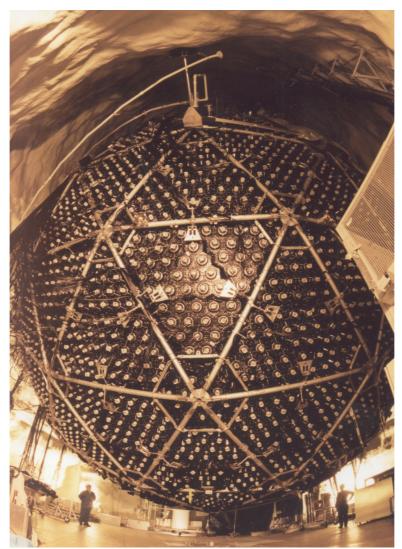


FIGURE 149 A typical underground experiment to observe neutrino oscillations: the Sudbury Neutrino Observatory in Canada (© Sudbury Neutrino Observatory)

our body. The reason is, as usual, that the weak interaction is felt only over distances less than  $10^{-17}$  m, about 1/100th of the diameter of a proton. The weak interaction is indeed weak.

\* \*

Already in 1957, the great physicist Bruno Pontecorvo imagined that travelling neutrinos could spontaneously change into their own antiparticles. Today, it is known experimentally that travelling neutrinos can change generation, and one speaks of *neutrino oscillations*. Such experiments are carried out in large deep underground caves; the most famous one is shown in Figure 149. In short, experiments show that the weak interaction mixes neutrino types in the same way that it mixes quark types.

\* \*

Only one type of particles interacts (almost) only weakly: neutrinos. Neutrinos carry no electric charge, no colour charge and almost no gravitational charge (mass). To get an impression of the weakness of the weak interaction, it is usually said that the probability of a neutrino to be absorbed by a lead screen of the thickness of one light-year is less than 50%. The universe is thus essentially empty for neutrinos. Is there room for bound states of neutrinos circling masses? How large would such a bound state be? Can we imagine bound states, which would be called neutrinium, of neutrinos and antineutrinos circling each other? The answer depends on the mass of the neutrino. Bound states of massless particles do not exist. They could and would decay into two free massless particles.\*

Since neutrinos are massive, a neutrino–antineutrino bound state is possible in principle. How large would it be? Does it have excited states? Can they ever be detected? These issues are still open.

The weak interaction is so weak that a neutrino–antineutrino annihilation – which is only possible by producing a massive intermediate Z boson – has never been observed up to this day.

\*

Exploring the mixing of the weak and the electromagnetic interaction led to the prediction of the *Higgs boson*. The fascination of the Higgs boson is underlined by the fact that it is the only fundamental particle that bears the name of a physicist. By the way, the paper by Peter Higgs on the boson named after him is only 79 lines long, and has only five equations.

\* \*

In the years 1993 and 1994 an intense marketing campaign was carried out across the United States of America by numerous particle physicists. They sought funding for the 'superconducting supercollider', a particle accelerator with a circumference of 80 km. This should have been the largest machine ever built, with a planned cost of more than twelve thousand million dollars, aiming at finding the Higgs boson before the Europeans would do so at a fraction of that cost. The central argument brought forward was the following: since the Higgs boson is the basis of particle masses, it was central to US science to know about it first. Apart from the issue of the relevance of the conclusion, the worst is that the premise is wrong.

Page 234

Ref. 195

We have seen above that 99 % of the mass of protons, and thus of the universe, is due to quark confinement; this part of mass appears even if the quarks are approximated as massless. The Higgs boson is *not* responsible for the origin of mass itself; it just might shed some light on the issue. In particular, the Higgs boson does not allow calculating

or understanding the mass of any particle. The whole campaign was a classic case of disinformation, and many people involved have shown their lack of honesty.\*\* In the end, the project was stopped, mainly for financial reasons.

Challenge 148 ny

Ref. 210

<sup>\*</sup> In particular, this is valid for photons bound by gravitation; this state is not possible.

<sup>\*\*</sup> We should not be hypocrites. The supercollider lie is negligible when compared to other lies. The biggest lie in the world is probably the one that states that to ensure its survival, the USA government need to spend more on the military than all other countries in the world combined. This lie is, every single year, around 40 times as big as the once-only supercollider lie. Many other governments devote even larger percentages of

Juvenal, Saturae 1, 30.

\* \*

There is no generally accepted name for the quantum field theory of the weak interaction. The expression *quantum asthenodynamics* (QAD) – from the Greek word for 'weak' – has not been universally adopted.

\* \*

Do ruminating *cows* move their jaws equally often in clockwise and anticlockwise direction? In 1927, the theoretical physicists Pascual Jordan and Ralph de Laer Kronig published a study showing that in Denmark the two directions are almost equally distributed. The rumination direction of cows is thus not related to the weak interaction.

\* \*

Of course, the weak interaction is responsible for radioactive  $\beta$  decay, and thus for part of the radiation background that leads to mutations and thus to biological evolution.

\* \*

Due to the large toll it placed on society, research in nuclear physics, has almost disappeared from the planet, like poliomyelitis has. Like poliomyelitis, nuclear research is kept alive only in a few highly guarded laboratories around the world, mostly by questionable figures, in order to build dangerous weapons. Only a small number of experiments carried on by a few researchers are able to avoid this involvement and continue to advance the topic.

\* \*

Interesting aspects of nuclear physics appear when powerful lasers are used. In 1999, a British team led by Ken Ledingham observed laser induced uranium fission in <sup>238</sup>U nuclei. In the meantime, this has even be achieved with table-top lasers. The latest feat, in 2003, was the transmutation of <sup>129</sup>I to <sup>128</sup>I with a laser. This was achieved by focussing a 360 J laser pulse onto a gold foil; the ensuing plasma accelerates electrons to relativistic speed, which hit the gold and produce high energy  $\gamma$  rays that can be used for the transmutation.

#### A SUMMARY OF THE WEAK INTERACTION

The weak interaction is described by a non-Abelian gauge theory based on a broken SU(2) gauge group for weak processes. The weak interaction mixes with the unbroken U(1) gauge group of the electrodynamic interaction. This description matches the observed properties of  $\beta$  decay, of particle transformations, of neutrinos and their mixing, of the massive intermediate W and Z bosons, of maximal parity violation, of the heat

Ref. 212

Ref. 213

their gross national product to their own version of this lie. As a result, the defence spending lie is directly responsible for most of the poverty in all the countries that use it.

<sup>\* &#</sup>x27;It is hard not to be satirical.'

#### 8 AND THE HANDEDNESS OF NATURE

production inside the Earth, of several important reactions in the Sun and of the origin of matter in the universe. Even though the weak interaction is weak, it is a bit everywhere.

The weak interaction is described by a Lagrangian. After a century of intense research, the Lagrangian is known in all its details, including, since 2012, the Higgs boson. Theory and experiment agree whenever comparisons have been made.

All remaining limitations of the gauge theory of the weak interaction are only conceptual. Like in all of quantum field theory, also in the case of the weak interaction the mathematical form of the Lagrangian is almost uniquely defined by requiring renormalizability, Lorentz invariance, and (broken) gauge invariance – SU(2) in this case. We say again 'almost', as we did for the case of the strong interaction, because the Lagrangian

Page 239

- of the weak and electromagnetic interactions contains a few parameters that remain unexplained:
- The two coupling constants g and g' of the weak and the electromagnetic interaction are unexplained. (They define weak mixing angle  $\theta_w = \arctan(g'/g)$ .)
- The mass  $M_Z = 91 \text{ GeV}/c^2$  of the neutral Z boson is unexplained.
- The number n = 3 of generations is unexplained.
- The masses of the six leptons and the six quarks are unexplained.
- The four parameters of the Cabibbo–Kobayashi–Maskawa quark mixing matrix and the six parameters of the neutrino mixing matrix are unexplained, including the respective CP violating phases.
- The properties of space-time, in particular its Lorentz invariance, its continuity and the number of its dimensions are assumed from the outset and are obviously all unexplained.
- It is also not known how the weak interaction behaves in strong gravity, thus in strongly curved space-time.

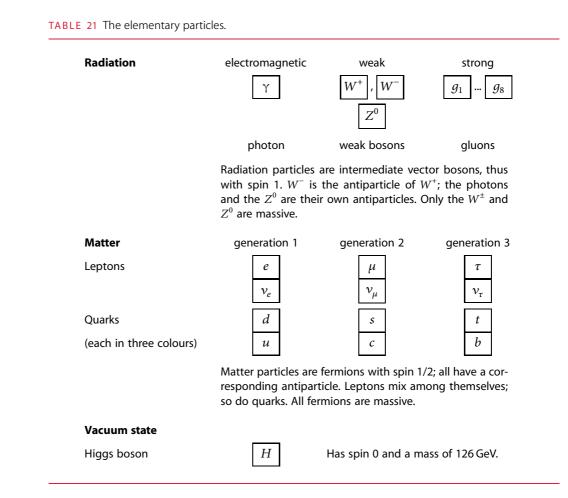
Before exploring how to overcome these limitations, we summarize all results found so far in the so-called *standard model of particle physics*.



# CHAPTER 9 THE STANDARD MODEL OF PARTICLE PHYSICS – AS SEEN ON TELEVISION

The expression standard model of elementary particle physics stands for he summary of all knowledge about the motion of quantum particles in nature. he standard model can be explained in four tables: the table of the elementary particles, the table of their properties, the table of possible Feynman diagrams and the table of fundamental constants.

The following table lists the known elementary particles found in nature.



The table has not changed much since the mid-1970s, except for the Higgs boson, which has been found in 2012. Assuming that the table is complete, it contains *all* constituents that make up all matter and all radiation in nature. Thus the table lists all constituents – the real 'uncuttables' or 'atoms', as the Greek called them – of material objects and beams of radiation. The elementary particles are the basis for materials science, geology, astronomy, engineering, chemistry, biology, medicine, the neurosciences and psychology. For this reason, the table regularly features in mass tabloids, on television and on the internet.

The full list of elementary particles allows us to put together a full table of particle properties, shown in Table 22. It lists *all* properties of the elementary particles. To save space, colour and weak isospin are not mentioned explicitly. Also the decay modes of the unstable particles are not given in detail; they are found in the standard references.

Ref. 186

Vol. I, page 29

The Table 22 on particle properties is fascinating. It allows us to give a *complete* characterization of the intrinsic properties of *any composed object or image*. At the beginning of our study of motion, we were looking for a complete list of the permanent, *intrinsic properties* of moving entities. Now we have it.

TABLE 22         Elementary particle properties	rties.
---	--------

Particle	Mass m <sup>a</sup>	LIFETIME $\tau$ o energy width, <sup>b</sup> main decay modes	spin J, <sup>c</sup> n parity <i>P</i> ,	Charge, isospin, strange- ness, <sup>c</sup> charm, beauty, topness: <i>QISCBT</i>	LEPTON & BARYON NUM- BERS LB
Elementary	radiation (bosons)				
photon y	0 (< $2 \cdot 10^{-54}$ kg)	stable	$I(J^{PC}) = 0, 1(1^{})$	000000	0,0
$W^{\pm}$	$80.385(15) \mathrm{GeV}/c^2$	2.085(42) GeV 67.60(27) % had 32.40(27) % <i>l</i> <sup>+</sup> v		±100000	0,0
Ζ	91.1876(21) GeV/ <i>c</i> <sup>2</sup>	0.265(1)  ys = 2.4952(23) Ge 69.91(6) % hadr 10.0974(69) % l <sup>4</sup>	$eV/c^2$ ons	000000	0,0
gluon	0	stable	$I(J^P) = 0(1^-)$	000000	0,0
Elementary	matter (fermions): lept	cons			
electron <i>e</i>	9.109 382 91(40) $\cdot$ 10 <sup>-31</sup> kg = 81.871 050 = 0.510 998 928(11) 1 gyromagnetic ratio $\mu$ electric dipole mome	$D6(36) \text{ pJ}/c^2$ MeV/ $c^2 = 0.00054$ $\mu_e/\mu_B = -1.001159$	2 48 579 909 46(22 9 652 180 76(27)	-100 000 ) u	1,0

Particle	Mass m <sup>a</sup>	LIFETIME $\tau$ of ENERGY WIDTH, <sup>b</sup> MAIN DECAY MODES	spin <i>J</i> , <sup>c</sup> i parity <i>P</i> ,	Charge, isospin, strange- ness, <sup>c</sup> charm, beauty, topness: QISCBT	LEPTON & BARYON NUM- BERS LB
muon μ	0.188 353 109(16) yg	2.196 9811(22) $\mu$ 99 % $e^- \bar{v}_e v_\mu$	s $J = \frac{1}{2}$	-100000	1,0
	= 105.658 3715(35) MeV/ $c^2$ = 0.113 428 9267(29) u gyromagnetic ratio $\mu_{\mu}/(e\hbar/2m_{\mu}) = -1.001 165 9209(6)$ electric dipole moment $d = (-0.1 \pm 0.9) \cdot 10^{-21} e$ m				
tau $ au$	$1.776 \ 82(16) \ \mathrm{GeV}/c^2$	290.6(1.0) fs	$J = \frac{1}{2}$	-100000	1,0
el. neutrino v <sub>e</sub>	$< 2 \mathrm{eV}/c^2$		$J = \frac{1}{2}$		1,0
muon neutrino $v_{\mu}$	$< 2 \mathrm{eV}/c^2$		$J = \frac{1}{2}$		1,0
tau neutrino $v_{\tau}$	$< 2 \mathrm{eV}/c^2$		$J = \frac{1}{2}$		1,0
Elementary r	natter (fermions): qua	rks <sup>f</sup>			
up <i>u</i> down <i>d</i>	1.8 to 3.0 MeV/ $c^2$ 4.5 to 5.5 MeV/ $c^2$	see proton see proton	$I(J^{P}) = \frac{1}{2}(\frac{1}{2}^{+})$ $I(J^{P}) = \frac{1}{2}(\frac{1}{2}^{+})$		$0, \frac{1}{3} \\ 0, $
strange s	95(5) MeV/ $c^2$		$I(J^P) = \overline{0}(\frac{1}{2}^+)$	$-\frac{1}{3}0-1000$	$0, \frac{1}{3}$
charm <i>c</i>	$1.275(25)\mathrm{GeV}/c^2$		$I(J^P) = 0(\frac{1}{2}^+)$		$0, \frac{1}{3}$
bottom <i>b</i>	$4.18(17) \mathrm{GeV}/c^2$	$\tau = 1.33(11)  \mathrm{ps}$			$0, \frac{1}{3}$
top t	$173.5(1.4)\mathrm{GeV}/c^2$		$I(J^P) = 0(\frac{1}{2}^+)$	$+\frac{2}{3}0000+1$	$0, \frac{1}{3}$
Elementary b	ooson				
Higgs H	$126(1)  \text{GeV}/c^2$	not measured	J = 0		

Notes:

*a*. See also the table of SI prefixes on page 327. About the  $eV/c^2$  mass unit, see page 331.

b. The energy width  $\Gamma$  of a particle is related to its lifetime  $\tau$  by the indeterminacy relation  $\Gamma \tau = \hbar$ . There is a difference between the *half-life*  $t_{1/2}$  and the *lifetime*  $\tau$  of a particle: they are related by  $t_{1/2} = \tau \ln 2$ , where  $\ln 2 \approx 0.693 \ 147 \ 18$ ; the half-life is thus shorter than the lifetime. The unified *atomic mass unit* u is defined as 1/12 of the mass of a carbon 12 atom at rest and in its ground state. One has  $1 \ u = \frac{1}{12} m(^{12}C) = 1.660 \ 5402(10) \ yg$ .

*c*. To keep the table short, the header does not explicitly mention *colour*, the charge of the strong interactions. This has to be added to the list of basic object properties. Quantum numbers containing the word 'parity' are multiplicative; all others are additive. Time parity *T* (not to be confused with topness *T*), better called motion inversion parity, is equal to CP. The isospin *I* (or  $I_Z$ ) is defined only for up and down quarks and their composites, such as the proton and the neutron. In the literature one also sees references to the so-called *G*-parity, defined as  $G = (-1)^{IC}$ .

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The table also does not mention the *weak charge* of the particles. The details on weak charge *g*, or, more precisely, on the *weak isospin*, a quantum number assigned to all left-handed fermions (and right-handed anti-fermions), but to no right-handed fermion (and no left-handed antifermion), are given in the section on the weak interactions.

d. 'Beauty' is now commonly called *bottomness*; similarly, 'truth' is now commonly called *topness*. The signs of the quantum numbers S, I, C, B, T can be defined in different ways. In the standard assignment shown here, the sign of each of the non-vanishing quantum numbers is given by the sign of the charge of the corresponding quark.

*e*. The electron radius is observed to be less than  $10^{-22}$  m. It is possible to store single electrons in traps for many months.

f. See page 234 for the precise definition and meaning of the quark masses.

The other aim that we formulated at the beginning of our adventure was to find the complete list of all *state properties*. This aim is also achieved, namely by the wave function and the field values due to the various bosons. Were it not for the possibility of space-time curvature, we would be at the end of our exploration.

The main ingredient of the standard model are the Lagrangians of the electromagnetic, the weak and the strong interactions. The combination of the Lagrangians, based on the U(1), SU(3) and broken SU(2) gauge groups, is possible only in one specific way. The Lagrangian can be summarized by the Feynman diagram of Figure 150.

To complete the standard model, we need the coupling constants of the three gauge interactions, the masses of all the particles, and the values of the mixing among quarks and among leptons. Together with all those constants of nature that define the SI system and the number of space-time dimensions, the following table therefore completes the standard model.

QUANTITY	Symbol	VALUE IN SI UNITS	Uncert. <sup>a</sup>		
Constants that define the SI	neasurement unit	ts			
Vacuum speed of light <sup>c</sup>	С	299 792 458 m/s	0		
Vacuum permeability <sup>c</sup>	$\mu_0$	$4\pi \cdot 10^{-7} \mathrm{H/m}$	0		
		= 1.256 637 061 435 μH/m0			
Vacuum permittivity <sup>c</sup>	$\varepsilon_0 = 1/\mu_0 c^2$	8.854 187 817 620 pF/m	0		
Original Planck constant	h	$6.62606957(52)\cdot10^{-34}\mathrm{Js}$	$4.4\cdot 10^{-8}$		
Reduced Planck constant,	ħ	$1.054571726(47)\cdot 10^{-34}\mathrm{Js}$	$4.4\cdot 10^{-8}$		
quantum of action					
Positron charge	е	0.160 217 656 5(35) aC	$2.2\cdot 10^{-8}$		
Boltzmann constant	k	$1.3806488(13)\cdot 10^{-23}\mathrm{J/K}$	$9.1\cdot 10^{-7}$		
Gravitational constant	G	$6.67384(80)\cdot 10^{-11}\mathrm{Nm}^2/\mathrm{kg}$	$2 1.2 \cdot 10^{-4}$		
Gravitational coupling consta	$\mathrm{nt}\kappa = 8\pi G/c^4$	$2.07650(25)\cdot10^{-43}\mathrm{s}^2/\mathrm{kg}\mathrm{m}$	$1.2\cdot 10^{-4}$		
Fundamental constants (of unknown origin)					
Number of space-time dimen	sions	3 + 1	0 <sup>b</sup>		
Fine-structure constant <sup>d</sup> or	$\alpha = \frac{e^2}{4\pi\varepsilon_0\hbar c}$	1/137.035999074(44)	$3.2\cdot 10^{-10}$		
e.m. coupling constant		= 0.007 297 352 5698(24)	$3.2\cdot10^{-10}$		

 TABLE 23 Basic physical constants.

Ref. 214, Ref. 215

Page 246

QUANTITY	Symbol	VALUE IN SI UNITS	Uncert. <sup>a</sup>	
Fermi coupling constant <sup>d</sup> or	$G_{\rm F}/(\hbar c)^3$	$1.166364(5)\cdot 10^{-5}\mathrm{GeV}^{-2}$	$4.3 \cdot 10^{-6}$	
weak coupling constant	$\alpha_{\rm w}(M_{\rm Z}) = g_{\rm w}^2/4$	π 1/30.1(3)	$1 \cdot 10^{-2}$	
Weak mixing angle	$\sin^2 \theta_{\rm W}(\overline{MS})$	0.231 24(24)	$1.0\cdot 10^{-3}$	
	$\sin^2 \theta_{\rm W}$ (on shell)0.2224(19)		$8.7\cdot 10^{-3}$	
	$= 1 - (m_{\rm W}/m_{\rm Z})$			
Strong coupling constant <sup>d</sup>	$\alpha_{\rm s}(M_{\rm Z}) = g_{\rm s}^2/4\tau$	τ 0.118(3)	$25\cdot 10^{-3}$	
		(0.97428(15) 0.2253(7)	0.00347(16)	
CKM quark mixing matrix	V	$\begin{pmatrix} 0.97428(15) & 0.2253(7) \\ 0.2252(7) & 0.97345(16) \\ 0.00862(26) & 0.0403(11) \end{pmatrix}$	0.0410(11)	
		0.00862(26) 0.0403(11)	0.999152(45)	
Jarlskog invariant	J	$2.96(20) \cdot 10^{-5}$		
	(	0.82 0.55	-0.15 + 0.038i	
PMNS neutrino mixing m.	P –(	0.36 + 0.020i $0.70 + 0.013i$	0.61	
	\ 0	$\begin{array}{rrr} 0.82 & 0.55 \\ 0.36 + 0.020i & 0.70 + 0.013i \\ .44 + 0.026i & -0.45 + 0.017i \end{array}$	0.77	
Particle masses: see previous table				

TABLE 23 (Continued) Basic physical constants.

a. Uncertainty: standard deviation of measurement errors.

b. Only measured from to  $10^{-19}$  m to  $10^{26}$  m.

c. Defining constant.

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*d*. All coupling constants depend on the 4-momentum transfer, as explained in the section on renormalization. *Fine-structure constant* is the traditional name for the electromagnetic coupling constant  $g_{\rm em}$  in the case of a 4-momentum transfer of  $Q^2 = m_{\rm e}^2 c^2$ , which is the smallest one possible. At higher momentum transfers it has larger values, e.g.,  $g_{\rm em}(Q^2 = M_{\rm W}^2 c^2) \approx 1/128$ . In contrast, the strong coupling constant has lower values at higher momentum transfers; e.g.,  $\alpha_{\rm s}(34 \,{\rm GeV}) = 0.14(2)$ .

In short, with the three tables and the figure, the standard model describes *every* observation ever made in flat space-time. In particular, the standard model includes a minimum action, a maximum speed, electric charge quantization and the least action principle.

#### SUMMARY AND OPEN QUESTIONS

The standard model of particle physics clearly distinguishes *elementary* from *composed* particles. The standard model provides the full list of properties that characterizes a particle – and thus any moving object and image. These properties are: mass, spin, charge, colour, weak isospin, parity, charge parity, isospin, strangeness, charm, topness, beauty, lepton number and baryon number.

The standard model describes electromagnetic and nuclear interactions as as exchanges of virtual radiation particles. In particular, the standard model describes the three types of radiation that are observed in nature with full precision, using gauge groups. The standard model is based on quantization and conservation of electric charge, weak charge and colour, as well as on a smallest action value  $\hbar$  and a maximum energy speed *c*. As a result, the standard model describes the structure of the atoms, their form-

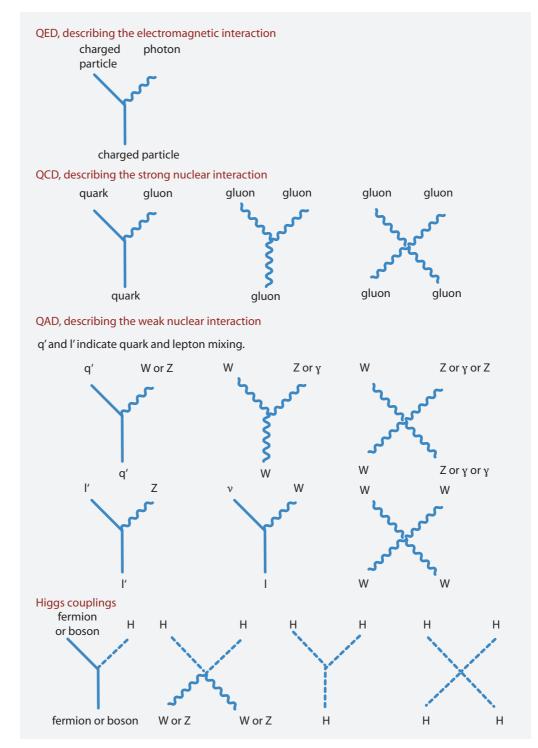


FIGURE 150 The Feynman diagrams of the standard model.

ation in the history of the universe, the properties of matter and the mechanisms of life. Despite the prospect of fame and riches, not one deviation between experiment and the standard model has been found.

In short, the standard model realizes the dream of Leucippus and Democritus, plus a bit more: we know the bricks that compose all of matter and radiation, and in addition we know how they move, interact and transform, in flat space-time, with *perfect* accuracy.

Despite this perfect accuracy, we also know what we still do *not* know:

- We do not know the origin of the coupling constants.
- We do not know why positrons and protons have the same charge.
- We do not know the origin of the masses of the particles.
- We do not know the origin of the mixing and CP violation parameters.
- We do not know the origin of the gauge groups.
- We do not know the origin of the three particle generations.
- We do not know whether the particle concept survives at high energy.
- We do not know what happens in curved space-time.

To study these issues, the simplest way is to explore nature at particle energies that are as high as possible. There are two methods: building large experiments and exploring hypothetical models. Both are useful.



# CHAPTER 10 DREAMS OF UNIFICATION

Materie ist geronnenes Licht.\*\* Albertus Magnus

s there a common origin to the three particle interactions? We have seen n the preceding chapters that the Lagrangian densities of the three gauge nteractions are determined almost uniquely by two types of requirements: to possess a certain gauge symmetry, and to be consistent with space-time, through Lorentz invariance and renormalizability. The search for *unification* of the interactions thus seems to require the identification of the one, unified symmetry of nature. (Do you agree?)

Challenge 149 s

Ref. 216

Between 1970 and 2015, several conjectures have fuelled the hope to achieve unification through higher symmetry. The most popular were grand unification, supersymmetry, conformal field theory, coupling constant duality and mathematical quantum field theory. We give a short summary of these efforts; we start with the first candidate, which is conceptually the simplest.

## GRAND UNIFICATION

At all measured energies up to the year 2016, thus below about 3 TeV, there are no contradictions between the Lagrangian of the standard model and observation. On the other hand, the Lagrangian itself can be conjectured to be a low energy approximation to the unified theory. It should thus be possible – attention, this a belief – to find a unifying symmetry that *contains* the symmetries of the electroweak and strong interactions as subgroups. In this way, the three gauge interactions would be different aspects of a single, 'unified' interaction. We can then examine the physical properties that follow from this unifying symmetry and compare them with observation. This approach, called *grand unification*, attempts the unified description of all types of matter. All known elementary particles are seen as fields which appear in a Lagrangian determined by a single gauge symmetry group.

Like for each gauge theory described so far, also the grand unified Lagrangian is fixed by the symmetry group, the representation assignments for each particle, and the corresponding coupling constant. A general search for the grand symmetry group starts with all those (semisimple) Lie groups which contain  $U(1) \times SU(2) \times SU(3)$ . The smallest groups with these properties are SU(5), SO(10) and E(6); they are defined in Appendix C.

<sup>\*\* &#</sup>x27;Matter is coagulated light.' Albertus Magnus (b. *c.* 1192 Lauingen, d. 1280 Cologne) was the most important thinker of his time.

For each of these candidate groups, the predicted consequences of the model can be stud-Ref. 217 ied and compared with experiment.

#### Comparing predictions and data

Grand unification models – also incorrectly called GUTs or *grand unified theories* – make several predictions that can be matched with experiment. First of all, any grand unified model predicts relations between the quantum numbers of quarks and those of leptons. In particular, grand unification explains why the electron charge is exactly the opposite of the proton charge.

Grand unification models predict a value for the weak mixing angle  $\theta_w$ ; this angle is Ref. 216 not fixed by the standard model. The most frequently predicted value,

$$\sin^2 \theta_{\rm w,th} = 0.2 \tag{103}$$

is close to the measured value of

$$\sin^2 \theta_{\rm w,ex} = 0.231(1) , \qquad (104)$$

which is not a good match, but might be correct, in view of the approximations in the prediction.

All grand unified models predict the existence of *magnetic monopoles*, as was shown by Gerard 't Hooft. However, despite extensive searches, no such particles have been found yet. Monopoles are important even if there is only one of them in the whole universe: the existence of a single monopole would imply that electric charge is quantized.

If monopoles were found, grand unification would explain why electric charge appears in multiples of a smallest unit.

Grand unification predicts the existence of heavy intermediate vector bosons, called *X* bosons. Interactions involving these bosons do not conserve baryon or lepton number, but only the difference B - L between baryon and lepton number. To be consistent with data, the X bosons must have a mass of the order of  $10^{16}$  GeV. However, this mass is and always will be outside the range of experiments, so that the prediction cannot be tested directly.

Most spectacularly, the X bosons of grand unification imply that the *proton decays*. This prediction was first made by Pati and Abdus Salam in 1974. If protons decay, means that neither coal nor diamond<sup>\*</sup> – nor any other material – would be for ever. Depending on the precise symmetry group, grand unification predicts that protons decay into pions, electrons, kaons or other particles. Obviously, we know 'in our bones' that the proton lifetime is rather high, otherwise we would die of leukaemia; in other words, the low level of cancer in the world already implies that the lifetime of the proton is larger than about  $10^{16}$  years.

Detailed calculations for the proton lifetime  $\tau_p$  using the gauge group SU(5) yield the

Ref. 218

Ref. 219

<sup>\*</sup> As is well known, diamond is not stable, but metastable; thus diamonds are not for ever, but coal might be, as long as protons do not decay.

Ref. 216 expression

$$\tau_{\rm p} \approx \frac{1}{\alpha_{\rm G}^2(M_{\rm X})} \frac{M_{\rm X}^4}{M_{\rm p}^5} \approx 10^{31\pm1} \,\mathrm{a}$$
 (105)

where the uncertainty is due to the uncertainty of the mass  $M_X$  of the gauge bosons involved and to the exact decay mechanism. Several large experiments have tried and are still trying to measure this lifetime. So far, the result is simple but clear. Not a single proton decay has ever been observed. The data can be summarized by

$$\begin{aligned} \tau(\mathbf{p} \to e^+ \ \pi^0) &> 5 \cdot 10^{33} \ \mathbf{a} \\ \tau(\mathbf{p} \to K^+ \ \bar{\nu}) &> 1.6 \cdot 10^{33} \ \mathbf{a} \\ \tau(\mathbf{n} \to e^+ \ \pi^-) &> 5 \cdot 10^{33} \ \mathbf{a} \\ \tau(\mathbf{n} \to K^0 \ \bar{\nu}) &> 1.7 \cdot 10^{32} \ \mathbf{a} \end{aligned} \tag{106}$$

These values are higher than the prediction by SU(5) – and SO(10) – models. For other gauge group candidates proton decay measurements require more time.

#### The state of grand unification

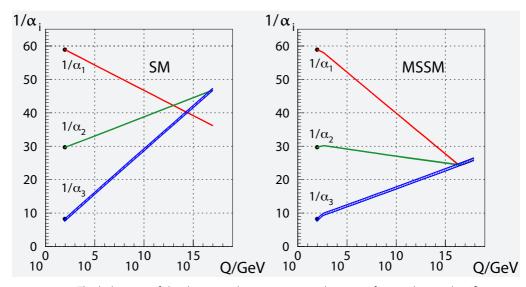
To settle the issue of grand unification definitively, one last prediction of grand unification remains to be checked: the unification of the coupling constants. Most estimates of the grand unification energy are near the Planck energy, the energy at which gravitation starts to play a role even between elementary particles. As grand unification does not take gravity into account, for a long time there was a doubt whether something was lacking in the approach. This doubt changed into certainty when the precision measurements of the coupling constants became available, in 1991, and were put into the diagram of Figure 151. The GUT prediction of the way the constants evolve with energy implies that the three constants do *not* meet at one energy. Simple grand unification by SU(5), SU(10) or  $E_6$  is thus ruled out by experiment.

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Ref. 221

This state of affairs is changed if *supersymmetry* is taken into account. Supersymmetry is a conjecture on the way to take into account low-energy effects of gravitation in the particle world. Supersymmetry conjectures new elementary particles that change the curves at intermediate energies, so that they all meet at a grand unification energy of about  $10^{16}$  GeV. (The line thicknesses in Figure 151 represent the experimental errors.) The inclusion of supersymmetry also puts the proton lifetime prediction back to a value higher (but not by much) than the present experimental bound and predicts the correct value of the mixing angle. With supersymmetry, one can thus retain the advantages of grand unification (charge quantization, one coupling constant) without being in contradiction with experiments.

In summary, pure grand unification is in contradiction with experiments. This is not a surprise, as its goal, to unify the description of matter, *cannot* been achieved in this way. Indeed, the unifying gauge group must be introduced, i.e., added, at the very beginning. Adding the group is necessary because grand unification cannot deduce the gauge group from a general principle. Neither does pure grand unification tell us completely



**FIGURE 151** The behaviour of the three coupling constants with energy, for simple grand unification (left) and for the minimal supersymmetric model (right); the graph shows the constants  $\alpha_1 = \frac{5}{3} \alpha_{em} / \cos^2 \theta_W$  for the electromagnetic interaction (the factor 5/3 appears in GUTs),  $\alpha_2 = \alpha_{em} / \sin^2 \theta_W$  for the weak interaction and the strong coupling constant  $\alpha_3 = \alpha_s$  (© W. de Boer).

which elementary particles exist in nature. In other words, grand unification only *shifts* the open questions of the standard model to the next level, while keeping most of the open questions unanswered. The name 'grand unification' was wrong from the beginning. We definitively need to continue our adventure.

#### Searching for higher symmetries

Since we want to reach the top of Motion Mountain, we go on. We have seen in the preceding sections that the main ingredients of the Lagrangian that describes motion are the symmetry properties. We recall that a Lagrangian is just the mathematical name for the concept that measures change. The discovery of the correct symmetry, together with mathematical consistency, usually restricts the possible choices for a Lagrangian down to a limited number, and to one in the best case. This Lagrangian then allows making experimental predictions.

The history of particle physics from 1920 to 1965 has shown that progress was always coupled to the discovery of *larger* symmetries, in the sense that the newly discovered symmetries always included the old ones as a subgroup. Therefore, in the twentieth century, researchers searched for the largest possible symmetry that is consistent with experiments on the one hand and with gauge theories on the other hand. Since grand unification failed, a better approach is to search directly for a symmetry that includes gravity.

#### Supersymmetry

In the search for possible symmetries of a Lagrangian describing a gauge theory and gravity, one way to proceed is to find general mathematical theorems which restrict the Ref. 222 symmetries that a Lagrangian can possibly have.



Ref. 223 A well-known theorem by Coleman and Mandula states that if the symmetry transformations transform fermions into fermions and bosons into bosons, no quantities other than the following can be conserved:

• the energy momentum tensor  $T^{\mu\nu}$ , a consequence of the *external* Poincaré spacetime symmetry, and

• the internal quantum numbers, all scalars, associated with each gauge group generator – such as electric charge, colour, etc. – and consequences of the *internal* symmetries of the Lagrangian.

But, and here comes a way out, if transformations that *mix* fermions and bosons are considered, new conserved quantities become possible. This family of symmetries includes gravity and came to be known as *supersymmetry*. Its conserved quantities are not scalars but *spinors*. Therefore, *classical* supersymmetry does not exist; it is a purely quantummechanical symmetry. The study of supersymmetry has been a vast research field. For example, supersymmetry generalizes gauge theory to super-gauge theory. The possible super-gauge groups have been completely classified.

Supersymmetry can be extended to incorporate gravitation by changing it into a local gauge theory; in that case one speaks of *supergravity*. Supergravity is based on the idea that coordinates can be fermionic as well as bosonic. Supergravity thus makes specific statements on the behaviour of space-time at small distances. Supergravity predicts N additional conserved, spinorial charges. The number N lies between 1 and 8; each value leads to a different candidate Lagrangian. The simplest case is called N = 1 supergravity.

In short, supersymmetry is a conjecture to unify matter and radiation at low energies. Many researchers conjectured that supersymmetry, and in particular N = 1 supergravity, might be an approximation to reality.

Supersymmetric models have around 100 fundamental constants, in comparison to around 25 for the standard model of particle physics. The precise experimental predictions depend on the values of these constants. Nevertheless, a number of general predictions are possible and can be tested by experiment.

— Supersymmetry predicts partners to the usual elementary particles, called *sparticles*. Fermions are predicted to have boson partners, and vice versa. For example, supersymmetry predicts a *photino* as fermionic partner of the photon, *gluinos* as partner of the gluons, a *selectron* as partner of the electron, etc. However, none of these particles have been observed yet.

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- Supersymmetry allows for the unification of the coupling constants in a way compatible with the data, as shown already above.
- Supersymmetry slows down the proton decay rates predicted by grand unified theories. The slowed-down rates are compatible with observation.
- Supersymmetry predicts electric dipole moments for the neutron and other elementary particles. The largest predicted values for the neutron,  $10^{-30}e$  m, are in contradiction with observations; the smallest predictions have not yet been reached by experiment. In comparison, the values expected from the standard model are at most  $10^{-33}e$  m. This is a vibrant experimental research field that can save tax payers from financing an additional large particle accelerator.

However, up to the time of this writing, the year 2016, there was no experimental evid-

ence for supersymmetry. In particular, the Large Hadron Collider at CERN in Geneva has not found any hint of supersymmetry. In fact, experiments excluded almost all supersymmetric particle models proposed in the past.

Is supersymmetry an ingredient of the unified theory? The safe answer is: this is unclear. The optimistic answer is: there is still a small chance that supersymmetry can hold in nature. The pessimistic answer is: supersymmetry is a belief system contradicting observations and made up to correct the failings of grand unified theories. The last volume of this adventure will tell which answer is correct.

## Other attempts

If supersymmetry is not successful, it might be that even higher symmetries are required for unification. Therefore, researchers have explored *quantum groups*, *non-commutative space-time*, *conformal symmetry*, *topological quantum field theory*, and other abstract symmetries. None of these approaches led to useful results; neither experimental predictions nor progress towards unification. But two further approaches deserve special mention: duality symmetries and extensions to renormalization.

#### DUALITIES - THE MOST INCREDIBLE SYMMETRIES OF NATURE

An important discovery of mathematical physics took place in 1977, when Claus Montonen and David Olive proved that the standard concept of symmetry could be expanded dramatically in a different and new way.

The standard class of symmetry transformations, which turns out to be only the first class, acts on fields. This class encompasses gauge symmetries, space-time symmetries, motion reversal, parities, flavour symmetries and supersymmetry.

The second, new class is quite different. If we take the coupling constants of nature, we can imagine that they are members of a continuous space of all possible coupling constants, called the *parameter space*.\* Montonen and Olive showed that there are transformations in parameter space that leave nature invariant. These transformations thus form a new, second class of symmetries of nature.

In fact, we already encountered a member of this class: renormalization symmetry. But Olive and Montonen expanded the symmetry class considerably by the discovery of *electromagnetic duality*. Electromagnetic duality is a discrete symmetry exchanging

$$e \leftrightarrow \frac{4\pi\hbar c}{e}$$
 (107)

where the right hand side turns out to be the unit of magnetic charge. Electro-magnetic duality thus relates the electric charge e and the magnetic charge m

$$Q_{\rm el} = me$$
 and  $Q_{\rm mag} = ng = 2\pi\hbar c/e$  (108)

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<sup>\*</sup> The space of solutions for all value of the parameters is called the moduli space.

and puts them on equal footing. In other words, the transformation exchanges

$$\alpha \leftrightarrow \frac{1}{\alpha} \quad \text{or} \quad \frac{1}{137.04} \leftrightarrow 137.04 ,$$
 (109)

and thus exchanges weak and strong coupling. In other words, electromagnetic duality relates a regime where particles make sense (the low coupling regime) with one where particles do not make sense (the strong coupling regime). It is the most mind-boggling symmetry ever conceived.

Dualities are among the deepest connections of physics. They contain  $\hbar$  and are thus intrinsically quantum. They do not exist in classical physics and thus confirm that quantum theory is more fundamental than classical physics. More clearly stated, dualities are intrinsically non-classical symmetries. Dualities confirm that quantum theory stands on its own.

If one wants to understand the values of unexplained parameters such as coupling constants, an obvious thing to do is to study *all* possible symmetries in parameter space, thus all possible symmetries of the second class, possibly combining them with those of the first symmetry class. Indeed, the combination of duality with supersymmetry is studied in superstring theory.

These investigations showed that there are several types of dualities, which all are *non-perturbative* symmetries:

- S duality, the generalization of electromagnetic duality for all interactions;
- T duality, also called space-time duality, a mapping between small and large lengths and times following  $l \leftrightarrow l_{\text{Pl}}^2/l_{;*}^*$
- infrared dualities.

Despite the fascination of the idea, research into dualities has not led to any experimental prediction. However, the results highlighted a different way to approach quantum field theory. Dualities play an important role in superstring theory, which we will explore later on.

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#### Collective aspects of quantum field theory

For many decades, mathematicians asked physicists: What is the essence of quantum field theory? Despite intensive research, this question has yet to be answered precisely.

Half of the answer is given by the usual definition found in physics textbooks: QFT is the most general known way to describe quantum mechanically continuous systems with a *finite* number of types of quanta but with an *infinite* number of degrees of freedom. For example, this definition implies that the Lagrangian must be relativistically invariant and must be described by a gauge theory. However, this half of the answer is already sufficient to spell trouble. We will show in the next part of our ascent that space and time have a minimal distance scale and that nature does not have infinite numbers of degrees of freedom. In other words, *quantum field theory is an effective theory*; this is the modern

Vol. VI, page 40

Vol. IV, page 112 Page 293

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Ref. 224

<sup>\*</sup> Space-time duality, the transformation between large and small sizes, leads one to ask whether there is an inside and an outside to particles. We encountered this question already in our study of gloves. We will encounter the issue again below, when we explore eversion and inversion. The issue will be fully clarified only in the last volume of our adventure.

way to say that it is approximate, or more bluntly, that it is wrong. But let us put these issues aside for the time being.

The second, still partly unknown half of the answer would specify which (mathematical) conditions a physical system, i.e., a Lagrangian, actually needs to realize in order to become a quantum field theory. Despite the work of many mathematicians, no complete list of conditions is known yet. But it is known that the list includes at least two conditions. First of all, a quantum field theory must be *renormalizable*. Secondly, a quantum field theory must be *asymptotically free*; in other words, the coupling must go to zero when the energy goes to infinity. This condition ensures that interactions are defined properly. Only a subset of renormalizable Lagrangians obey this condition.

In four dimensions, the *only* known quantum field theories with these two properties are the non-Abelian gauge theories. These Lagrangians have several general aspects which are not directly evident when we arrive at them through the usual way, i.e., by generalizing naive wave quantum mechanics. This standard approach, the historical one, emphasizes the *perturbative* aspects: we think of elementary fermions as field quanta and of interactions as exchanges of virtual bosons, to various orders of perturbation.

On the other hand, all field theory Lagrangians also show two other configurations, apart from particles, which play an important role. These mathematical solutions appear when a non-perturbative point of view is taken; they are *collective* configurations.

- Quantum field theories show solutions which are static and of finite energy, created by non-local field combinations, called *solitons*. In quantum field theories, solitons are usually magnetic monopoles and dyons; also the famous *skyrmions* are solitons. In this approach to quantum field theory, it is assumed that the actual equations of nature are non-linear at high energy. Like in liquids, one then expects stable, localized and propagating solutions, the solitons. These solitons could be related to the observed particles.
- Quantum field theories show self-dual or anti-self dual solutions, called *instantons*. Instantons play a role in QCD, and could also play a role in the fundamental Lagrangian of nature.
- Quantum field theory defines particles and interactions using perturbation expansions. Do particles exist non-perturbatively? When does the perturbation expansion break down? What happens in this case? Despite these pressing issues, no answer has ever been found.
- Ref. 225 All these fascinating topics have been explored in great detail by mathematical physicists. This research has deepened the understanding of gauge theories. However, none of the available results has yet helped to approach unification.

#### Curiosities about unification

From the 1970s onwards, it became popular to draw graphs such as the one of Figure 152. They are found in many books. This approach towards the final theory of motion was inspired by the experimental success of electroweak unification and to the success among theoreticians of the idea of grand unification.

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Unfortunately, grand unification contradicts experiment. In fact, as explained above, not even the electromagnetic and the weak interactions have been unified. (It took about a decade to brainwash people into believing the contrary; this was achieved by intro-

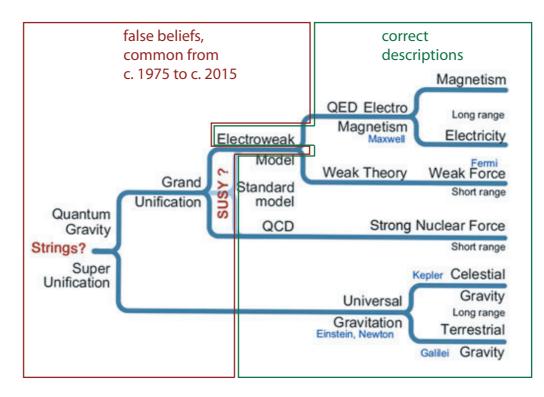


FIGURE 152 Blue and black: a typical graph on unification, as found for years in publications on the topic (© CERN). Red and green: its correct and incorrect parts.

ducing the incorrect term 'electroweak unification' instead of a correct term akin to 'electroweak compatibility' or 'electroweak mixing'.) In other words, the larger part of Figure 152 is not correct. Unfortunately, the graph and the story behind it has led most researchers along the wrong path for several decades.

Over the years, the length of this chapter became shorter and shorter. This was due to the large number of unification attempts that were found to be in contradiction with experiment. It is hard to describe the vast amount of effort that has been invested, usually in vain, in the quest for unification of the description of motion.

\* \*

For a professional and up-to-date introduction into modern particle research, see the summer student lectures that are given at CERN every year. They can be found at cdsweb. cern.ch/collection/SummerStudentLectures?ln=en.

## A summary on unification, mathematics and higher symmetries

The decades of theoretical research since the 1970s have shown:

▷ Mathematical physics is not the way to search for unification of the de-

scription of motion.

All the searches for unification that were guided by *mathematical ideas* – by mathematical theorems or by mathematical generalizations – have failed. Mathematics is not helpful in this quest. The standard model of particle physics and general relativity remain separate. In addition, the research effort has led to a much more concrete result:

▷ The search for a *higher symmetry* in nature has failed.

Despite thousands of extremely smart people exploring many possible higher symmetries of nature, their efforts have not been successful.

Symmetry considerations are not helpful in the search for unification. Symmetry *simplifies* the description of nature; but symmetry does not *specify* the description. It seems that researchers have fallen into the trap of music theory. Anybody who has learned to play an instrument has heard the statement that 'mathematics is at the basis of music'. Of course, this is nonsense; emotions are at the basis of music. But the incorrect statement about mathematics lurks in the head of every musician. Looking back to research in the twentieth century, it seems that the same has happened to researchers in the field of unification. From these failures we conclude:

▷ Unification requires to extract an underlying *physical* principle.

On the other hand, in the twentieth century, researchers have failed to find such a principle. This failure leads to two questions. In the quest for unification, is there really an alternative to the search for higher symmetry? And did researchers rely on implicit, incorrect assumptions about the structure of particles or of space-time? Before we explore these fascinating issues, we take a break to inspire us.



# CHAPTER 11 BACTERIA, FLIES AND KNOTS

La première et la plus belle qualité de la nature est le mouvement qui l'agite sans cesse ; mais ce mouvement n'est qu'une suite perpétuelle de crimes ; ce n'est que par des crimes qu'elle le conserve. Donatien de Sade, *Justine, ou les malheurs de la vertu.*\*\*

Where the provided support of the second look at everyday motion and its mathematical description.

To enjoy this chapter, we change a dear habit. So far, we always described any general example of motion as composed of the motion of *point particles*. This worked well in classical physics, in general relativity and in quantum theory; we based the approach on the silent assumption that during motion, each point of a complex system can be followed separately. We will soon discover that this assumption is *not* realized at smallest scales. Therefore the most useful description of motion of *extended* bodies uses methods that do not require that body parts be followed piece by piece. We explore these methods in this chapter; doing so is a lot of fun in its own right.

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If we describe elementary particles as extended entities – as we soon will have to – a particle moving through space is similar to a dolphin swimming through water, or to a bee flying through air, or to a vortex advancing in a liquid. Therefore we explore how this happens.

## Bumblebees and other miniature flying systems

If a butterfly passes by during our mountain ascent, we can stop a moment to appreciate a simple fact: a butterfly flies, and it is rather small. If we leave some cut fruit in the kitchen until it rots, we observe the even smaller fruit flies (*Drosophila melanogaster*), just about

<sup>\*\* &#</sup>x27;The primary and most beautiful of nature's qualities is motion, which agitates her at all times; but this motion is simply a perpetual consequence of crimes; she conserves it by means of crimes only.' Donatien Alphonse François de Sade (b. 1740 Paris, d. 1814 Charenton-Saint-Maurice) is the intense writer from whom the term 'sadism' was deduced.

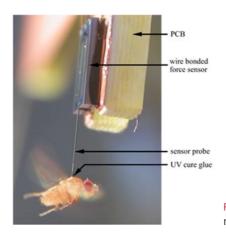


FIGURE 153 A flying fruit fly, tethered to a force-measuring microelectromechanical system (© Bradley Nelson).

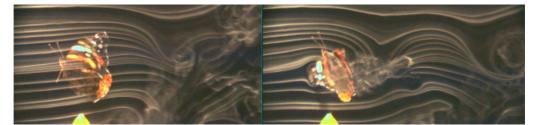


FIGURE 154 Vortices around a butterfly wing (© Robert Srygley/Adrian Thomas).

two millimetres in size. Figure 153 shows a fruit fly in flight. If you have ever tried to build small model aeroplanes, or if you even only compare these insects to paper aeroplanes – possibly the smallest man-made flying thing you might have seen – you start to get a feeling for how well evolution has optimized flying insects.

Compared to paper planes, insects also have engines, flapping wings, sensors, navigation systems, gyroscopic stabilizers, landing gear and of course all the features due to life, reproduction and metabolism, built into an incredibly small volume. Evolution really is an excellent engineering team. The most incredible flyers, such as the common house fly (*Musca domestica*), can change flying direction in only 30 ms, using the stabilizers that nature has given them by reshaping the original second pair of wings. Human engineers are getting more and more interested in the technical solutions evolution has developed; many engineers are trying to achieve similar miniaturization. The topic of miniature flying systems is extremely vast, so that we will pick out only a few examples.

Ref. 226

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How does a bumblebee (Bombus terrestris) fly? The lift *mg* generated by a *fixed* wing (as explained before) follows the empirical relation

$$mg = f A v^2 \rho \tag{110}$$

where A is the surface of the wing, v is the speed of the wing in the fluid of density  $\rho$ . The factor f is a pure number, usually with a value between 0.2 and 0.4, that depends on the angle of the wing and its shape; here we use the average value 0.3. For a Boeing Vol. I, page 38 747, the surface is 511 m<sup>2</sup>, the top speed at sea level is 250 m/s; at an altitude of 12 km the

n Mountain – The Adventure of Physics copyright © Christoph Schiller June 1990–May 2020 free pdf file available at www.motionmoun

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density of air is only a quarter of that on the ground, thus only  $0.31 \text{ kg/m}^3$ . We deduce (correctly) that a Boeing 747 has a mass of about 300 ton. For bumblebees with a speed of 3 m/s and a wing surface of 1 cm<sup>2</sup>, we get a lifted mass of about 35 mg, far less than the weight of the bee, namely about 1 g. The mismatch is even larger for fruit flies. In other words, an insect cannot fly if it keeps its wings *fixed*. It could not fly with fixed wings even if it had tiny propellers attached to them!

Due to the limitations of fixed wings at small dimensions, insects and small birds must *move* their wings, in contrast to aeroplanes. They must do so not only to take off or to gain height, but also to simply remain airborne in horizontal flight. In contrast, aeroplanes generate enough lift with *fixed* wings. Indeed, if you look at flying animals, such as the ones shown in Figure 155, you note that the larger they are, the less they need to move their wings (at cruising speed).

Can you deduce from equation (110) that birds or insects can fly but people cannot? Conversely, the formula also (partly) explains why human-powered aeroplanes must be so large.\*

But *how* do insects, small birds, flying fish or bats have to move their wings in order to fly? This is a tricky question and the answer has been uncovered only recently. The main point is that insect wings move in a way to produce eddies at the front edge which in turn thrust the insect upwards. Aerodynamic studies of butterflies – shown in Figure 154 – and studies of enlarged insect models moving in oil instead of in air are exploring the precise way insects make use of vortices. At the same time, more and more 'mechanical birds' and 'model aeroplanes' that use flapping wings for their propulsion are being built around the world. The field is literally in full swing.\*\* Researchers are especially interested in understanding how vortices allow change of flight direction at the small dimensions typical for insects. Another aim is to reduce the size of flying machines.

The expression (110) for the lift of fixed wings also shows what is necessary for safe take-off and landing. The lift of all wings *decreases* for smaller speeds. Thus both animals and aeroplanes *increase* their wing surface in these occasions. Many birds also vigorously increase the flapping of wings in these situations. But even strongly flapping, enlarged wings often are insufficient for take-off. Many flying animals, such as swallows, therefore avoid landing completely. For flying animals which do take off from the ground, nature most commonly makes them hit the wings against each other, over their back, so that when the wings separate again, the low pressure between them provides the first lift. This method is used by insects and many birds, including pheasants. As bird watchers

Challenge 150 e

Challenge 151 s

Ref. 228

Ref. 229

281

<sup>\*</sup> Another part of the explanation requires some aerodynamics, which we will not study here. Aerodynamics shows that the power consumption, and thus the resistance of a wing with given mass and given cruise speed, is inversely proportional to the square of the wingspan. Large wingspans with long slender wings are thus of advantage in (subsonic) flying, especially when energy is scarce.

One issue is mentioned here only in passing: why does an aircraft fly? The correct general answer is: *because it deflects air downwards*. How does an aeroplane achieve this? It can do so with the help of a tilted plank, a rotor, flapping wings, or a fixed wing. And when does a fixed wing deflect air downwards? First of all, the wing has to be tilted with respect to the air flow; in addition, the specific cross section of the wing can increase the downward flow. The relation between wing shape and downward flow is a central topic of applied aerodynamics.

<sup>\*\*</sup> The website www.aniprop.de presents a typical research approach and the sites ovirc.free.fr and www. ornithopter.org give introductions into the way to build such systems for hobbyists.



**FIGURE 155** Examples of the three larger wing types in nature, all optimized for rapid flows: turkey vulture (*Cathartes aura*), ruby-throated hummingbird (*Archilochus colubris*) and a dragonfly (© S.L. Brown, Pennsylvania Game Commission/Joe Kosack and nobodythere).

know, pheasants make a loud 'clap' when they take off. The clap is due to the low pressure region thus created.

Both wing use and wing construction depend on size. In fact, there are four types of wings in nature.

- 1. First of all, all large flying objects, such aeroplanes and large birds, fly using *fixed* wings, except during take-off and landing. This wing type is shown on the left-hand side of Figure 155.
- 2. Second, common size birds use *flapping* wings. (Hummingbirds can have over 50 wing beats per second.) These first two types of wings have a thickness of about 10 to 15% of the wing depth. This wing type is shown in the centre of Figure 155.
- 3. At smaller dimensions, a third wing type appears, the *membrane wing*. It is found in dragonflies and most everyday insects. At these scales, at Reynolds numbers of around 1000 and below, thin *membrane* wings are the most efficient. The *Reynolds number* measures the ratio between inertial and viscous effects in a fluid. It is defined as

$$Re = \frac{lv\rho}{\eta}$$
(111)

where *l* is a typical length of the system, *v* the speed,  $\rho$  the density and  $\eta$  the dynamic *viscosity* of the fluid.\* A Reynolds number much larger than one is typical for rapid air flow and fast moving water. In fact, the value of the Reynolds number distinguishes a 'rapid' or 'turbulent' flow on the one hand, and a 'slow', 'laminar' or 'viscous' flow on the other. An example of membrane wing is shown on the right-hand side of Figure 155. All the first three wing types are designed for *turbulent* flows.

dy ra ng vi d e a ic v 0 p e t Wh Hy f t

Challenge 152 ny

<sup>\*</sup> The viscosity is the resistance to flow a fluid poses. It is defined by the force *F* necessary to move a layer of surface *A* with respect to a second, parallel one at distance *d*; in short, the (coefficient of) *dynamic viscosity* is defined as  $\eta = d F/A v$ . The unit is 1 kg/s m or 1 Pa s or 1 N s/m<sup>2</sup>, once also called 10 P or 10 poise. In other words, given a horizontal tube, the viscosity determines how strong the pump needs to be to pump the fluid through the tube at a given speed. The viscosity of air 20°C is  $1.8 \times 10^{-5}$  kg/s m or 18 µPa s and increases with temperature. In contrast, the viscosity of liquids decreases with temperature. (Why?) The viscosity of water at 0°C is 1.8 mPa s, at 20°C it is 1.0 mPa s (or 1 cP), and at 40°C is 0.66 mPa s. Hydrogen has a viscosity smaller than 10 µPa s, whereas honey has 25 Pa s and pitch 30 MPa s.

Physicists also use a quantity  $\nu$  called the *kinematic viscosity*. It is defined with the help of the mass density of the fluid as  $\nu = \eta/\rho$  and is measured in m<sup>2</sup>/s, once called 10<sup>4</sup> stokes. The kinematic viscosity of water at 20°C is 1 mm<sup>2</sup>/s (or 1 cSt). One of the smallest values is that of acetone, with 0.3 mm<sup>2</sup>/s; a larger one is glycerine, with 2000 mm<sup>2</sup>/s. Gases range between 3 mm<sup>2</sup>/s and 100 mm<sup>2</sup>/s.

#### 11 BACTERIA, FLIES AND KNOTS



FIGURE 156 The wings of a few types of insects smaller than 1 mm (thrips, *Encarsia, Anagrus, Dicomorpha*) (HortNET).

- 4. The fourth type of wings is found at the smallest possible dimensions, for insects smaller than one millimetre; their wings are not membranes at all, but are optimized for viscous air flow. Typical are the cases of thrips and of parasitic wasps, which can be as small as 0.3 mm. All these small insects have wings which consist of a central *stalk* surrounded by hair. In fact, Figure 156 shows that some species of thrips have wings which look like miniature toilet brushes.
- 5. At even smaller dimensions, corresponding to Reynolds number below 10, nature does not use wings any more, though it still makes use of air transport. In principle, at the smallest Reynolds numbers gravity plays no role any more, and the process of flying merges with that of swimming. However, air currents are too strong compared with the speeds that such a tiny system could realize. No active navigation is then possible any more. At these small dimensions, which are important for the transport through air of spores and pollen, nature uses the air currents for passive transport, making use of special, but fixed shapes.

We summarize: active flying is only possible through shape change. Only two types of shape changes are possible for active flying: that of wings and that of propellers (including turbines). Engineers are studying with intensity how these shape changes have to take place in order to make flying most effective. Interestingly, a similar challenge is posed by

Ref. 230 Ref. 231

Swimming

swimming.

Swimming is a fascinating phenomenon. The Greeks argued that the ability of fish to swim is a proof that water is made of atoms. If atoms would not exist, a fish could not advance through it. Indeed, swimming is an activity that shows that matter cannot be continuous. Studying swimming can thus be quite enlightening. But how exactly do fish swim?

Whenever dolphins, jellyfish, submarines or humans *swim*, they take water with their fins, body, propellers, hands or feet and push it backwards. Due to momentum conser-

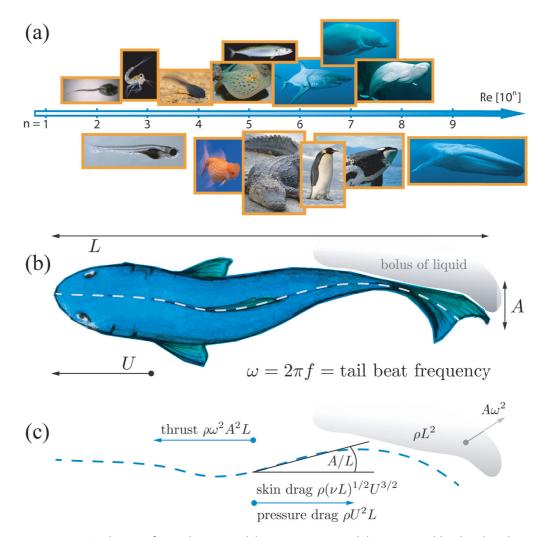


FIGURE 157 A selection of animals using undulatory swimming and the main variables that describe it. Ref. 232 (© L. Mahadevan/Macmillan from )

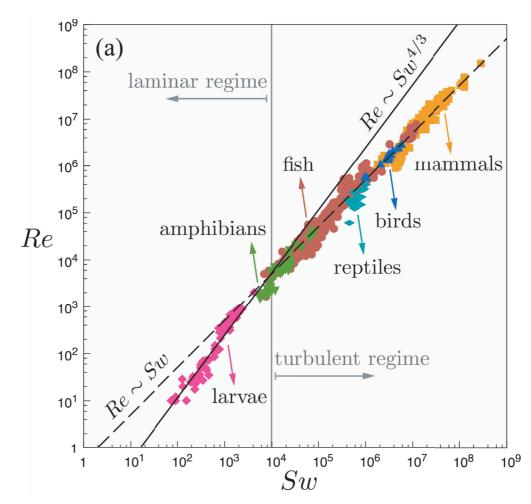
vation they then move forward.\*

Ref. 232

284

Most fish and aquatic mammals swim by bending their bodies and alternating between two extreme deformations. An overview of animals that use this type of swimming – experts call it *undulatory gait* – is given in Figure 157. For all such swimming, the Reynolds number obeys Re = vL/v >> 1; here v is the swimming speed, L the body length and v the kinematic viscocity. The wide range of Reynolds number values observed for swimming living beings is shown in the graph. The swimming motion is best described by the so-called swimming number Sw =  $\omega AL/v$ , where  $\omega$  and A are the circular beat frequency and amplitude. The next graph, Figure 158, shows that for tur-

Vol. I, page 89 \* Fish could use propellers, as the arguments against wheels we collected at the beginning of our walk do not apply for swimming. But propellers with blood supply would be a weak point in the construction, and thus make fish vulnerable. Therefore, nature has not developed fish with propellers.



**FIGURE 158** Undulatory swimming follows simple scaling rules for organisms that range from a few mm to 30 m in length. The Reynolds number *Re* describes the ratio between inertial effects (the water thrown behind) and the disspiative effects (the friction of the water). The swimming number *Sw* describes the body kinematics. (© L. Mahadevan/Macmillan from )

Challenge 153 e

Ref. 234

Ref. 232

bulent swimming, the swimming speed v almost exclusively depends on the amplitude and frequency of the undulatory motion; for smaller organisms that swim in the laminar regime, the swimming speed also depends on the length of the organism. In short, fish, dolphins, submarines and people swim in the same way that fireworks

or rockets fly: by throwing matter behind them, through lift. Lift-based propulsion is the main type of macroscopic swimming. Do all organisms swim in this way? No. Several organisms swim by expelling water jets, for example cephalopods such as squids. And above all, *small* organisms advancing through the molecules of a liquid use a completely different, *microscopic* way of swimming.

Small organisms such as bacteria do *not* have the capacity to propel or accelerate water against their surroundings. Indeed, the water remains attached around a microorganism without ever moving away from it. Physically speaking, in these cases of swimming the kinetic energy of the water is negligible. In order to swim, unicellular beings thus need to



FIGURE 159 A swimming scallop (here from the genus *Chlamys*) (© Dave Colwell).

use other effects. In fact, their only possibility is to change their body shape in controlled ways. Seen from far away, the swimming of microorganisms thus resembles the motion of particles through vacuum: like microorganisms, also particles have nothing to throw behind\* them.

A good way to distinguish macroscopic from microscopic swimming is provided by scallops. *Scallops* are molluscs up to a few cm in size; an example is shown in Figure 159. Scallops have a double shell connected by a hinge that they can open and close. If they close it *rapidly*, water is expelled and the mollusc is accelerated; the scallop then can glide for a while through the water. Then the scallop opens the shell again, this time *slowly*, and repeats the feat. When swimming, the larger scallops look like clockwork false teeth. Scallops thus use a macroscopic swimming process.

If we reduce the size of the scallop by a thousand times to the size of a single cell we get a simple result: such a tiny scallop *cannot* swim. The lack of scalability of swimming methods is due to the changing ratio between inertial and dissipative effects at different scales. This ratio is measured by the *Reynolds number Re*. For the scallop the Reynolds number, is defined as  $Re = vL/\eta$ , where v is the relative speed between swimmer and water, L the length of the swimmer and  $\eta$  is the *kinematic viscosity* of the water, around  $1 \text{ mm}^2/\text{s}$ .

For the scallop, the Reynolds number is about 100, which shows that when it swims, inertial effects are much more important than dissipative, viscous effects. For a bacterium the Reynolds number is much smaller than 1, so that inertial effects effectively play no role. There is no way to accelerate water *away* from a bacterial-sized scallop, and thus no way to glide. Bacteria *cannot* swim like scallops or people do; bacteria cannot throw water behind them. And this is not the only problem microorganism face when they want to swim.

A well-known mathematical theorem states that no cell-sized being can move if the shape change is the same in the two halves of the motion, i.e., when opening and closing are just the inverse of each other. Such a shape change would simply make it move back and forward. Another mathematical theorem, the so-called *scallop theorem*, that states

Vol. I, page 429

Ref. 233

<sup>\*</sup> There is an exception: gliding bacteria move by secreting slime, even though it is still not fully clear why this leads to motion.

Ref. 235

that no microscopic system can swim if it uses movable parts with only *one* degree of freedom. Thus it is impossible to move, at cell dimensions, using the method that the scallop uses on centimetre scale.

In order to swim, microorganisms thus need to use a more evolved, *two-dimensional motion* of their shape. Indeed, biologists found that all microorganisms use one of the following four swimming styles:

- 1. Microorganisms of compact shape of diameter between 20  $\mu$ m and about 20 mm, use *cilia*. Cilia are hundreds of little hairs on the surface of the organism. Some organisms have cilia across their full surface, other only on part of it. These organisms move the cilia in waves wandering around their surface, and these surface waves make the body advance through the fluid. All children watch with wonder *Paramecium*, the unicellular animal they find under the microscope when they explore the water in which some grass has been left for a few hours. *Paramecium*, which is between 100  $\mu$ m and 300  $\mu$ m in size, as well as many plankton species<sup>\*</sup> use cilia for its motion. The cilia and their motion are clearly visible in the microscope. A similar swimming method is even used by some large animals; you might have seen similar waves on the borders of certain ink fish; even the motion of the manta (partially) belongs into this class. Ciliate motion is an efficient way to change the shape of a body making use of two dimensions and thus avoiding the scallop theorem.
- 2. Sperm and eukaryote microorganisms whose sizes are in the range between  $1 \, \mu m$ and 50 µm swim using an (eukaryote) flagellum.\*\* Flagella, Latin for 'small whips', work like flexible oars. Even though their motion sometimes appears to be just an oscillation, flagella get a kick only during one half of their motion, e.g. at every swing to the left. Flagella are indeed used by the cells like miniature oars. Some cells even twist their flagellum in a similar way that people rotate an arm. Some microorganisms, such as Chlamydomonas, even have two flagella which move in the same way as people move their legs when they perform the breast stroke. Most cells can also Ref. 237 change the sense in which the flagellum is kicked, thus allowing them to move either forward or backward. Through their twisted oar motion, bacterial flagella avoid re-Ref 238 tracing the same path when going back and forward. As a result, the bacteria avoid the scallop theorem and manage to swim despite their small dimensions. The flexible oar motion they use is an example of a non-adiabatic mechanism; an important fraction of the energy is dissipated.
- 3. The smallest swimming organisms, bacteria with sizes between 0.2 μm and 5 μm, swim using *bacterial* flagella. These flagella, also called prokaryote flagella, are different from the ones just mentioned. Bacterial flagella move like turning corkscrews. They are used by the famous *Escherichia coli* bacterium and by all bacteria of the genus *Salmonella*. This type of motion is one of the prominent exceptions to the non-existence of wheels in nature; we mentioned it in the beginning of our walk. Corkscrew motion is an example of an adiabatic mechanism.

A Coli bacterium typically has a handful of flagella, each about 30 nm thick and of corkscrew shape, with up to six turns; the turns have a 'wavelength' of  $2.3 \,\mu$ m. Each

<sup>\*</sup> See the www.liv.ac.uk/ciliate website for an overview.

Ref. 236 \*\* The largest sperm, of 5.8 cm length, are produced by the 1.5 mm sized *Drosophila bifurca* fly, a relative of the famous *Drosophila melanogaster*.

flagellum is turned by a sophisticated rotation motor built into the cell, which the cell can control both in rotation direction and in angular velocity. For Coli bacteria, the range is between 0 and about 300 Hz.

A turning flagellum does not propel a bacterium like a propeller; as mentioned, the velocities involved are much too small, the Reynolds number being only about  $10^{-4}$ . At these dimensions and velocities, the effect is better described by a corkscrew turning in honey or in cork: a turning corkscrew produces a motion against the material around it, in the direction of the corkscrew axis. The flagellum moves the bacterium in the same way that a corkscrew moves the turning hand with respect to the cork.

4. One group of bacteria, the spirochaetes, move as a whole like a cork-screw through water. An example is *Rhodospirillum rubrum*, whose motion can be followed in the video on www.microbiologybytes.com/video/motility.com. These bacteria have an internal motor round an axial filament, that changes the cell shape in a non-symmetrical fashion and yield cork-screw motion. A different bacterium is *Spiroplasma*, a helical bacterium – but not a spirochaete – that changes the cell shape, again in a non-symmetrical fashion, by propagating kink pairs along its body surface. Various other microorganisms move by changing their body shape.

To test your intuition, you may try the following puzzle: is microscopic swimming possible in two spatial dimensions? In four?

By the way, still smaller bacteria do not swim at all. Indeed, each bacterium faces a minimum swimming speed requirement: it must outpace diffusion in the liquid it lives Ref. 242 in. Slow swimming capability makes no sense; numerous microorganisms therefore do not manage or do not swim at all. Some microorganisms are specialized to move along liquid-air interfaces. In fact, there are many types of interfacial swimming, including macroscopic types, but we do not cover them here. Other microorganisms attach themselves to solid bodies they find in the liquid. Some of them are able to *move* along these solids. The amoeba is an example for a microorganism moving in this way. Also the smallest active motion mechanisms known, namely the motion of molecules in muscles and in cell membranes, work this way.

Let us summarize these observations. All known active motion, or self-propulsion, (in flat space) takes place in fluids – be it air or liquids. All active motion requires shape change. Macroscopic swimming works by accelerating the fluid in the direction opposite to the direction of motion. Microscopic swimming works through smart shape change that makes the swimmer advance through the fluid. In order that shape change leads to motion, the environment, e.g. the fluid, must itself consist of moving components always pushing onto the swimming entity. The motion of the swimming entity can then be deduced from the particular shape change it performs. The mathematics of swimming through shape change is fascinating; it deserves to be explored.

# ROTATION, FALLING CATS AND THE THEORY OF SHAPE CHANGE

At small dimensions, flying and swimming takes place through shape change. In the last decades, the description of shape change has changed from a fashionable piece of research to a topic whose results are both appealing and useful. There are many studies, both experimental and theoretical, about the exact way small systems move in water and

Ref. 240

Ref 241

Challenge 154 s

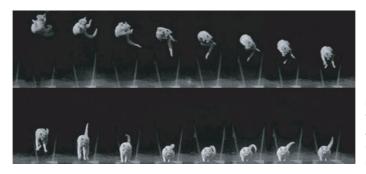


FIGURE 160 Cats can turn themselves, even with *no* initial angular momentum (photographs by Etienne-Jules Marey, 1894).

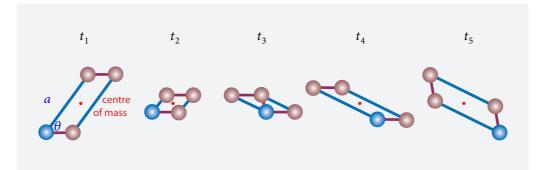


FIGURE 161 Humans can turn themselves in mid air like cats: see the second, lateral rotation of Artem Silchenko, at the 2006 cliff diving world championship (© World High Diving Federation).

air, about the achievable and achieved efficiency, and much more.

It is not a surprise that organized shape change can lead to *translational motion*. Amoebas, earthworms, caterpillars, snakes, and even human themselves move though shape change.

But shape change can also lead to a *rotation* of a body. In this case, the ideas are not restricted to microscopic systems, but apply at all scales. In particular, the theory of shape change is useful in explaining how falling cats manage to fall always on their feet. Cats are not born with this ability; they have to learn it. But the feat has fascinated people for



**FIGURE 162** The square cat: in free space, or also on perfect ice, a deformable body in the shape of a parallelogram made of four masses and rods that is able to change the body angle  $\theta$  and two rod lengths *a* is able to rotate itself around the centre of mass without outside help. One mass and the length-changing rods are coloured to illustrate the motion.

centuries, as shown in the old photograph given in Figure 160. In fact, cats confirm in Vol. I, page 120 three dimensions what we already knew for two dimensions:

▷ A deformable body can change its own orientation in space *without* outside help.

This is in strong contrast to translation, for which outside help is always needed. Archimedes famously said: Give me a place to stand, and I'll move the Earth. But to *rotate* the Earth, a place to stand is *not* needed!

Not only cats, also humans can perform the feat: simply observe the second, lateral rotation of the diver in Figure 161. Cosmonauts in space stations and passengers of parabolic 'zero-gravity' flights regularly do the same, as do many artificial satellites sent into space.

In the 1980s, the work by Berry, Wilczek, Zee and ShapereBerry, MichaelWilczek, FrankZee, AnthonyShapere, Alfred showed that all motion due to shape change is described by a gauge theory. The equivalence between the two situations is detailed in

Ref. 243 Ref. 244 scribed by a gauge theory. The equivalence between the two situations is detailed in Table 24. A simple and beautiful example for these ideas has been given by Putterman and Raz and is illustrated in Figure 162. Imagine four spheres on perfect ice, all of the same mass and size, connected by four rods forming a parallelogram. Now imagine that this parallelogram, using some built-in motors, can change length along one side, called *a*, and that it can also change the angle  $\theta$  between the sides. Putterman and Raz call this the *square cat*. The figure shows that the square cat can change its own orientation on the ice while, obviously, keeping its centre of mass at rest. The figure also shows that the change of orientation only works because the two motions that the cat can perform, the stretching and the angle change, do *not* commute. The order in which these deformations occur is essential for achieving the desired rotation.

The rotation of the square cat occurs in *strokes*; large rotations are achieved by repeating strokes, similar to the situation of swimmers. If the square cat would be swimming in a liquid, the cat could thus rotate itself – though it could not advance.

When the cat rotates itself, each stroke results in a rotation angle that is independent

Challenge 155 d

C o n c e p t	Shape change	GAUGE THEORY
System	deformable body	matter-field combination
Gauge freedom	freedom of description of body orientation and position	freedom to define vector potential
Gauge-dependent quantity	shape's angular orientation and position	vector potential, phase
	orientation and position change along an open path	vector potential and phase change along open path
Gauge transformation	changes angular orientation and position	changes vector potential
Gauge-independent quantities	orientation and position after full stroke	phase difference on closed path, integral of vector potential along a closed path
	deformations	field strengths
Gauge group	e.g. possible rotations SO(3) or motions E(3)	U(1), SU(2), SU(3)

TABLE 24 The correspondence between shape change and gauge theory.

of the speed of the stroke. The same experience can be made when rotating oneself on an office chair by rotating the arm above the head: the chair rotation angle after arm turn is independent of the arm speed. Stroke motion leads to a puzzle: what is the largest angle that a cat can turn in one stroke?

Rotation in strokes has a number of important implications. First of all, the number of strokes is a quantity that all observers agree upon: it is observer-invariant. Secondly, the orientation change after a *complete* stroke is also observer-invariant. Thirdly, the orientation change for *incomplete* strokes is observer-dependent: it depends on the way that orientation is defined. For example, if orientation is defined by the direction of the body diagonal through the black mass (see Figure 162), it changes in a certain way during a stroke. If the orientation is defined by the direction of the black mass, it changes in a different way during a stroke. Only when a full stroke is completed do the two values coincide. Mathematicians say that the choice of the definition and thus the value of the orientation is *gauge-dependent*, but that the value of the orientation change at a full stroke is *gauge-invariant*.

In summary, the square cat shows three interesting points. First, already rather simple deformable bodies can change their orientation in space. Secondly, the orientation of a deformable body can only change if the deformations it can perform are *non-commuting*. Thirdly, such deformable bodies are described by *gauge theories*: certain aspects of the bodies are gauge-invariant, others are gauge-dependent. This summary leads to a question: Can we use these ideas to increase our understanding of the gauge theories of the electromagnetic, weak and strong interaction? Shapere and Wilczek say no. We will explore this issue in the next volume. In fact, shape change bears even more surprises.

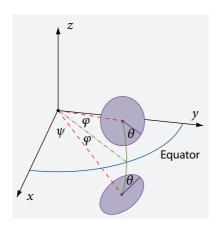


FIGURE 163 Swimming on a curved surface using two discs.

#### SWIMMING IN CURVED SPACE

In flat space it is not possible to produce translation through shape change. Only orientation changes are possible. Surprisingly, if space is *curved*, motion does become possible. A simple example was published in 2003 by Jack Wisdom. He found that cyclic changes in the shape of a body can lead to net translation, a rotation of the body, or both.

Indeed, we know from Galilean physics that on a frictionless surface we cannot move, but that we can change orientation. This is true only for a flat surface. On a curved surface, we can use the ability to turn and translate it into motion.

Take two massive discs that lie on the surface of a frictionless, spherical planet, as shown in Figure 163. Consider the following four steps: 1. the disc separation  $\varphi$  is increased by the angle  $\Delta \varphi$ , 2. the discs are rotated oppositely about their centres by the angle  $\Delta \theta$ , 3. their separation is decreased by  $-\Delta \varphi$ , and 4. they are rotated back by  $-\Delta \theta$ . Due to the conservation of angular momentum, the two-disc system changes its longitude  $\Delta \psi$  as

$$\Delta \psi = rac{1}{2} \gamma^2 \Delta \theta \Delta \varphi$$
 ,

where  $\gamma$  is the angular radius of the discs. This cycle can be repeated over and over. The cycle allows a body, located on the surface of the Earth, to swim along the surface. Unfortunately, for a body of size of one metre, the motion for each swimming cycle is only around  $10^{-27}$  m.

Wisdom showed that the same procedure also works in curved space, thus in the presence of gravitation. The mechanism thus allows a falling body to swim away from the path of free fall. Unfortunately, the achievable distances for everyday objects are negligibly small. Nevertheless, the effect exists.

In other words, there is a way to swim through curved space that looks similar to swimming at low Reynolds numbers, where swimming results of simple shape change. Does this tell us something about fundamental descriptions of motion? The last part of our ascent will tell.

(112)

Ref. 245

Challenge 156 ny



FIGURE 164 A way to turn a sphere inside out, with intermediate steps ordered clockwise (© John Sullivan).

#### TURNING A SPHERE INSIDE OUT

A text should be like a lady's dress; long enough to cover the subject, yet short enough to keep it interesting. Anonymous

Ref. 246

Ref. 247, Ref. 248

Exploring the theme of motion of wobbly entities, a famous example cannot be avoided. In 1957, the mathematician Stephen Smale proved that a sphere can be turned inside out. The discovery brought him the Fields medal in 1966, the highest prize for discoveries in mathematics. Mathematicians call his discovery the *eversion* of the sphere.

To understand the result, we need to describe more clearly the rules of mathematical eversion. First of all, it is assumed that the sphere is made of a thin membrane which has the ability to stretch and bend without limits. Secondly, the membrane is assumed to be able to *intersect* itself. Of course, such a ghostly material does not exist in everyday life; but in mathematics, it can be imagined. A third rule requires that the membrane must be deformed in such a way that the membrane is not punctured, ripped nor creased; in short, everything must happen *smoothly* (or differentiably, as mathematicians like to say).

Even though Smale proved that eversion is possible, the first way to actually perform it was discovered by the blind topologist Bernard Morin in 1961, based on ideas of Arnold Shapiro. After him, several additional methods have been discovered. Ref. 249 Several computer videos of sphere eversions are now available.\* The most famous ones are *Outside in*, which shows an eversion due to William P. Thurston, and *The Optiverse*, which shows the most efficient method known so far, discovered by a team led by John Sullivan and shown in Figure 164.

Why is sphere eversion of interest to physicists? If elementary particles were extended and at the same time were of spherical shape, eversion might be a particle symmetry. To see why, we summarize the effects of eversion on the whole surrounding space, not only on the sphere itself. The final effect of eversion is the transformation

$$(x, y, z) \to \frac{(x, y, -z) R^2}{r^2}$$
 (113)

where *R* is the radius of the sphere and *r* is the length of the coordinate vector (x, y, z), thus  $r = \sqrt{x^2 + y^2 + z^2}$ . Due to the minus sign in the *z*-coordinate, eversion differs from inversion, but not by too much. As we will find out in the last part of our adventure, a transformation similar to eversion, space-time duality, is a fundamental symmetry of nature.

### CLOUDS

Clouds are another important class of wobbly objects. The lack of a definite boundary makes them even more fascinating than amoebas, bacteria or falling cats. We can observe the varieties of clouds from any aeroplane.

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Vol. VI, page 114

The common cumulus or cumulonimbus in the sky, like all the other meteorological clouds, are vapour and water droplet clouds. Galaxies are clouds of stars. Stars are clouds of plasma. The atmosphere is a gas cloud. Atoms are clouds of electrons. Nuclei are clouds of protons and neutrons, which in turn are clouds of quarks. Comparing different cloud types is illuminating and fun.

Clouds of all types can be described by a shape and a size, even though in theory they have no bound. An *effective* shape and size can be defined by that region in which the cloud density is only, say, 1% of the maximum density; slightly different procedures can also be used. All clouds are described by *probability densities* of the components making up the cloud. All clouds show *conservation* of the number of their constituents.

Vol. I, page 257

Whenever we see a cloud, we can ask why it does not collapse. Every cloud is an aggregate; all aggregates are kept from collapse in only *three* ways: through rotation, through pressure, or through the Pauli principle, i.e., the quantum of action. For example, galaxies are kept from collapsing by rotation. Most stars, the atmosphere and rain clouds are kept from collapsing by gas pressure. Neutron stars, the Earth, atomic nuclei, protons or the electron clouds of atoms are kept apart by the quantum of action.

A rain cloud is a method to keep several thousand tons of water suspended in the air. Can you explain what keeps it afloat, and what else keeps it from continuously diffusing

<sup>\*</sup> Summaries of the videos can be seen at the website www.geom.umn.edu/docs/outreach/oi, which also has a good pedagogical introduction. Another simple eversion and explanation is given by Erik de Neve on his website www.usefuldreams.org/sphereev.htm. It is even possible to run the eversion film software at home; see the website www.cslub.uwaterloo.ca/~mjmcguff/eversion. Figure 164 is from the website new. math.uiuc.edu/optiverse.

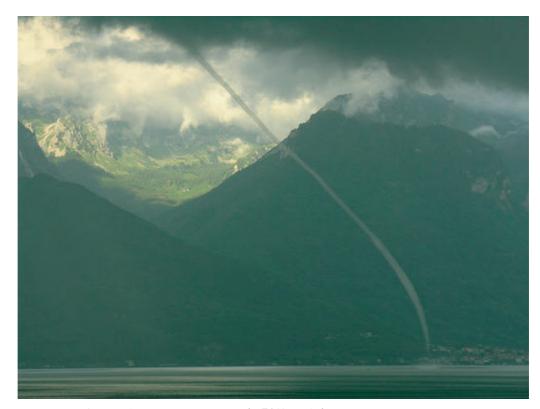


FIGURE 165 A vortex in nature: a waterspout (© Zé Nogueira).

Challenge 157 s into a thinner and thinner structure?

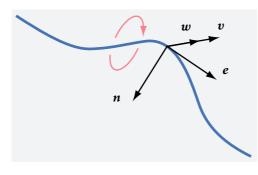
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Two rain clouds can merge. So can two atomic electron clouds. So can galaxies. But only atomic clouds are able to *cross* each other. We remember that a normal atom can be inside a Rydberg atom and leave it again without change. In contrast, rain clouds, stars, galaxies or other macroscopic clouds cannot cross each other. When their paths cross, they can only merge or be ripped into pieces. Due to this lack of crossing ability, only microscopic clouds can be counted. In the macroscopic cases, there is no real way to define a 'single' cloud in an accurate way. If we aim for full precision, we are unable to claim that there is more than one rain cloud, as there is no clear-cut boundary between them. Electronic clouds are different. True, in a piece of solid matter we can argue that there is only a single electronic cloud throughout the object; however, when the object is divided, the cloud is divided in a way that makes the original atomic clouds reappear. We thus can speak of 'single' electronic clouds.

If one wants to be strict, galaxies, stars and rain clouds can be seen as made of localized particles. Their cloudiness is only apparent. Could the same be true for electron clouds? And what about space itself? Let us explore some aspects of these questions.

# VORTICES AND THE SCHRÖDINGER EQUATION

Fluid dynamics is a topic with many interesting aspects. Take the *vortex* that can be observed in any deep, emptying bath tub: it is an extended, one-dimensional 'object', it is



**FIGURE 166** The mutually perpendicular tangent e, normal n, torsion w and velocity v of a vortex in a rotating fluid.

deformable, and it is observed to wriggle around. Larger vortices appear as tornadoes on Earth and on other planets, as *waterspouts*, and at the ends of wings or propellers of all kinds. Smaller, quantized vortices appear in superfluids. An example is shown in Figure 165; also the spectacular fire whirls and fire tornados observed every now and then are vortices.

Ref. 250 a b

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Vortices, also called *vortex tubes* or *vortex filaments*, are thus wobbly entities. Now, a beautiful result from the 1960s states that a vortex filament in a rotating liquid is described by the one-dimensional Schrödinger equation. Let us see how this is possible.

Any deformable linear vortex, as illustrated in Figure 166, is described by a continuous set of position vectors  $\mathbf{r}(t, s)$  that depend on time t and on a single parameter s. The parameter s specifies the relative position along the vortex. At each point on the vortex, there is a unit tangent vector  $\mathbf{e}(t, s)$ , a unit normal curvature vector  $\mathbf{n}(t, s)$  and a unit torsion vector  $\mathbf{w}(t, s)$ . The three vectors, shown in Figure 166, are defined as usual as

$$e = \frac{\partial r}{\partial s},$$
  

$$\kappa n = \frac{\partial e}{\partial s},$$
  

$$\tau w = -\frac{\partial (e \times n)}{\partial s},$$
(114)

where  $\kappa$  specifies the value of the curvature and  $\tau$  specifies the value of the torsion. In general, both numbers depend on time and on the position along the line.

In the simplest possible case the rotating environment induces a local velocity v for the vortex that is proportional to the curvature  $\kappa$ , perpendicular to the tangent vector e and perpendicular to the normal curvature vector n:

$$\boldsymbol{v} = \eta \kappa (\boldsymbol{e} \times \boldsymbol{n}) , \qquad (115)$$

Ref. 250

50 where  $\eta$  is the so-called *coefficient of local self-induction* that describes the coupling between the liquid and the vortex motion. This is the evolution equation of the vortex.

We now assume that the vortex is deformed only *slightly* from the straight configuration. Technically, we are thus in the *linear* regime. For such a linear vortex, directed along

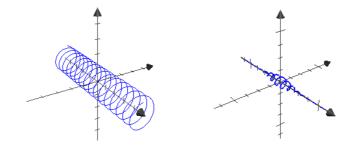


FIGURE 167 Motion of a vortex: the fundamental helical solution and a moving helical 'wave packet'.

the *x*-axis, we can write

$$\mathbf{r} = (x, y(x, t), z(x, t))$$
 (116)

Slight deformations imply  $\partial s \approx \partial x$  and therefore

$$\boldsymbol{e} = (1, \frac{\partial y}{\partial x}, \frac{\partial z}{\partial x}) \approx (1, 0, 0) ,$$
  

$$\kappa \boldsymbol{n} \approx (0, \frac{\partial^2 y}{\partial x^2}, \frac{\partial^2 z}{\partial x^2}) , \text{ and}$$
  

$$\boldsymbol{v} = (0, \frac{\partial y}{\partial t}, \frac{\partial z}{\partial t}) . \qquad (117)$$

We can thus rewrite the evolution equation (115) as

$$(0, \frac{\partial y}{\partial t}, \frac{\partial z}{\partial t}) = \eta \left(0, -\frac{\partial^2 z}{\partial x^2}, \frac{\partial^2 y}{\partial x^2}\right).$$
(118)

This equation is well known; if we drop the first coordinate and introduce complex numbers by setting  $\Phi = y + iz$ , we can rewrite it as

$$\frac{\partial \Phi}{\partial t} = i\eta \frac{\partial^2 \Phi}{\partial x^2} . \tag{119}$$

Ref. 251

This is the one-dimensional Schrödinger equation for the evolution of a free wave function! The complex function  $\Phi$  specifies the transverse deformation of the vortex. In other words, we can say that the Schrödinger equation in one dimension describes the evolution of the deformation for an almost linear vortex in a rotating liquid. We note that there is no constant  $\hbar$  in the equation, as we are exploring a *classical* system. Schrödinger's equation is linear in  $\Phi$ . Therefore the fundamental solution is

$$\Phi(x, y, z, t) = a e^{i(\tau x - \omega t)} \quad \text{with} \quad \omega = \eta \tau^2 \quad \text{and} \quad \kappa = a \tau^2 .$$
(120)

The amplitude *a* and the wavelength or pitch  $b = 1/\tau$  can be freely chosen, as long as the approximation of small deviation is fulfilled; this condition translates as  $a \ll b$ .\* In the present interpretation, the fundamental solution corresponds to a vortex line that is deformed into a *helix*, as shown in Figure 167. The angular speed  $\omega$  is the rotation speed around the axis of the helix.

A helix moves along the axis with a speed given by

$$v_{\text{helix along axis}} = 2\eta\tau . \tag{121}$$

In other words, for extended entities following evolution equation (115), rotation and translation are coupled.\*\* The momentum *p* can be defined using  $\partial \Phi / \partial x$ , leading to

$$p = \tau = \frac{1}{b} . \tag{122}$$

Momentum is thus inversely proportional to the helix wavelength or pitch, as expected. The energy *E* is defined using  $\partial \Phi / \partial t$ , leading to

$$E = \eta \tau^2 = \frac{\eta}{b^2} \,. \tag{123}$$

Energy and momentum are connected by

$$E = \frac{p^2}{2\mu} \quad \text{where} \quad \mu = \frac{1}{2\eta} \,. \tag{124}$$

In other words, a vortex with a coefficient  $\eta$  – describing the coupling between environ-Page 296 ment and vortex – is thus described by a number  $\mu$  that behaves like an effective mass. We can also define the (real) quantity  $|\Phi| = a$ ; it describes the *amplitude* of the deformation.

In the Schrödinger equation (119), the second derivative implies that the deformation 'wave packet' has tendency to spread out over space. Can you confirm that the wavelength-frequency relation for a vortex wave group leads to something like the indeterminacy relation (however, without a  $\hbar$  appearing explicitly)?

In summary, the complex amplitude  $\Phi$  for a linear vortex in a rotating liquid behaves like the one-dimensional wave function of a non-relativistic free particle. In addition, we found a suggestion for the reason that complex numbers appear in the Schrödinger equation of quantum theory: they could be due to the intrinsic rotation of an underlying substrate. Is this suggestion correct? We will find out in the last part of our adventure.

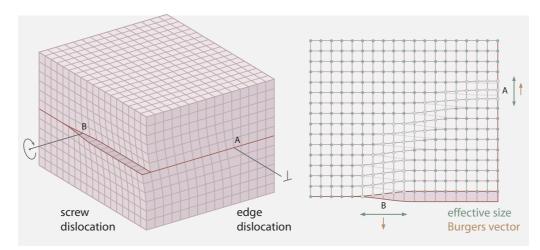
Vol. VI, page 174

Challenge 160 ny

Challenge 158 ny

Challenge 159 ny

<sup>\*</sup> The curvature is given by  $\kappa = a/b^2$ , the torsion by  $\tau = 1/b$ . Instead of  $a \ll b$  one can thus also write  $\kappa \ll \tau$ . \*\* A wave packet moves along the axis with a speed given by  $v_{\text{packet}} = 2\eta\tau_0$ , where  $\tau_0$  is the torsion of the helix of central wavelength.



**FIGURE 168** The two pure dislocation types, edge and screw dislocations, seen from the outside of a cubic crystal (left) and the mixed dislocation – a quarter of a dislocation loop – joining them in a horizontal section of the same crystal (right) (© Ulrich Kolberg).

## FLUID SPACE-TIME

General relativity shows that space can move and oscillate: space is a wobbly entity. Is space more similar to clouds, to fluids, or to solids?

An intriguing approach to space-time as a fluid was published in 1995 by Ted Jacobson. He explored what happens if space-time, instead of assumed to be continuous, is assumed to be the statistical average of numerous components moving in a disordered fashion.

The standard description of general relativity describes space-time as an entity similar to a flexible mattress. Jacobson studied what happens if the mattress is assumed to be made of a fluid. A fluid is a collection of (undefined) components moving randomly and described by a temperature varying from place to place.

Jacobson started from the Fulling–Davies–Unruh effect and assumed that the local fluid temperature is given by a multiple of the local gravitational acceleration. He also used the proportionality – correct on horizons – between area and entropy. Since the energy flowing through a horizon can be called heat, one can thus translate the expression  $\delta Q = T\delta S$  into the expression  $\delta E = a\delta A(c^2/4G)$ , which describes the behaviour of space-time at horizons. As we have seen, this expression is fully equivalent to general relativity.

In other words, imagining space-time as a fluid is a powerful analogy that allows deducing general relativity. Does this mean that space-time actually *is* similar to a fluid? So far, the analogy is not sufficient to answer the question and we have to wait for the last part of our adventure to settle it. In fact, just to confuse us a bit more, there is an old argument for the opposite statement.

# DISLOCATIONS AND SOLID SPACE-TIME

General relativity tells us that space behaves like a deformable mattress; space thus behaves like a solid. There is a second argument that underlines this point and that exerts a

Vol. II, page 144

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Ref. 252

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continuing fascination. This argument is connected to a famous property of the motion of dislocations.

*Dislocations* are one-dimensional construction faults in crystals, as shown in Figure 168. A general dislocation is a mixture of the two pure dislocation types: *edge dislocations* and *screw dislocations*. Both are shown in Figure 168.

If one explores how the atoms involved in dislocations can rearrange themselves, one finds that edge dislocations can only move perpendicularly to the added plane. In contrast, screw dislocations can move in all directions.\* An important case of general, mixed dislocations, i.e., of mixtures of edge and screw dislocations, are closed *dislocation rings*. On such a dislocation ring, the degree of mixture changes continuously from place to place.

Any dislocation is described by its *strength* and by its effective *size*; they are shown, respectively, in red and blue in Figure 168. The *strength* of a dislocation is measured by the so-called *Burgers vector*; it measures the misfits of the crystal around the dislocation. More precisely, the Burgers vector specifies by how much a section of perfect crystal needs to be displaced, after it has been cut open, to produce the dislocation. Obviously, the strength of a dislocation is quantized in multiples of a minimal Burgers vector. In fact, dislocations with large Burgers vectors can be seen as composed of dislocations of minimal Burgers vector, so that one usually studies only the latter.

The size or *width* of a dislocation is measured by an *effective width w*. Also the width is a multiple of the lattice vector. The width measures the size of the deformed region of the crystal around the dislocation. Obviously, the size of the dislocation depends on the elastic properties of the crystal, can take continuous values and is direction-dependent. The width is thus related to the energy content of a dislocation.

A general dislocation can move, though only in directions which are both perpendicular to its own orientation and to its Burgers vector. Screw dislocations are simpler: they can move in any direction. Now, the motion of screw dislocations has a peculiar property. We call *c* the speed of sound in a pure (say, cubic) crystal. As Frenkel and Kontorowa found in 1938, when a screw dislocation moves with velocity *v*, its width *w* changes as

$$w = \frac{w_0}{\sqrt{1 - v^2/c^2}} \,. \tag{125}$$

In addition, the energy of the moving dislocation obeys

$$E = \frac{E_0}{\sqrt{1 - v^2/c^2}} \,. \tag{126}$$

A screw dislocation thus cannot move faster than the speed of sound *c* in a crystal and its width shows a speed-dependent contraction. (Edge dislocations have similar, but more complex behaviour.) The motion of screw dislocations in solids is thus described by the same effects and formulae that describe the motion of bodies in special relativity; the

## Challenge 161 e

<sup>\*</sup> See the uet.edu.pk/dmems/edge\_dislocation.htm, uet.edu.pk/dmems/screw\_dislocation.htm and uet.edu.pk/dmems/mixed\_dislocation.htm web pages to watch a moving dislocation.

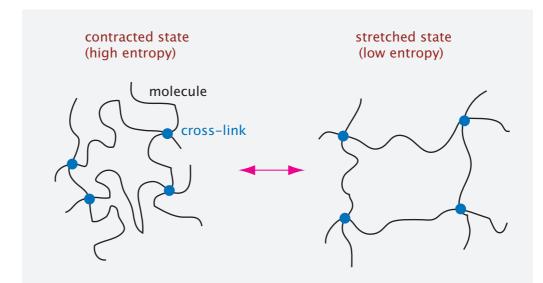


FIGURE 169 An illustration of the relation between polymer configurations and elasticity. The molecules in the stretched situation have fewer possible shape configurations and thus lower entropy; therefore, the material tends back to the contracted situation.

speed of sound is the limit speed for dislocations in the same way that the speed of light is the limit speed for objects.

Does this mean that elementary particles are dislocations of space or even of spacetime, maybe even dislocation rings? The speculation is appealing, even though it supposes that space-time is a solid crystal, and thus contradicts the model of space or spacetime as a fluid. Worse, we will soon encounter other reasons to reject modelling spacetime as a lattice; maybe you can find a few arguments already by yourself. Still, expressions (125) and (126) for dislocations continue to fascinate.

At this point, we are confused. Space-time seems to be solid and liquid at the same time. Despite this contrast, the discussion somehow gives the impression that there is something waiting to be discovered. But what? We will find out in the last part of our adventure.

## Polymers

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Challenge 162 s

Ref. 254 The study of polymers is both economically important and theoretically fascinating. Polymers are materials built of long and flexible macromolecules that are sequences of many ('poly' in Greek) similar monomers. These macromolecules are thus wobbly entities.

Polymers form *solids*, like rubber or plexiglas, *melts*, like those used to cure teeth, and many kinds of *solutions*, like glues, paints, eggs, or people. Polymer gases are of lesser importance.

All the material properties of polymers, such as their elasticity, their viscosity, their electric conductivity or their unsharp melting point, depend on the number of monomers and the topology of their constituent molecules. In many cases, this depend-

ence can be calculated. Let us explore an example.

If *L* is the contour length of a free, ideal, unbranched polymer molecule, the *average* end-to-end distance *R* is proportional to the square root of the length *L*:

$$R = \sqrt{Ll} \sim \sqrt{L} \quad \text{or} \quad R \sim \sqrt{N} \tag{127}$$

where N is the number of monomers and l is an effective monomer length describing the scale at which the polymer molecule is effectively stiff. R is usually much smaller than L; this means that free, ideal polymer molecules are usually in a *coiled* state.

Obviously, the end-to-end distance R varies from molecule to molecule, and follows a Gaussian distribution for the probability P of a end-to-end distance R:

$$P(R) \sim e^{\frac{-3R^2}{2Nl^2}}$$
 (128)

The average end-to-end distance mentioned above is the root-mean-square of this distribution. Non-ideal polymers are polymers which have, like non-ideal gases, interactions with neighbouring molecules or with solvents. In practice, polymers follow the ideal behaviour quite rarely: polymers are ideal only in certain solvents and in melts.

If a polymer is *stretched*, the molecules must rearrange. This changes their entropy and produces an elastic force f that tries to inhibit the stretching. For an ideal polymer, the force is not due to molecular interactions, but is entropic in nature. Therefore the force can be deduced from the *free energy* 

$$F \sim -T\ln P(R) \tag{129}$$

of the polymer: the force is then simply given as  $f = \partial F(R)/\partial R$ . For an ideal polymer, using its probability distribution, the force turns out to be proportional to the stretched length. Thus the spring constant *k* can be introduced, given by

$$k = \frac{f}{R} = \frac{3T}{Ll} \,. \tag{130}$$

We thus deduced a material property, the spring constant k, from the simple idea that polymers are made of long, flexible molecules. The proportionality to temperature T is a result of the entropic nature of the force; the dependence on L shows that longer molecules are more easy to stretch. For a real, non-ideal polymer, the calculation is more complex, but the procedure is the same. Indeed, this is the mechanism at the basis of the elasticity of rubber.

Using the free energy of polymer conformations, we can calculate the material properties of macromolecules in many other situations, such as their reaction to compression, their volume change in the melt, their interactions in solutions, the effect of branched molecules, etc. This is a vast field of knowledge on its own, which we do not pursue here. Modern research topics include the study of knotted polymers and the study of polymer mixtures. Extensive computer calculations and experiments are regularly compared.

Do polymers have some relation to the structure of physical space? The issue is open.

Challenge 163 e

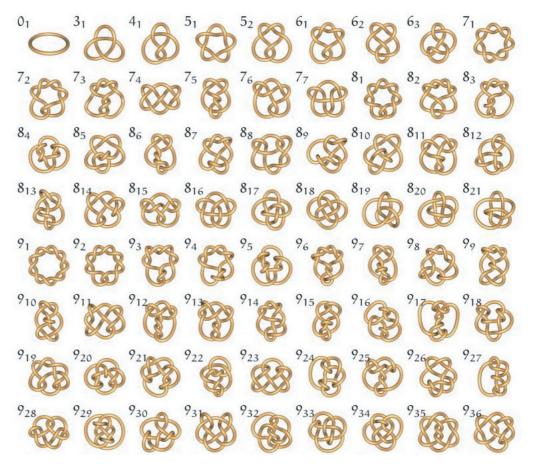


FIGURE 170 The knot diagrams for the simplest prime knots (© Robert Scharein).

It is sure, however, that polymers are often knotted and linked.

# KNOTS AND LINKS

Ref. 255

C Don't touch this, or I shall tie your fingers into knots! (Nasty, but surprisingly efficient child

education technique.)

Knots and their generalization are central to the study of wobbly object motion. A *(mathematical) knot* is a closed piece of rubber string, i.e., a string whose ends have been glued together, which cannot be deformed into a circle or a simple loop. The simple loop is also called the *trivial knot*.

Knots are of importance in the context of this chapter as they visualize the limitations of the motion of wobbly entities. In addition, we will discover other reasons to study knots later on. In this section, we just have a bit of fun.\*

<sup>\*</sup> Beautiful illustrations and detailed information about knots can be found on the Knot Atlas website at katlas.math.toronto.edu and at the KnotPlot website at www.knotplot.com.

Ref. 256

In 1949, Schubert proved that every knot can be decomposed in a unique way as sum of prime knots. Knots thus behave similarly to integers.

If prime knots are ordered by their crossing numbers, as shown in Figure 170, the trivial knot  $(0_1)$  is followed by the trefoil knot  $(3_1)$  and by the figure-eight knot  $(4_1)$ . The figure only shows *prime knots*, i.e., knots that cannot be decomposed into two knots that are connected by two parallel strands. In addition, the figure only shows one of the often possible two mirror versions.

Together with the search for invariants, the tabulation of knots – a result of their classification – is a modern mathematical sport. Flat knot diagrams are usually ordered by the minimal number of crossings as done in Figure 170. There is 1 knot with zero, 1 with three and 1 with four crossings (not counting mirror knots); there are 2 knots with five and 3 with six crossings, 7 knots with seven, 21 knots with eight, 41 with nine, 165 with ten, 552 with eleven, 2176 with twelve, 9988 with thirteen, 46 972 with fourteen, 253 293

The mirror image of a knot usually, but not always, is different from the original. If you want a challenge, try to show that the trefoil knot, the knot with three crossings, is different from its mirror image. The first mathematical proof was by Max Dehn in 1914.

Antiknots do not exist. An *antiknot* would be a knot on a rope that cancels out the corresponding knot when the two are made to meet along the rope. It is easy to prove that this is impossible. We take an infinite sequence of knots and antiknots on a string, K - K + K - K + K - K... On the one hand, we could make them disappear in this way K - K + K - K + K - K... = (K - K) + (K - K) + (K - K)... = 0. On the other hand, we could do the same thing using K - K + K -

with fifteen and 1388705 knots with sixteen crossings.

The only knot *K* with an antiknot is thus the unknot K = 0.\*How do we describe such a knot through the telephone? Mathematicians have spent a lot of time to figure out smart ways to achieve it. The obvious way is to flatten the knot onto a plane and to list the position and the type (below or above) of the crossings. (See Figure 171.) But what is the *simplest* way to describe knots by the telephone? The task is not completely finished, but the end is in sight. Mathematicians do not talk about 'telephone messages', they talk about *knot invariants*, i.e., about quantities that do not depend on the precise shape of the knot. At present, the best description of knots use polynomial invariants. Most of them are based on a discovery by Vaughan Jones in 1984. However, though the Jones polynomial allows us to uniquely describe most simple knots, it fails to do so for more complex ones. But the Jones polynomial finally allowed mathematicians to prove that a diagram which is alternating and eliminates nugatory crossings (i.e., if it is 'reduced') is indeed one which has minimal number of crossings. The polynomial also allows showing that any two reduced alternating diagrams are related by a sequence of flypes.

In short, the simplest way to describe a knot through the telephone is to give its Kauffman polynomial, together with a few other polynomials.

Since knots are stable in time, a knotted line in three dimensions is equivalent to a knotted surface in space-time. When thinking in higher dimensions, we need to be careful. Every knot (or knotted line) can be untied in four or more dimensions. However,

Ref. 256

Ref. 257

<sup>\*</sup> This proof does *not* work when performed with numbers; we would be able to deduce 1 = 0 by setting Challenge 164 s K=1. Why is this proof valid with knots but not with numbers?

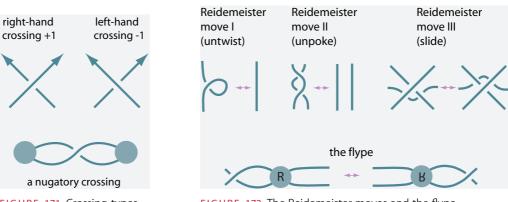


FIGURE 171 Crossing types in knots.

FIGURE 172 The Reidemeister moves and the flype.



FIGURE 173 A tight open overhand knot and a tight open figure-eight knot (© Piotr Pieranski)

there is no surface *embedded* in four dimensions which has as t = 0 slice a knot, and as t = 1 slice the circle. Such a surface embedding needs at least five dimensions.

In higher dimensions, knots are thus possible *only* if n-spheres are tied instead of circles; for example, as just said, 2-spheres can be tied into knots in 4 dimensions, 3-spheres in 5 dimensions and so forth.

## The hardest open problems that you can tell your grandmother

Even though mathematicians have achieved good progress in the classification of knots, surprisingly, they know next to nothing about the *shapes* of knots. Here are a few problems that are still open today:

- This is the simplest unsolved knot problem: Imagine an ideally wobbly rope, that is, a rope that has the same radius everywhere, but whose curvature can be changed as one prefers. Tie a trefoil knot into the rope. By how much do the ends of the rope get nearer? In 2006, there are only numerical estimates for the answer: about 10.1 radiuses. There is no formula yielding the number 10.1. Alternatively, solve the following problem: what is the rope length of a closed trefoil knot? Also in this case, only numerical values are known about 16.33 radiuses but no exact formula. The same is valid for any other knot, of course.
- For mathematical knots, i.e., *closed* knots, the problem is equally unsolved. For example: the ropelength of the tight trefoil knot is known to be around 16.33 diameters, and that of the figure-eight knot about 21.04 diameters. For beautiful visualizations of

Challenge 165 r

Ref. 259

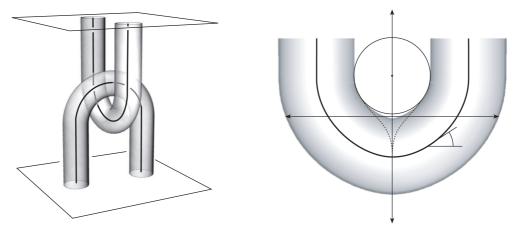


FIGURE 174 The ropelength problem for the simple clasp, and the candidate configuration that probably minimizes ropelength, leaving a gap between the two ropes (© Jason Cantarella).

the tightening process, see the animations on the website www.jasoncantarella.com/ movs. But what is the formula giving the ropelength values? Nobody knows, because the precise shape of the trefoil knot – or of any other knot – is unknown. Lou Kauffman has a simple comment for the situation: 'It is a scandal of mathematics!'

— Mathematicians also study more general structures than knots. *Links* are the generalization of knots to several closed strands. *Braids* and *long links* are the generalization of links to *open* strands. Now comes the next surprise, illustrated in Figure 174. Even for two ropes that form a simple *clasp*, i.e., two linked letters 'U', the ropelength problem is unsolved – and there is not even a knot involved! In fact, in 2004, Jason Cantarella and his colleagues have presented a candidate for the shape that minimizes ropelength. Astonishingly, the candidate configuration leaves a small gap between the two ropes, as shown in Figure 174.

In short, the shape of knots is a research topic that has barely taken off. Therefore we have to leave these questions for a future occasion.

# Curiosities and fun challenges on knots and wobbly entities

Knots appear rarely in nature. For example, tree branches or roots do not seem to grow many knots during the lifetime of a plant. How do plants avoid this? In other words, why are there no knotted bananas or knotted flower stems in nature?

Recent research has also explored how octopusses avoid knots in their arms. It was found that the arms secrete a chemical substance that prevents arms or parts of the arms from sticking together.

\* \*

Not only knot, also links can be classified. The simplest links, i.e., the links for which the simplest configuration has the smallest number of crossings, are shown in Figure 175.

\* \*

Challenge 166 r

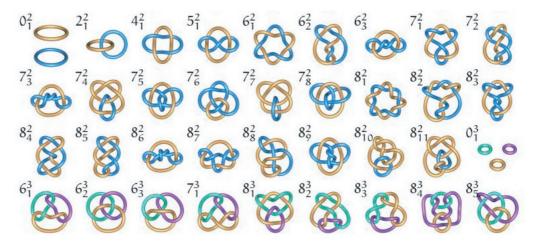


FIGURE 175 The diagrams for the simplest links with two and three components (© Robert Scharein).



FIGURE 176 A hagfish tied into a knot (© Christine Ortlepp).

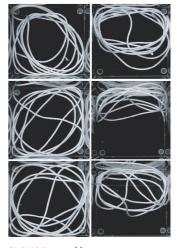


FIGURE 177 How apparent order for long rope coils (left) changes over time when shaking the container (right) (© 2007 PNAS).

The physics of human swimming is fascinating. To learn the details on how to move in order to swim as rapidly as possible, explore the wonderful website coachsci.sdsu.edu/ swim by Brent Rushall. He tells how to move the arms, the trunk and the legs and he shows how champions perform these movements. Rushall also tells about the bizarre theories that are aired in the field of swimming, such as the mistaken idea that lift plays a role in human swimming.

Ref. 262

A famous type of eel, the *knot fish Myxine glutinosa*, also called hagfish or slime eel, is able to make a knot in his body and move this knot from head to tail. Figure 176 shows

\* \*

an example. The hagfish uses this motion to cover its body with a slime that prevents predators from grabbing it; it also uses this motion to escape the grip of predators, to get rid of the slime after the danger is over, and to push against a prey it is biting in order to extract a piece of meat. All studied knot fish form only left handed trefoil knots, by the way; this is another example of chirality in nature.

\* \*

Proteins, the molecules that make up many cell structures, are chains of aminoacids. It seems that very few proteins are knotted, and that most of these form trefoil knots. However, a figure-eight knotted protein has been discovered in 2000 by William Taylor.

\* \*

One of the most incredible discoveries of recent years is related to knots in DNA molecules. The *DNA molecules* inside cell nuclei can be hundreds of millions of base pairs long; they regularly need to be packed and unpacked. When this is done, often the same happens as when a long piece of rope or a long cable is taken out of a closet.

It is well known that you can roll up a rope and put it into a closet in such a way that it looks orderly stored, but when it is pulled out at one end, a large number of knots is suddenly found. In 2007, this effects was finally explored in detail. Strings of a few metres in length were put into square boxes and shaken, in order to speed up the effect. The result, shown partly in Figure 177, was astonishing: almost every imaginable knot – up to a certain complexity that depends on the length and flexibility of the string – was formed in this way.

To make a long story short, the tangling also happens to nature when it unpacks DNA in cell nuclei. Life requires that DNA molecules move inside the cell nucleus without hindrance. So what does nature do? Nature takes a simpler approach: when there are unwanted crossings, it cuts the DNA, moves it over and puts the ends together again. In cell nuclei, there are special enzymes, the so-called topoisomerases, which perform this process. The details of this fascinating process are still object of modern research.

The great mathematician Carl-Friedrich Gauß – often written as 'Gauss' in English – was the first person to ask what happens when an electrical current I flows along a wire A that is *linked* with a wire B. He discovered a beautiful result by calculating the effect of the magnetic field of one wire onto the other:

$$\frac{1}{4\pi I} \int_{A} \mathrm{d}\boldsymbol{x}_{A} \cdot \boldsymbol{B}_{B} = \frac{1}{4\pi} \int_{A} \mathrm{d}\boldsymbol{x}_{A} \cdot \int_{B} \mathrm{d}\boldsymbol{x}_{B} \times \frac{(\boldsymbol{x}_{A} - \boldsymbol{x}_{B})}{|\boldsymbol{x}_{A} - \boldsymbol{x}_{B}|^{3}} = n , \qquad (131)$$

where the integrals are performed along the wires. Gauss found that the number *n* does not depend on the precise shape of the wires, but only on the way they are linked. Deforming the wires does not change the resulting number *n*. Mathematicians call such a number a *topological invariant*. In short, Gauss discovered a physical method to calculate a mathematical invariant for links; the research race to do the same for other invariants, and in particular for knots and braids, is still going on today.

In the 1980s, Edward Witten was able to generalize this approach to include the nuc-

Ref. 261

Ref. 263

Ref. 264



FIGURE 178 A large raindrop falling downwards.



FIGURE 179 Is this possible?

lear interactions, and to define more elaborate knot invariants, a discovery that brought him the Fields medal.

\* \*

If we move along a knot and count the crossings where we stay above and subtract the number of crossings where we pass below, we get a number called the *writhe* of the knot. It is not an invariant, but usually a tool in building them. Indeed, the writhe is not necessarily invariant under one of the three Reidemeister moves. Can you see which one, using Figure 172? However, the writhe is invariant under flypes.

\* \*

\* \*

Modern knot research is still a topic with many open questions. A recent discovery is the *quasi-quantization of three-dimensional writhe* in tight knots. Many discoveries are still expected in the domain of geometric knot theory.

Challenge 168 e	There are two ways to tie your shoes. Can you find them?

Challenge 169 s What is the shape of raindrops? Try to picture it. However, use your reason, not your prejudice! By the way, it turns out that there is a maximum size for raindrops, with a value of about 4 mm. The shape of such a large raindrop is shown in Figure 178. Can you imagine where the limit comes from?

Challenge 170 s What is the entity shown in Figure 179 – a knot, a braid or a link?

\* \*

\* \*

Challenge 171 d Can you find a way to classify tie knots?

Challenge 172 s Are you able to find a way to classify the way shoe laces can be threaded?



FIGURE 180 A flying snake, Chrysopelea paradisii, performing the feat that gave it its name (QuickTime film © Jake Socha).

Ref. 267	A striking example of how wobbly entities can behave is given in Figure 180. There is indeed a family of snakes that like to jump off a tree and sail through the air to a neighbouring tree. Both the jump and the sailing technique have been studied in recent years. The website www.flyingsnake.org by Jake Socha provides additional films. His fascinating publications tell more about these intriguing reptiles.
	* *
Vol. I, page 327	When a plane moves at supersonic speed through humid air, sometimes a conical cloud forms and moves with the plane. How does this cloud differ from the ones studied above?
Challenge 173 e	
	* *
Challenge 174 ny	One of the toughest challenges about clouds: is it possible to make rain on demand? So far, there are almost no positive results. Inventing a method, possibly based on hygroscopic salt injection or with the help of lasers, will be a great help to mankind.
	* *
	Do knots have a relation to elementary particles? The question is about 150 years old. It was first investigated by William Thomson-Kelvin and Peter Tait in the late nineteenth century. So far, no proof of a relation has been found. Knots might be of importance at Planck scales, the smallest dimensions possible in nature. We will explore how knots and the structure of elementary particles might be related in the last volume of this adventure.
	Summary on wobbly objects
Vol. I, page 316	We can sum up the possible motions of extended systems in a few key themes. In earl- ier chapters we studied waves, solitons and interpenetration. These observations are de- scribed by wave equations. In this chapter we explored the way to move through shape

change, explored eversion, studied vortices, fluids, polymers, knots and their rearrangement, and explored the motion of dislocations in solids. We found that shape change is described by gauge theory, eversion is described by space-duality, vortices follow the Schrödinger equation, fluids and polymers resemble general relativity and black holes, knot shapes are hard to calculate and dislocations behave relativistically.

The motion of wobbly objects is a neglected topic in textbooks on motion. Research is progressing at full speed; it is expected that many beautiful analogies with traditional physics will be discovered in the near future. For example, in this chapter we have not explored any possible analogy for the motion of light. Similarly, including quantum theory into the description of wobbly bodies' motion remains a fascinating issue for anybody aiming to publish in a new field.

In summary, we found that wobbly entities can reproduce most fields of modern physics. Are there wobbly entities that reproduce *all* of modern physics? We will explore the question in the last volume.

~~\_\_\_\_\_A

Challenge 175 r

# CHAPTER 12 QUANTUM PHYSICS IN A NUTSHELL - AGAIN

ompared to classical physics, quantum theory is definitely more omplex. The basic idea however, is simple: in nature there is a smallest hange, or a smallest action, with the value  $\hbar = 1.1 \cdot 10^{-34}$  Js. The smallest action value leads to all the strange observations made in the microscopic domain, such as wave behaviour of matter, indeterminacy relations, decoherence, randomness in measurements, indistinguishability, quantization of angular momentum, tunnelling, pair creation, decay, particle reactions and virtual particle exchange.

## QUANTUM FIELD THEORY IN A FEW SENTENCES

C Deorum offensae diis curae. Voltaire, *Traité sur la tolérance*.

All of quantum theory can be resumed in a few sentences.

 $\triangleright$  In nature, actions smaller than  $\hbar = 1.1 \cdot 10^{-34}$  Js are not observed.

The existence of a smallest action in nature directly leads to the main lesson we learned about motion in the quantum part of our adventure:

- ▷ If something moves, it is made of quantons, or quantum particles.
- ▷ There are *elementary* quantum particles.

These statements apply to everything, thus to all objects and to all images, i.e., to matter and to radiation. Moving stuff is made of *quantons*. Stones, water waves, light, sound waves, earthquakes, tooth paste and everything else we can interact with is made of moving quantum particles. Experiments show:

▷ All intrinsic object properties observed in nature – such as electric charge, weak charge, colour charge, spin, parity, lepton number, etc., with the only exception of mass – appear as *integer* numbers of a smallest unit; in composed systems they either add or multiply.

▷ An *elementary quantum particle* or *elementary quanton* is a countable entity, smaller than its own Compton wavelength, described by energymomentum, mass, spin, C, P and T parity, electric charge, colour, weak isospin, isospin, strangeness, charm, topness, beauty, lepton number and baryon number.

All moving entities are made of elementary quantum particles. To see how deep this result is, you can apply it to all those moving entities for which it is usually forgotten, such as ghosts, spirits, angels, nymphs, daemons, devils, gods, goddesses and souls. You can check yourself what happens when their particle nature is taken into account.

Quantum particles are never at rest, cannot be localized, move probabilistically, behave as particles or as waves, interfere, can be polarized, can tunnel, are indistinguishable, have antiparticles, interact locally, define length and time scales and they limit measurement precision.

Quantum particles come in two types:

▷ Matter is composed of *fermions*: quarks and leptons. There are 6 quarks that make up nuclei, and 6 leptons – 3 charged leptons, including the electron, and 3 uncharged neutrinos. Elementary fermions have spin 1/2 and obey the Pauli exclusion principle.

▷ Radiation is due to the three gauge interactions and is composed of *bosons*: photons, the weak vector bosons and the 8 gluons. These elementary bosons all have spin 1.

In our adventure, we wanted to know what matter and interactions are. Now we know: they are due to elementary quantum particles. The exploration of motion inside matter, including particle reactions and virtual particle exchange, showed us that matter is made of a *finite number* of elementary quantum particles. Experiments show:

▷ In flat space, elementary particles interact in one of three ways: there is the *electromagnetic interaction*, the *strong nuclear interaction* and the *weak nuclear interaction*.

▷ The three interactions are *exchanges of virtual bosons*.

 $\triangleright$  The three interactions are described by the gauge symmetries U(1), SU(3) and a broken, i.e., approximate SU(2) symmetry.

The three gauge symmetries fix the Lagrangian of every physical system in flat spacetime. The most simple description of the Lagrangians is with the help of Feynman diagrams and the gauge groups.

▷ In all interactions, energy, momentum, angular momentum, electric charge, colour charge, CPT parity, lepton number and baryon number are conserved.

The list of conserved quantities implies:

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▷ Quantum *field* theory is the part of quantum physics that includes the description of *particle transformations*.

The possibility of particle transformations – including particle reactions, particle emission and particle absorption – results from the existence of a minimum action and of a maximum speed in nature. Emission of light, radioactivity, the burning of the Sun and the history of the composite matter we are made of are due to particle transformations.

Due to the possibility of particle transformations, quantum field theory introduces a limit for the localization of particles. In fact, any object of mass m can be localized only within intervals of the Compton wavelength

$$\lambda_{\rm C} = \frac{h}{mc} = \frac{2\pi\hbar}{mc} \,, \tag{132}$$

where c is the speed of light. At the latest at this distance we have to abandon the classical description and use quantum field theory. If we approach the Compton wavelength, particle transformations become so important that classical physics and even simple quantum theory are not sufficient.

*Quantum electrodynamics* is the quantum field description of electromagnetism. It includes and explains all particle transformations that involve photons. The Lagrangian of QED is determined by the electromagnetic gauge group U(1), the requirements of space-time (Poincaré) symmetry, permutation symmetry and renormalizability. The latter requirement follows from the continuity of space-time. Through the effects of virtual particles, QED describes electromagnetic decay, lamps, lasers, pair creation, Unruh radiation for accelerating observers, vacuum energy and the Casimir effect, i.e., the attraction of neutral conducting bodies. Particle transformations due to quantum electrodynamics also introduce corrections to classical electrodynamics; among others, particle transformations produce small departures from the superposition principle for electromagnetic fields, including the possibility of photon-photon scattering.

The theory of *weak nuclear interaction* describes parity violation, quark mixings, neutrino mixings, massive vector bosons and the Higgs field for the breaking of the weak SU(2) gauge symmetry. The weak interaction explains a large part of radioactivity, including the heat production inside the Earth, and describes processes that make the Sun shine.

*Quantum chromodynamics*, the field theory of the strong nuclear interaction, describes all particle transformations that involve gluons. At fundamental scales, the strong interaction is mediated by eight elementary gluons. At larger, femtometre scales, the strong interaction effectively acts through the exchange of spin 0 pions, is strongly attractive, and leads to the formation of atomic nuclei. The strong interaction determines nuclear fusion and fission. Quantum chromodynamics, or QCD, explains the masses of mesons and baryons through their description as bound quark states.

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By including particle transformations, quantum field theory provides a common basis of concepts and descriptions to materials science, nuclear physics, chemistry, biology, medicine and to most of astronomy. For example, the same concepts allow us to answer questions such as why water is liquid at room temperature, why copper is red, why the rainbow is coloured, why the Sun and the stars continue to shine, why there are about

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110 elements, where a tree takes the material to make its wood and why we are able to move our right hand at our own will. Quantum theory explains the origin of material properties and the origin of the properties of life.

Quantum field theory describes all material properties, be they mechanical, optical, electric or magnetic. It describes all waves that occur in materials, such as sound and phonons, magnetic waves and magnons, light, plasmons, and all localized excitations. Quantum field theory also describes collective effects in matter, such as superconduct-ivity, semiconductor effects and superfluidity. Finally, quantum field theory describes all interactions between matter and radiation, from colour to antimatter creation.

Quantum field theory also clarifies that the particle description of nature, including the conservation of particle number – defined as the difference between particles and antiparticles – follows from the possibility to describe interactions *perturbatively*. A perturbative description of nature is possible only at low energies. At extremely high energies, higher than those observed in experiments, the situation is expected to change and non-perturbative effects should come into play. These situations will be explored in the next volume.

## ACHIEVEMENTS IN PRECISION

Classical physics is unable to predict *any* property of matter. Quantum field theory predicts all properties of matter, and to the full number of digits – sometimes thirteen – that can be measured today. The precision is usually *not* limited by the inaccuracy of theory, it is limited by the measurement accuracy. In other words, the agreement between quantum field theory and experiment is only limited by the amount of money one is willing to spend. Table 25 shows some predictions of classical physics and of quantum field theory. The predictions are deduced from the properties of nature collected in the millennium list, which is given in the next section.

TABLE 25 Selected c	comparisons between	classical physics,	quantum theory a	and experiment.

Observable	CLAS- SICAL PREDIC- TION	Prediction of Quantum Theory <sup>a</sup>	M E A S U R E - M E N T	Cost esti- mate <sup>b</sup>
Simple motion of bodies				
Indeterminacy	0	$\Delta x \Delta p \ge \hbar/2$	$(1 \pm 10^{-2})  \hbar/2$	10 k€
Matter wavelength	none	$\lambda p = 2\pi\hbar$	$(1\pm10^{-2})\hbar$	10 k€
Tunnelling rate in $\alpha$ decay	0	$1/\tau$ is finite	$(1 \pm 10^{-2})  \tau$	5 k€
Compton wavelength	none	$\lambda_{\rm c} = h/m_{\rm e}c$	$(1\pm10^{-3})\lambda$	20 k€
Pair creation rate	0	$\sigma E$	agrees	100 k€
Radiative decay time in hydrogen	none	$\tau \sim 1/n^3$	$(1 \pm 10^{-2})$	5 k€
Smallest angular momentum	0	ħ/2	$(1 \pm 10^{-6})\hbar/2$	10 k€
Casimir effect/pressure	0	$p=(\pi^2\hbar c)/(240r^4)$	$(1 \pm 10^{-3})$	30 k€

experiment.				
OBSERVABLE	CLAS- SICAL PREDIC- TION	PREDICTION OF QUANTUM THEORY <sup>a</sup>	M e a s u r e - m e n t	Cost esti- mate <sup>b</sup>
Colours of objects				
Spectrum of hot objects	diverges	$\lambda_{\rm max} = hc/(4.956  kT)$	$(1 \pm 10^{-4}) \Delta \lambda$	10 k€
Lamb shift	none	$\Delta \lambda = 1057.86(1) \mathrm{MHz}$	$(1\pm 10^{-6})\Delta\lambda$	50 k€
Rydberg constant	none	$R_{\infty} = m_{\rm e} c \alpha^2 / 2h$	$(1 \pm 10^{-9}) R_{\infty}$	50 k€
Stefan-Boltzmann constant	none	$\sigma = \pi^2 k^4 / 60 \hbar^3 c^2$	$(1\pm3\cdot10^{-8})\sigma$	20 k€
Wien's displacement constant	none	$b = \lambda_{\max} T$	$(1 \pm 10^{-5}) b$	20 k€
Refractive index of water	none	1.34	a few %	1 k€
Photon-photon scattering	0	from QED: finite	agrees	50 M€
Laser radiation exists	no	yes	agrees	10€
Particle and interaction p	roperties			
Electron gyromagnetic ratio	1 or 2	2.002 319 304 3(1)	2.002 319 304 3737(82)	30 M€
Z boson mass	none	$m_Z^2 = m_W^2 (1 + \sin \theta_W^2)$	$(1 \pm 10^{-3}) m_Z$	100 M€
Proton mass	none	$(1 \pm 5\%) m_{\rm p}$	$m_{\rm p} = 1.67  {\rm yg}$	1 M€
Proton lifetime	≈ 1 µs	$\infty$	$>10^{35}$ a	100 M€
Chemical reaction rate	0	from QED	correct within errors	2 k€
Composite matter proper	ties			
Atom lifetime	≈ 1 µs	00	> 10 <sup>20</sup> a	1€
Molecular size	none	from QED	within $10^{-3}$	20 k€
Von Klitzing constant	$\infty$	$h/e^2 = \mu_0 c/2\alpha$	$(1 \pm 10^{-7}) h/e^2$	1 M€
AC Josephson constant	0	2e/h	$(1 \pm 10^{-6})  2e/h$	5 M€
Heat capacity of metals at 0 K	25 J/K	0	$< 10^{-3} \text{ J/K}$	10 k€
Heat capacity of diatomic gas at 0 K	25 J/K	0	$< 10^{-3} \text{ J/K}$	10 k€
Water density	none	1000.00 kg/m <sup>3</sup> at 4°C	agrees	10 k€
Minimum electr. conductivity	0	$G = 2e^2/\hbar$	$G(1 \pm 10^{-3})$	3 k€
Ferromagnetism	none	exists	exists	2€
Superfluidity	none	exists	exists	200 k€
Bose-Einsein condensation	none	exists	exists	2 M€

 TABLE 25 (Continued) Selected comparisons between classical physics, quantum theory and experiment.

OBSERVABLE	C l a s - s i c a l	PREDICTION OF QUANTUM	M e a s u r e - m e n t	Соят еяті-
	PREDIC-	T H E O R Y $a$		$M A T E^{b}$
	ΤΙΟΝ			
Superconductivity (metal)	none	exists	exists	100 k€
Superconductivity (high T)	none	none yet	exists	100 k€

**TABLE 25** (Continued) Selected comparisons between classical physics, quantum theory and experiment.

*a*. All these predictions are calculated from the fundamental quantities given in the millennium list.

*b*. Sometimes the cost for the calculation of the prediction is higher than that of the experimental observation. (Can you spot the examples?) The sum of the two is given.

We notice that the values predicted by quantum theory do not differ from the measured ones. In contrast, classical physics does not allow us to calculate any of the observed values. This shows the progress that quantum physics has brought in the description of nature.

In short, in the microscopic domain quantum theory is in *perfect* correspondence with nature; despite prospects of fame and riches, despite the largest number of researchers ever, no contradiction with observation has been found yet. But despite this impressive agreement, there still are *unexplained* observations; they form the so-called *millennium list*.

## What is unexplained by quantum theory and general relativity?

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The material gathered in this quantum part of our mountain ascent, together with the earlier summary of general relativity, allows us to describe *all* observed phenomena connected to motion. For the first time, there are no known differences between theory and practice.

Despite the precision of the description of nature, some things are missing. Whenever we ask 'why?' about an observation and continue doing so after each answer, we arrive at one of the *unexplained* properties of nature listed in Table 26. The table lists all issues about fundamental motion that were unexplained in the year 2000, so that we can call it the *millennium list* of open problems.

**TABLE 26** The millennium list: *everything* the standard model and general relativity *cannot* explain; thus, also the list of the *only* experimental data available to test the final, unified description of motion.

Observable Property unexplained since the year 2000

# Local quantities unexplained by the standard model: particle properties

- $\alpha = 1/137.036(1)$  the low energy value of the electromagnetic coupling or fine structure constant
- $\alpha_{w}$  or  $\theta_{w}$  the low energy value of the weak coupling constant or the value of the weak mixing angle

TABLE 26	(Continued)	Everything	the standard	model and	general	relativity	cannot	explain.
----------	-------------	------------	--------------	-----------	---------	------------	--------	----------

OBSERVABLE PROPERTY UNEXPLAINED SINCE THE YEAR 2000

$\alpha_{s}$	the value of the strong coupling constant at one specific energy value
m <sub>q</sub>	the values of the 6 quark masses
$m_{\rm l}$	the values of 6 lepton masses
$m_{ m W}$	the value of the mass of the W vector boson
$m_{ m H}$	the value of the mass of the scalar Higgs boson
$\theta_{12}, \theta_{13}, \theta_{23}$	the value of the three quark mixing angles
δ	the value of the CP violating phase for quarks
$\theta^{\nu}_{12}, \theta^{\nu}_{13}, \theta^{\nu}_{23}$	the value of the three neutrino mixing angles
$\delta^{\nu}, \alpha_1, \alpha_2$	the value of the three CP violating phases for neutrinos
$3 \cdot 4$	the number of fermion generations and of particles in each generation
J, P, C, etc.	the origin of all quantum numbers of each fermion and each boson
Concepts unexpla	ined by the standard model
c, ħ, k	the origin of the invariant Planck units of quantum field theory
3 + 1	the number of dimensions of physical space and time
SO(3,1)	the origin of Poincaré symmetry, i.e., of spin, position, energy, momentum
Ψ	the origin and nature of wave functions
S(n)	the origin of particle identity, i.e., of permutation symmetry
Gauge symmetry	
U(1)	the origin of the electromagnetic gauge group, i.e., of the quantization of elec- tric charge, of the vanishing of magnetic charge, and of minimal coupling
SU(2)	the origin of weak interaction gauge group, its breaking and P violation
SU(3)	the origin of strong interaction gauge group and its CP conservation
Renorm. group	the origin of renormalization properties
$\delta W = 0$	the origin of the least action principle in quantum theory
$W = \int L_{\rm SM}  \mathrm{d}t$	the origin of the Lagrangian of the standard model of particle physics
Global quantities	unexplained by general relativity and cosmology
0	the observed flatness, i.e., vanishing curvature, of the universe
$1.2(1) \cdot 10^{26} \mathrm{m}$	the distance of the horizon, i.e., the 'size' of the universe (if it makes sense)
$ \rho_{\rm de} = \Lambda c^4 / (8\pi G) $ $ \approx 0.5 \mathrm{nJ/m}^3 $	the value and nature of the observed vacuum energy density, dark energy or cosmological constant
$(5 \pm 4) \cdot 10^{79}$	the number of baryons in the universe (if it makes sense), i.e., the average visible matter density in the universe
$ ho_{ m dm}$	the density and nature of dark matter
$f_0(1,, c. 10^{90})$	the initial conditions for $c. 10^{90}$ particle fields in the universe (if or as long as they make sense), including the homogeneity and isotropy of matter distribution, and the density fluctuations at the origin of galaxies
Concente un evole	in addition and a source loans

# Concepts unexplained by general relativity and cosmology

*c*, *G* the origin of the invariant Planck units of general relativity

OBSERVABLI	E FROPERTY UNEXPLAINED SINCE THE YEAR 2000
$R \times S^3$	the observed topology of the universe
$G^{\mu u}$	the origin and nature of curvature, the metric and horizons
$\delta W = 0$	the origin of the least action principle in general relativity
$W = \int L_{\rm GR} dt$	the origin of the Lagrangian of general relativity

 TABLE 26 (Continued) Everything the standard model and general relativity cannot explain.

 OBSERVABLE
 PROPERTY UNEXPLAINED SUNCE THE XEAR 2000

The millennium list has several notable aspects. First of all, neither quantum mechanics nor general relativity explain any property unexplained in the other field. The two theories do not help each other; the unexplained parts of both fields simply add up. Secondly, both in quantum theory and in general relativity, motion still remains the change of position with time. In short, so far, we did not achieve our goal: we still do not understand motion! We are able to describe motion with full precision, but we still do not know what it is. Our basic questions remain: What are time and space? What is mass? What is charge and what are the other properties of objects? What are fields? Why are all the electrons the same?

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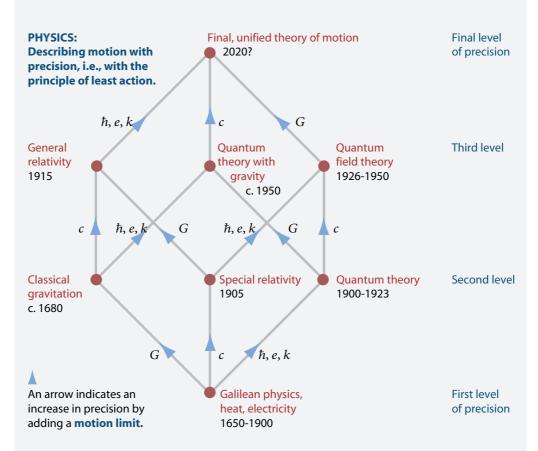
We also note that the millennium list of open questions, Table 26, contains extremely *different* concepts. This means that at this point of our walk there is *a lot* we do not understand. Finding the answers will require effort.

On the other hand, the millennium list of unexplained properties of nature is also *short*. The description of nature that our adventure has produced so far is concise and precise. No discrepancies from experiments are known. In other words, we have a good description of motion *in practice*. Going further is unnecessary if we only want to improve measurement precision. Simplifying the above list is mainly important from the *conceptual* point of view. For this reason, the study of physics at university often stops at this point. However, as the millennium list shows, even though we have *no* known discrepancies with experiments, we are *not* at the top of Motion Mountain.

### The physics cube

Page 8 Another review of the progress and of the open issues of physics, already given in the introduction, is shown in Figure 181: the *physics cube*. From the lowest corner of the cube, representing Galilean physics and related topics from everyday life, three edges – labelled *c*, *G* and *ħ*, *e*, *k* – lead to classical gravity, special relativity and quantum theory. Each constant implies a limit to motion; in the corresponding theory, this *one* limit is taken into account, thus improving the precision of the description. From these second level theories, similar edges lead upwards to general relativity, quantum field theory and quantum theory with gravity. Each of these third level theories takes into account *two* of the limits and thus improves precision even more.\* The present volume completes the third level of precision. We stress that each theory in the second and third level is *exact*,

<sup>\*</sup> Of course, Figure 181 gives a simplified view of the history of physics. A more precise diagram might use different arrows for  $\hbar$  (with k) and e, making the figure a four-dimensional cube. However, not all of its corners would have dedicated theories (can you confirm this?). Also the weak and the strong coupling constants might have to be added. The diagram would be far less appealing. And most of all, the conclusions mentioned in the text would not change.



**FIGURE 181** A simplified history of the description of motion in physics, by giving the limits to motion included in each description. The arrows show which constant of nature needs to be added and taken into account to reach the next level of precision. (The electric charge *e* is taken to represent all three discrete gauge charges.)

though only *in its domain*. And even though the limits of each domain are obvious, no differences between experiment and theory are known.

From the third level theories, the edges lead to the last missing corner: the (unified) theory of motion that takes into account *all limits* of nature. Only this theory is a complete and unified description of nature. Since we already know all limits to motion, in order to arrive at the last level, we do not need new experiments. We do not need new knowledge. We only have to advance, in the right direction, with careful thinking. And we can start from three different points. This is the topic of the last volume of our adventure.

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Ref. 270

# The intense emotions due to quantum field theory and general RELATIVITY

It is sometimes deemed chic to pretend that the adventure is over at the stage we have just reached,\* the third level of Figure 181. The reasoning given is as follows. If we change the values of the unexplained constants in the millennium list of Table 26 only ever so slightly, nature would look completely different from what it does. Indeed, these consequences have been studied in great detail; an overview of the connections is given in the following table.

TABLE 27 A selection of the conse	quences of changing the	properties of nature.

OBSERVABLE	C h a n g e	Result
Local quantities, f	rom quantum th	ieory
$\alpha_{ m em}$	smaller:	Only short lived, smaller and hotter stars; no Sun.
	larger:	Darker Sun, animals die of electromagnetic radiation too much proton decay, no planets, no stellar explosions, no star formation, no galaxy formation.
	+60 %:	Quarks decay into leptons.
	+200 %:	Proton-proton repulsion makes nuclei impossible.
$lpha_{ m w}$	-50 %:	Carbon nucleus unstable.
	very weak:	No hydrogen, no p-p cycle in stars, no C-N-O cycle.
	+2 %:	No protons from quarks.
	$G_F m_e^2 \neq \sqrt{G m_e^2}$ :	Either no or only helium in the universe.
	much larger:	No stellar explosions, faster stellar burning.
$\alpha_{\rm s}$	-9 %:	No deuteron, stars far less bright.
	-1 %:	No C resonance, no life.
	+3.4 %:	Diproton stable, faster star burning.
	much larger:	Carbon unstable, heavy nuclei unstable, widespread leukaemia.
n-p mass difference	larger:	Neutron decays in proton inside nuclei; no elements.
	smaller:	Free neutron not unstable, all protons into neutrons during big bang; no elements.
	smaller than	Protons would capture electrons, no hydrogen atoms,
	$m_e$ :	star life much shorter.
m <sub>l</sub> changes:		

\* Actually this attitude is not new. Only the arguments have changed. Maybe the greatest physicist ever, Ref. 269 James Clerk Maxwell, already fought against this attitude over a hundred years ago: 'The opinion seems to

have got abroad that, in a few years, all great physical constants will have been approximately estimated, and that the only occupation which will be left to men of science will be to carry these measurements to another place of decimals. [...] The history of science shows that even during that phase of her progress in which she devotes herself to improving the accuracy of the numerical measurement of quantities with which she has long been familiar, she is preparing the materials for the subjugation of new regions, which would have remained unknown if she had been contented with the rough methods of her early pioneers.'

OBSERVABLE	C h a n g e	Result
e-p mass ratio	much different:	No molecules.
	much smaller:	No solids.
3 generations	6-8:	Only helium in nature.
	>8:	No asymptotic freedom and confinement.
Global quantities,	from general rel	ativity
horizon size	much smaller:	No people.
baryon number	very different:	No smoothness.
	much higher:	No solar system.
Initial condition ch	nanges:	
Moon mass	smaller:	Small Earth magnetic field; too much cosmic radiation; widespread child skin cancer.
Moon mass	larger:	Large Earth magnetic field; too little cosmic radiation; no evolution into humans.
Sun's mass	smaller:	Too cold for the evolution of life.
Sun's mass	larger:	Sun too short lived for the evolution of life.
Jupiter mass	smaller:	Too many comet impacts on Earth; extinction of animal life.
Jupiter mass	larger:	Too little comet impacts on Earth; no Moon; no dinosaur extinction.
Oort cloud object number	smaller:	No comets; no irregular asteroids; no Moon; still dinosaurs.
galaxy centre distance	smaller:	Irregular planet motion; supernova dangers.
initial cosmic speed	+0.1 %:	1000 times faster universe expansion.
	-0.0001 %:	Universe recollapses after 10000 years.
vacuum energy density	change by 10 <sup>-55</sup> :	No flatness.
3 + 1 dimensions	different:	No atoms, no planetary systems.
Local structures, f	rom quantum th	eory
permutation symmetry	none:	No matter.
Lorentz symmetry	none:	No communication possible.
U(1)	different:	No Huygens principle, no way to see anything.
SU(2)	different:	No radioactivity, no Sun, no life.
SU(3)	different:	No stable quarks and nuclei.

 TABLE 27 (Continued) A selection of the consequences of changing the properties of nature.

Global structures, from general relativity

#### 12 QUANTUM PHYSICS IN A NUTSHELL - AGAIN

OBSERVABLE	C h a n g e	Result
topology	other:	Unknown; possibly correlated $\gamma$ ray bursts or star images at the antipodes.

 TABLE 27 (Continued) A selection of the consequences of changing the properties of nature.

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Note. Some researchers speculate that the whole of Table 27 can be condensed into a single sentence: if any parameter in nature is changed, the universe would either have too many or too few black holes. However, the proof of this condensed summary is not complete yet. But it is a beautiful hypothesis.

The effects of changing nature that are listed in Table 27 lead us to a profound experience: even the tiniest changes in the properties of nature are incompatible with our existence. What does this experience mean? Answering this question too rapidly is dangerous. Many have fallen into one of several traps:

- The first trap is to deduce, incorrectly, that the unexplained numbers and other properties from the millennium list do not need to or even cannot be explained, i.e., deduced from more general principles.
- The second trap is to deduce, incorrectly, that the universe has been *created* or *designed*.
- The third trap is to deduce, incorrectly, that the universe is *designed for people*.
- The fourth trap is to deduce, incorrectly, that the universe is *one of many*.

All these traps are irrational and incorrect beliefs. All these beliefs have in common that they have no factual basis, that they discourage further search and that they sell many books.

The first trap is due to a combination of pessimism and envy; it is a type of wishful thinking. But wishful thinking has no place in the study of motion. The second trap works because many physicists incorrectly speak of *fine tuning* in nature. Many researchers succumb to the belief in 'creation' and are unable to steer clear from the logical errors contained in it. We discussed them earlier on. The third trap, is often, again incorrectly, called the *anthropic principle*. The name is a mistake, because we saw that the anthropic principle is indistinguishable both from the simian principle and from the simple request that statements be based on observations. Around 2000, the third trap has even become fashionable among frustrated particle theorists. The fourth trap, the belief in *multiple universes*, is a minority view, but sells many books. Most people that hold this view are found in institutions. And that is indeed where they belong.

Stopping our adventure, our mountain ascent, with an incorrect belief at the present stage is not different from doing so directly at the beginning. Such a choice has been taken in various societies that lacked the passion for rational investigation, and still is taken in circles that discourage the use of reason among their members. Looking for beliefs instead of looking for answers means to give up our ascent while pretending to have reached the top. Every such case is a tragedy, sometimes a small one, sometimes a larger one.

In fact, Table 27 purveys only one message: all evidence implies that we are only a *tiny part* of the universe, but that we are *linked* with all other aspects of it. Due to our small

size and due to all the connections with our environment, any imagined tiny change would make us disappear, like a water droplet is swept away by large wave. Our walk has repeatedly reminded us of this smallness and dependence, and overwhelmingly does so again at this point.

In our adventure, accepting the powerful message of Table 27 is one of the most aweinspiring, touching and motivating moments. It shows clearly how vast the universe is. It also shows how much we are dependent on many different and distant aspects of nature. Having faced this powerful experience, everybody has to make up his or her own mind on whether to proceed with the adventure or not. Of course, there is no obligation to do so.

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Challenge 180 s

## WHAT AWAITS US?

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Assuming that you have decided to continue the adventure, it is natural to ask what awaits you. The shortness of the millennium list of unexplained aspects of nature, given in Table 26, means that *no additional experimental data* are available as check of the final description of nature. Everything we need to arrive at the final description of motion will be deduced from the experimental data given in the millennium list, and from nothing else. In other words, future experiments will *not* help us – except if they change something in the millennium list. Accelerator experiments might do this with the particle list or astronomical experiments with the topology issue. Fantasy provides no limits; fortunately, nature does.

The lack of new experimental data means that to continue the walk is a *conceptual* adventure only. Nevertheless, storms rage near the top of Motion Mountain. We have to walk keeping our eyes open, without any other guidance except our reason. This is not an adventure of action, but an adventure of the mind. And it is a fascinating one, as we shall soon find out. To provide an impression of what awaits us, we rephrase the remaining issues in five simple challenges.

1 – What determines *colours*? In other words, what relations of nature fix the famous fine structure constant? Like the hero of Douglas Adams' books, physicists know the answer to the greatest of questions: it is 137.036. But they do not know the question.

2 – What fixes the contents of a *teapot*? It is given by its size to the third power. But why are there only three dimensions? Why is the tea content limited in this way?

3 – Was Democritus *right*? Our adventure has confirmed his statement up to this point: nature is indeed well described by the concepts of *particle* and of *vacuum*. At large scales, relativity has added a horizon, and at small scales, quantum field theory added vacuum energy and pair creation. Nevertheless, both theories *assume* the existence of particles and the existence of space-time, and neither *predicts* them. Even worse, both theories completely fail to predict the existence of *any* of the properties either of space-time – such as its dimensionality – or of particles – such as their masses and other quantum numbers. A lot is missing.

4 – Was Democritus *wrong*? It is often said that the standard model has only about twenty unknown parameters; this common mistake negates about  $10^{93}$  initial conditions! To get an idea of the problem, we simply estimate the number N of possible states of all

#### **12 QUANTUM PHYSICS IN A NUTSHELL - AGAIN**

particles in the universe by

$$N = n v d p f \tag{133}$$

where *n* is the number of particles, *v* is the number of variables (position, momentum, spin), *d* is the number of different values each of them can take (limited by the maximum of 61 decimal digits), *p* is the number of visible space-time points (about  $10^{183}$ ) and *f* is a factor expressing how many of all these initial conditions are actually independent of each other. We thus get the following number of possible states of all particles in the universe:

1

$$N = 10^{92} \cdot 8 \cdot 10^{61} \cdot 10^{183} \cdot f = 10^{336} \cdot f \tag{134}$$

from which the  $10^{93}$  initial conditions have to be explained. But no explanation is known. Worse, there is also the additional problem that we know nothing whatsoever about f. Its value could be 0, if all data were interdependent, or 1, if none were. Even worse, above we noted that initial conditions cannot be defined for the universe at all; thus f should be undefined and not be a number at all! Whatever the case, we need to understand how all the visible particles acquire their present  $10^{93}$  states.

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Challenge 181 e

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5 – Were our efforts up to this point *in vain*? Quite at the beginning of our walk we noted that in classical physics, space and time are defined using matter, whereas matter is defined using space-time. Hundred years of general relativity and of quantum theory, including dozens of geniuses, have not solved this oldest paradox of all. The issue is still open at this point of our walk, as you might want to check by yourself.

The answers to these five challenges define the goal of our adventure: the top of Motion Mountain. Answering the five challenges means to know *everything* about motion. It means to find, finally, the answer to the question that drove us here:

▷ What is motion?

In short, our quest for the unravelling of the essence of motion gets really interesting from this point onwards!

C That is why Leucippus and Democritus, who say that the atoms move always in the void and the unlimited, must say what movement is, and in what their natural motion consists. Aristotle, *Treaty of the Heaven* 





# APPENDIX A UNITS, MEASUREMENTS AND CONSTANTS

A gasurements are comparisons with standards. Standards are based on *units*. any different systems of units have been used throughout the world. ost of these standards confer power to the organization in charge of them. Such power can be misused; this is the case today, for example in the computer industry, and was so in the distant past. The solution is the same in both cases: organize an independent and global standard. For measurement units, this happened in the eighteenth century: in order to avoid misuse by authoritarian institutions, to eliminate problems with differing, changing and irreproducible standards, and – this is not a joke – to simplify tax collection and to make it more just, a group of scientists, politicians and economists agreed on a set of units. It is called the *Système International d'Unités*, abbreviated *SI*, and is defined by an international treaty, the 'Convention du Mètre'. The units are maintained by an international organization, the 'Conférence Générale des Poids et Mesures', and its daughter organizations, the 'Commission Internationale des Poids et Mesures' and the 'Bureau International des Poids et Mesures' (BIPM). All originated in the times just before the French revolution.

Ref. 273

## SI UNITS

All SI units are built from seven *base units*. Their simplest definitions, translated from French into English, are the following ones, together with the dates of their formulation and a few comments:

• 'The *second* is the duration of 9 192 631 770 periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the caesium 133 atom.' (1967) The 2019 definition is equivalent, but much less clear.\*

• 'The *metre* is the length of the path travelled by light in vacuum during a time interval of 1/299 792 458 of a second.' (1983) The 2019 definition is equivalent, but much less clear.\*

• 'The *kilogram*, symbol kg, is the SI unit of mass. It is defined by taking the fixed numerical value of the Planck constant h to be  $6.626\,070\,15\cdot10^{-34}$  when expressed in the unit J · s, which is equal to kg · m<sup>2</sup> · s<sup>-1</sup>.' (2019)\*

• 'The *ampere*, symbol A, is the SI unit of electric current. It is defined by taking the fixed numerical value of the elementary charge e to be  $1.602 \ 176 \ 634 \cdot 10^{-19}$  when expressed in the unit C, which is equal to A  $\cdot$  s.' (2019)\* This definition is equivalent to: One ampere is  $6.241 \ 509 \ 074... \cdot 10^{18}$  elementary charges per second.

• 'The *kelvin*, symbol K, is the SI unit of thermodynamic temperature. It is defined by

taking the fixed numerical value of the Boltzmann constant *k* to be  $1.380649 \cdot 10^{-23}$  when expressed in the unit J · K<sup>-1</sup>.' (2019)\*

• 'The mole, symbol mol, is the SI unit of amount of substance. One mole contains exactly  $6.02214076 \cdot 10^{23}$  elementary entities.' (2019)\*

• 'The *candela* is the luminous intensity, in a given direction, of a source that emits monochromatic radiation of frequency  $540 \cdot 10^{12}$  hertz and has a radiant intensity in that direction of (1/683) watt per steradian.' (1979) The 2019 definition is equivalent, but much less clear.\*

We note that both time and length units are defined as certain properties of a standard example of motion, namely light. In other words, also the Conférence Générale des Poids et Mesures makes the point that the observation of motion is a *prerequisite* for the definition and construction of time and space. *Motion is the fundament of every observation and of all measurement*. By the way, the use of light in the definitions had been proposed already in 1827 by Jacques Babinet.\*\*

From these basic units, all other units are defined by multiplication and division. Thus, all SI units have the following properties:

• SI units form a system with *state-of-the-art precision*: all units are defined with a precision that is higher than the precision of commonly used measurements. Moreover, the precision of the definitions is regularly being improved. The present relative uncertainty of the definition of the second is around  $10^{-14}$ , for the metre about  $10^{-10}$ , for the kilogram about  $10^{-9}$ , for the ampere  $10^{-7}$ , for the mole less than  $10^{-6}$ , for the kelvin  $10^{-6}$  and for the candela  $10^{-3}$ .

• SI units form an *absolute* system: all units are defined in such a way that they can be reproduced in every suitably equipped laboratory, independently, and with high precision. This avoids as much as possible any error or misuse by the standard-setting organization. In fact, the SI units are as now as near as possible to Planck's natural units, which are presented below. In practice, the SI is now an international standard defining the numerical values of the seven constants  $\Delta v_{Cs}$ , *c*, *h*, *e*, *k*, *N*<sub>A</sub> and *K*<sub>cd</sub>. After over 200 years of discussions, the CGPM has little left to do.

• SI units form a *practical* system: the base units are quantities of everyday magnitude. Frequently used units have standard names and abbreviations. The complete list includes the seven base units just given, the supplementary units, the derived units and the admitted units.

The *supplementary* SI units are two: the unit for (plane) angle, defined as the ratio of arc length to radius, is the *radian* (rad). For solid angle, defined as the ratio of the subtended area to the square of the radius, the unit is the *steradian* (sr).

The *derived* units with special names, in their official English spelling, i.e., without capital letters and accents, are:

Ref. 274

<sup>\*</sup> The symbols of the seven units are s, m, kg, A, K, mol and cd. The full offical definitions are found at www.bipm.org. For more details about the levels of the caesium atom, consult a book on atomic physics. The Celsius scale of temperature  $\theta$  is defined as:  $\theta/^{\circ}C = T/K - 273.15$ ; note the small difference with the number appearing in the definition of the kelvin. In the definition of the candela, the frequency of the light corresponds to 555.5 nm, i.e., green colour, around the wavelength to which the eye is most sensitive. \*\* Jacques Babinet (1794–1874), French physicist who published important work in optics.

N a m e	ABBREVIATION	N а м е	Abbreviation
hertz	Hz = 1/s	newton	$N = kg m/s^2$
pascal	$Pa = N/m^2 = kg/m s^2$	joule	$J = Nm = kg m^2/s^2$
watt	$W = kg m^2/s^3$	coulomb	C = As
volt	$V = kg m^2 / As^3$	farad	$F = As/V = A^2 s^4 / kg m^2$
ohm	$\Omega = V/A = kg m^2/A^2 s^3$	siemens	$S = 1/\Omega$
weber	$Wb = Vs = kg m^2 / As^2$	tesla	$T = Wb/m^2 = kg/As^2 = kg/Cs$
henry	$H = Vs/A = kg m^2/A^2 s^2$	degree Celsius	°C (see definition of kelvin)
lumen	lm = cd sr	lux	$lx = lm/m^2 = cd sr/m^2$
becquerel	Bq = 1/s	gray	$Gy = J/kg = m^2/s^2$
sievert	$Sv = J/kg = m^2/s^2$	katal	kat = mol/s
-			

The *admitted* non-SI units are *minute*, *hour*, *day* (for time), *degree*  $1^{\circ} = \pi/180$  rad, *minute*  $1' = \pi/10\,800$  rad, *second*  $1'' = \pi/648\,000$  rad (for angles), *litre*, and *tonne*. All other units are to be avoided.

All SI units are made more practical by the introduction of standard names and abbreviations for the powers of ten, the so-called *prefixes*:\*

Power	N a m e	Pown	er Na	M E	Pow	er Nami	E	Power	r Name	
$10^1$ dec	a da	$10^{-1}$	deci	d	$10^{18}$	Exa	Е	$10^{-18}$	atto	a
$10^2$ hec	to h	$10^{-2}$	centi	с	$10^{21}$	Zetta	Z	$10^{-21}$	zepto	Z
10 <sup>3</sup> kile	o k	$10^{-3}$	milli	m	$10^{24}$	Yotta	Y	$10^{-24}$	yocto	y
10 <sup>6</sup> Me	ga M	$10^{-6}$	micro	μ	unoffi	cial:		Ref. 275		
10 <sup>9</sup> Gig	ga G	$10^{-9}$	nano	n	$10^{27}$	Xenta	Х	$10^{-27}$	xenno	x
10 <sup>12</sup> Ter	а Т	$10^{-12}$	pico	р	$10^{30}$	Wekta	W	$10^{-30}$	weko	w
10 <sup>15</sup> Pet	a P	$10^{-15}$	femto	f	$10^{33}$	Vendekta	V	$10^{-33}$	vendeko	v
					$10^{36}$	Udekta	U	$10^{-36}$	udeko	u

• SI units form a *complete* system: they cover in a systematic way the full set of observables of physics. Moreover, they fix the units of measurement for all other sciences as well.

• SI units form a *universal* system: they can be used in trade, in industry, in commerce,

Translate: I was caught in such a traffic jam that I needed a microcentury for a picoparsec and that my car's fuel consumption was two tenths of a square millimetre.

Challenge 182 e

<sup>\*</sup> Some of these names are invented (yocto to sound similar to Latin *octo* 'eight', zepto to sound similar to Latin *septem*, yotta and zetta to resemble them, exa and peta to sound like the Greek words  $\dot{\xi}\xi\dot{\alpha}\kappa\iota\varsigma$  and  $\pi\epsilon\nu\tau\dot{\alpha}\kappa\iota\varsigma$  for 'six times' and 'five times', the unofficial ones to sound similar to the Greek words for nine, ten, eleven and twelve); some are from Danish/Norwegian (atto from *atten* 'eighteen', femto from *femten* 'fifteen'); some are from Latin (from *mille* 'thousand', from *centum* 'hundred', from *decem* 'ten', from *nanus* 'dwarf'); some are from Italian (from *piccolo* 'small'); some are Greek (micro is from  $\mu\kappa\rho\delta\varsigma$  'small', deca/deka from  $\delta\epsilon\kappa\alpha$  'ten', hecto from  $\epsilon\kappa\alpha\tau\delta\nu$  'hundred', kilo from  $\chii\lambda\iota\sigma$  'thousand', mega from  $\mu\epsilon\gamma\alpha\varsigma$  'large', giga from  $\gammai\gamma\alpha\varsigma$  'giant', tera from  $\tau\epsilon\rho\alpha\varsigma$  'monster').

at home, in education and in research. They could even be used by extraterrestrial civilizations, if they existed.

• SI units form a *self-consistent* system: the product or quotient of two SI units is also an SI unit. This means that in principle, the same abbreviation, e.g. 'SI', could be used for every unit.

The SI units are not the only possible set that could fulfil all these requirements, but they are the only existing system that does so.\*

### THE MEANING OF MEASUREMENT

Challenge 183 e

Every measurement is a comparison with a standard. Therefore, any measurement requires *matter* to realize the standard (even for a speed standard), and *radiation* to achieve the comparison. The concept of measurement thus assumes that matter and radiation exist and can be clearly separated from each other.

Every measurement is a comparison. Measuring thus implies that space and time exist, and that they differ from each other.

Every measurement produces a measurement result. Therefore, every measurement implies the *storage* of the result. The process of measurement thus implies that the situation before and after the measurement can be distinguished. In other terms, every measurement is an *irreversible* process.

Every measurement is a process. Thus every measurement takes a certain amount of time and a certain amount of space.

All these properties of measurements are simple but important. Beware of anybody who denies them.

# Planck's natural units

Since the exact form of many equations depends on the system of units used, theoretical physicists often use unit systems optimized for producing simple equations. The chosen units and the values of the constants of nature are related. In microscopic physics, the system of *Planck's natural units* is frequently used. They are defined by setting c = 1,  $\hbar = 1$ , G = 1, k = 1,  $\varepsilon_0 = 1/4\pi$  and  $\mu_0 = 4\pi$ . Planck units are thus defined from combinations of fundamental constants; those corresponding to the fundamental SI units are given in Table 29.\*\* The table is also useful for converting equations written in natural units back to SI units: just substitute every quantity X by  $X/X_{\rm Pl}$ .

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<sup>\*</sup> Apart from international units, there are also *provincial* units. Most provincial units still in use are of Roman origin. The mile comes from *milia passum*, which used to be one thousand (double) strides of about 1480 mm each; today a nautical mile, once defined as minute of arc on the Earth's surface, is defined as exactly 1852 m. The inch comes from *uncia/onzia* (a twelfth – now of a foot). The pound (from *pondere* 'to weigh') is used as a translation of *libra* – balance – which is the origin of its abbreviation lb. Even the habit of counting in dozens instead of tens is Roman in origin. These and all other similarly funny units – like the system in which all units start with 'f', and which uses furlong/fortnight as its unit of velocity – are now officially defined as multiples of SI units.

<sup>\*\*</sup> The natural units  $x_{\rm Pl}$  given here are those commonly used today, i.e., those defined using the constant  $\hbar$ , and not, as Planck originally did, by using the constant  $h = 2\pi\hbar$ . The electromagnetic units can also be defined with other factors than  $4\pi\epsilon_0$  in the expressions: for example, using  $4\pi\epsilon_0\alpha$ , with the *fine-structure constant*  $\alpha$ , gives  $q_{\rm Pl} = e$ . For the explanation of the numbers between brackets, see below.

N a m e	D e f	INI	ΓΙΟΝ	VA	LUE
Basic units					
the Planck length	$l_{ m Pl}$	=	$\sqrt{\hbar G/c^3}$	=	$1.6160(12) \cdot 10^{-35} \mathrm{m}$
the Planck time	$t_{ m Pl}$	=	$\sqrt{\hbar G/c^5}$	=	$5.3906(40)\cdot10^{-44}\mathrm{s}$
the Planck mass	$m_{ m Pl}$	=	$\sqrt{\hbar c/G}$	=	21.767(16) µg
the Planck current	$I_{ m Pl}$	=	$\sqrt{4\pi\varepsilon_0 c^6/G}$	=	$3.4793(22)\cdot10^{25}\mathrm{A}$
the Planck temperature	$T_{\rm Pl}$	=	$\sqrt{\hbar c^5/Gk^2}$	=	$1.4171(91) \cdot 10^{32} \mathrm{K}$
Trivial units					
the Planck velocity	$v_{ m Pl}$	=	С	=	0.3 Gm/s
the Planck angular momentum	$L_{\rm Pl}$	=	ħ	=	$1.1\cdot10^{-34}$ Js
the Planck action	$S_{aPl}$	=	$\hbar$	=	$1.1\cdot10^{-34}$ Js
the Planck entropy	$S_{ePl}$	=	k	=	13.8 yJ/K
Composed units					
the Planck mass density	$ ho_{ m Pl}$	=	$c^5/G^2\hbar$	=	$5.2 \cdot 10^{96}  \text{kg/m}^3$
the Planck energy	$E_{\mathrm{Pl}}$	=	$\sqrt{\hbar c^5/G}$	=	$2.0 \mathrm{GJ} = 1.2 \cdot 10^{28} \mathrm{eV}$
the Planck momentum	$p_{ m Pl}$	=	$\sqrt{\hbar c^3/G}$	=	6.5 Ns
the Planck power	$P_{\mathrm{Pl}}$	=	$c^5/G$	=	$3.6\cdot10^{52}\mathrm{W}$
the Planck force	$F_{\mathrm{Pl}}$	=	$c^4/G$	=	$1.2 \cdot 10^{44}$ N
the Planck pressure	$p_{ m Pl}$	=	$c^7/G\hbar$	=	$4.6 \cdot 10^{113}$ Pa
the Planck acceleration	$a_{\rm Pl}$	=	$\sqrt{c^7/\hbar G}$	=	$5.6 \cdot 10^{51} \text{ m/s}^2$
the Planck frequency	$f_{\mathrm{Pl}}$	=	$\sqrt{c^5/\hbar G}$	=	$1.9\cdot 10^{43}\mathrm{Hz}$
the Planck electric charge	$q_{ m Pl}$	=	$\sqrt{4\pi\varepsilon_0c\hbar}$	=	1.9 aC = 11.7 e
the Planck voltage	$U_{ m Pl}$	=	$\sqrt{c^4/4\pi\varepsilon_0 G}$	=	$1.0\cdot 10^{27}\mathrm{V}$
the Planck resistance	$R_{ m Pl}$	=	$1/4\pi\varepsilon_0 c$	=	30.0 Ω
the Planck capacitance	$C_{ m Pl}$	=	$4\pi\varepsilon_0\sqrt{\hbar G/c^3}$	=	$1.8\cdot10^{-45}\mathrm{F}$
the Planck inductance	$L_{\rm Pl}$	=	$(1/4\pi\varepsilon_0)\sqrt{\hbar G/c^7}$	=	$1.6\cdot10^{-42}\mathrm{H}$
the Planck electric field	$E_{\mathrm{Pl}}$	=	$\sqrt{c^7/4\pi\varepsilon_0\hbar G^2}$	=	$6.5 \cdot 10^{61}  \mathrm{V/m}$
the Planck magnetic flux density	$B_{\mathrm{Pl}}$	=	$\sqrt{c^5/4\pi\varepsilon_0\hbar G^2}$	=	$2.2\cdot10^{53}\mathrm{T}$

 TABLE 29 Planck's (uncorrected) natural units.

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The natural units are important for another reason: whenever a quantity is sloppily called 'infinitely small (or large)', the correct expression is 'as small (or as large) as the corresponding corrected Planck unit'. As explained throughout the text, and especially in the final part, this substitution is possible because almost all Planck units provide, within a correction factor of order 1, the extremal value for the corresponding observable – some an upper and some a lower limit. Unfortunately, these correction factors are not yet widely known. The exact extremal value for each observable in nature is obtained

when *G* is substituted by 4*G* and  $4\pi\epsilon_0$  by  $4\pi\epsilon_0\alpha$  in all Planck quantities. These extremal values, or *corrected Planck units*, are the *true natural units*. To exceed the extremal values (Challenge 185 s) is possible only for some extensive quantities. (Can you find out which ones?)

## OTHER UNIT SYSTEMS

A central aim of research in high-energy physics is the calculation of the strengths of all interactions; therefore it is not practical to set the gravitational constant *G* to unity, as in the Planck system of units. For this reason, high-energy physicists often only set  $c = \hbar = k = 1$  and  $\mu_0 = 1/\varepsilon_0 = 4\pi$ ,\* leaving only the gravitational constant *G* in the equations.

In this system, only one fundamental unit exists, but its choice is free. Often a standard length is chosen as the fundamental unit, length being the archetype of a measured quantity. The most important physical observables are then related by

$$\begin{split} 1/[l^2] &= [E]^2 = [F] = [B] = [E_{\text{electric}}], \\ 1/[l] &= [E] = [m] = [p] = [a] = [f] = [I] = [U] = [T], \\ 1 &= [v] = [q] = [e] = [R] = [S_{\text{action}}] = [S_{\text{entropy}}] = \hbar = c = k = [\alpha], \ (135) \\ [l] &= 1/[E] = [t] = [C] = [L] \quad \text{and} \\ [l]^2 &= 1/[E]^2 = [G] = [P] \end{split}$$

where we write [x] for the unit of quantity x. Using the same unit for time, capacitance and inductance is not to everybody's taste, however, and therefore electricians do not use this system.\*\*

Often, in order to get an impression of the energies needed to observe an effect under study, a standard energy is chosen as fundamental unit. In particle physics the most common energy unit is the *electronvolt* (eV), defined as the kinetic energy acquired by an electron when accelerated by an electrical potential difference of 1 volt ('protonvolt' would be a better name). Therefore one has  $1 \text{ eV} = 1.6 \cdot 10^{-19}$  J, or roughly

$$1 \text{ eV} \approx \frac{1}{6} \text{ aJ}$$
 (136)

which is easily remembered. The simplification  $c = \hbar = 1$  yields  $G = 6.9 \cdot 10^{-57} \text{ eV}^{-2}$  and allows one to use the unit eV also for mass, momentum, temperature, frequency, time and length, with the respective correspondences  $1 \text{ eV} \equiv 1.8 \cdot 10^{-36} \text{ kg} \equiv 5.4 \cdot 10^{-28} \text{ Ns} \equiv 242 \text{ THz} \equiv 11.6 \text{ kK}$  and  $1 \text{ eV}^{-1} \equiv 4.1 \text{ fs} \equiv 1.2 \text{ µm}.$ 

Challenge 186 e

Ref. 276

<sup>\*</sup> Other definitions for the proportionality constants in electrodynamics lead to the Gaussian unit system often used in theoretical calculations, the Heaviside–Lorentz unit system, the electrostatic unit system, and the electromagnetic unit system, among others.

<sup>\*\*</sup> In the list, *l* is length, *E* energy, *F* force,  $E_{\text{electric}}$  the electric and *B* the magnetic field, *m* mass, *p* momentum, *a* acceleration, *f* frequency, *I* electric current, *U* voltage, *T* temperature, *v* speed, *q* charge, *R* resistance, *P* power, *G* the gravitational constant.

The web page www.chemie.fu-berlin.de/chemistry/general/units\_en.html provides a tool to convert various units into each other.

Researchers in general relativity often use another system, in which the Schwarzschild radius  $r_s = 2Gm/c^2$  is used to measure masses, by setting c = G = 1. In this case, mass and length have the same dimension, and  $\hbar$  has the dimension of an area.

To get some feeling for the unit eV, the following relations are useful. Room temperature, usually taken as 20°C or 293 K, corresponds to a kinetic energy per particle of 0.025 eV or 4.0 zJ. The highest particle energy measured so far belongs to a cosmic ray with an energy of  $3 \cdot 10^{20}$  eV or 48 J. Down here on the Earth, an accelerator able to produce an energy of about 105 GeV or 17 nJ for electrons and antielectrons has been built, and one able to produce an energy of 14 TeV or 2.2 µJ for protons will be finished soon. Both are owned by CERN in Geneva and have a circumference of 27 km.

Ref. 278

Ref. 277

The lowest temperature measured up to now is 280 pK, in a system of rhodium nuclei held inside a special cooling system. The interior of that cryostat may even be the coolest point in the whole universe. The kinetic energy per particle corresponding to that temperature is also the smallest ever measured: it corresponds to 24 feV or  $3.8 \text{ vJ} = 3.8 \cdot 10^{-33} \text{ J}$ . For isolated particles, the record seems to be for neutrons: kinetic energies as low as  $10^{-7}$  eV have been achieved, corresponding to de Broglie wavelengths of 60 nm.

#### CURIOSITIES AND FUN CHALLENGES ABOUT UNITS

The Planck length is roughly the de Broglie wavelength  $\lambda_{\rm B} = h/mv$  of a man walking comfortably (m = 80 kg, v = 0.5 m/s); this motion is therefore aptly called the 'Planck stroll.'

The Planck mass is equal to the mass of about  $10^{19}$  protons. This is roughly the mass of a human embryo at about ten days of age.

\* \*

Ref. 280

The most precisely measured quantities in nature are the frequencies of certain millisecond pulsars, the frequency of certain narrow atomic transitions, and the Rydberg constant of *atomic* hydrogen, which can all be measured as precisely as the second is defined. The caesium transition that defines the second has a finite line width that limits the achievable precision: the limit is about 14 digits.

The most precise clock ever built, using microwaves, had a stability of 10<sup>-16</sup> during a running time of 500 s. For longer time periods, the record in 1997 was about 10<sup>-15</sup>; but
Ref. 282 values around 10<sup>-17</sup> seem within technological reach. The precision of clocks is limited for short measuring times by noise, and for long measuring times by drifts, i.e., by systematic effects. The region of highest stability depends on the clock type; it usually lies between 1 ms for optical clocks and 5000 s for masers. Pulsars are the only type of clock for which this region is not known yet; it certainly lies at more than 20 years, the time elapsed at the time of writing since their discovery.

\* \*

Ref. 283

The shortest times measured are the lifetimes of certain 'elementary' particles. In particular, the lifetime of certain D mesons have been measured at less than  $10^{-23}$  s. Such times are measured using a bubble chamber, where the track is photographed. Can you Challenge 187 s

Ref. 284

estimate how long the track is? (This is a trick question – if your length cannot be observed with an optical microscope, you have made a mistake in your calculation.)

The longest times encountered in nature are the lifetimes of certain radioisotopes, over  $10^{15}$  years, and the lower limit of certain proton decays, over  $10^{32}$  years. These times are thus much larger than the age of the universe, estimated to be fourteen thousand million years.

\* \*

There is a unit for the spicy heat of chili peppers, officially called the *pungency*. The pungency is due to an organic compound called *capsaicin*. If you multiply by 16 the capsaicin concentration in parts per million, you get the *Scoville heat unit* for chili peppers. A few extreme chili varieties exceed the value of 2 million Scoville units.

#### PRECISION AND ACCURACY OF MEASUREMENTS

Measurements are the basis of physics. Every measurement has an *error*. Errors are due to lack of precision or to lack of accuracy. *Precision* means how well a result is reproduced when the measurement is repeated; *accuracy* is the degree to which a measurement corresponds to the actual value.

Lack of precision is due to accidental or *random errors*; they are best measured by the *standard deviation*, usually abbreviated  $\sigma$ ; it is defined through

$$\sigma^{2} = \frac{1}{n-1} \sum_{i=1}^{n} (x_{i} - \bar{x})^{2} , \qquad (137)$$

where  $\bar{x}$  is the average of the measurements  $x_i$ . (Can you imagine why n - 1 is used in Challenge 188 s the formula instead of n?)

For most experiments, the distribution of measurement values tends towards a normal distribution, also called *Gaussian distribution*, whenever the number of measurements is increased. The distribution, shown in Figure 182, is described by the expression

$$N(x) \approx e^{-\frac{(x-\bar{x})^2}{2\sigma^2}}$$
 (138)

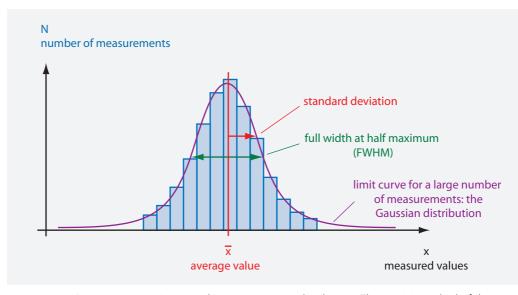
The square  $\sigma^2$  of the standard deviation is also called the *variance*. For a Gaussian distribution of measurement values, 2.35 $\sigma$  is the full width at half maximum.

Lack of accuracy is due to *systematic errors*; usually these can only be estimated. This estimate is often added to the random errors to produce a *total experimental error*, sometimes also called *total uncertainty*. The *relative* error or uncertainty is the ratio between the error and the measured value.

For example, a professional measurement will give a result such as 0.312(6) m. The number between the parentheses is the standard deviation  $\sigma$ , in units of the last digits. As above, a Gaussian distribution for the measurement results is assumed. Therefore, a value of 0.312(6) m implies that the actual value is expected to lie

Challenge 189 e

Ref. 285



**FIGURE 182** A precision experiment and its measurement distribution. The precision is high if the width of the distribution is narrow; the accuracy is high if the centre of the distribution agrees with the actual value.

- within  $1\sigma$  with 68.3 % probability, thus in this example within  $0.312 \pm 0.006$  m;
- within  $2\sigma$  with 95.4 % probability, thus in this example within 0.312 ± 0.012 m;
- within  $3\sigma$  with 99.73 % probability, thus in this example within  $0.312 \pm 0.018$  m;
- within  $4\sigma$  with 99.9937 % probability, thus in this example within  $0.312 \pm 0.024$  m;
- within  $5\sigma$  with 99.999 943 % probability, thus in this example within  $0.312 \pm 0.030$  m;
- within  $6\sigma$  with 99.999 999 80 % probability, thus within  $0.312 \pm 0.036$  m;
- within  $7\sigma$  with 99.999 999 999 74 % probability, thus within 0.312 ± 0.041 m.

However, these numbers are much too precise and should be taken with a grain of salt.

Note that standard deviations have one digit; you must be a world expert to use two, and a fool to use more. If no standard deviation is given, a (1) is assumed. As a result, among professionals, 1 km and 1000 m are *not* the same length!

What happens to the errors when two measured values *A* and *B* are added or subtracted? If the all measurements are independent – or <u>uncorrelated</u> – the standard deviation of the sum *and* that of difference is given by  $\sigma = \sqrt{\sigma_A^2 + \sigma_B^2}$ . For both the product or ratio of two measured and uncorrelated values *C* and *D*, the result is  $\rho = \sqrt{\rho_C^2 + \rho_D^2}$ , where the  $\rho$  terms are the *relative* standard deviations.

### LIMITS TO PRECISION

What are the limits to accuracy and precision? There is no way, even in principle, to measure a length x to a *precision* higher than about 61 digits, because in nature, the ratio between the largest and the smallest measurable length is  $\Delta x/x > l_{\rm Pl}/d_{\rm horizon} = 10^{-61}$ . (Is this ratio valid also for force or for volume?) In the final volume of our text, studies of clocks and metre bars strengthen this theoretical limit.

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But it is not difficult to deduce more stringent practical limits. No imaginable machine

can measure quantities with a higher precision than measuring the diameter of the Earth within the smallest length ever measured, about  $10^{-19}$  m; that is about 26 digits of precision. Using a more realistic limit of a 1000 m sized machine implies a limit of 22 digits. If, as predicted above, time measurements really achieve 17 digits of precision, then they are nearing the practical limit, because apart from size, there is an additional practical restriction: cost. Indeed, an additional digit in measurement precision often means an additional digit in equipment cost.

# Physical constants

In physics, general observations are deduced from more fundamental ones. As a consequence, many measurements can be deduced from more fundamental ones. The most fundamental measurements are those of the physical constants.

The following tables give the world's best values of the most important physical constants and particle properties – in SI units and in a few other common units – as published in the standard references. The values are the world averages of the best measurements made up to the present. As usual, experimental errors, including both random and estimated systematic errors, are expressed by giving the standard deviation in the last digits. In fact, behind each of the numbers in the following tables there is a long story which is worth telling, but for which there is not enough room here.

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Ref. 287

Ref. 286

In principle, *all* quantitative properties of matter can be calculated with quantum theory – more precisely, equations of the standard model of particle – and a set of *basic* physical constants that are given in the next table. For example, the colour, density and elastic properties of any material can be predicted, in principle, in this way.

Quantity	Symbol	VALUE IN SI UNITS	Uncert. <sup>a</sup>
Constants that define the S	l measurement uni	ts	
Vacuum speed of light <sup>c</sup>	С	299 792 458 m/s	0
Original Planck constant <sup>c</sup>	h	$6.62607015\cdot10^{-34}\mathrm{Js}$	0
Reduced Planck constant,	ħ	$1.054571817\ldots\cdot10^{-34}\mathrm{Js}$	0
quantum of action			
Positron charge <sup>c</sup>	е	0.160 217 6634 aC	0
Boltzmann constant <sup>c</sup>	k	$1.380649\cdot 10^{-23}\mathrm{J/K}$	0
Avogadro's number	$N_{ m A}$	$6.02214076\cdot 10^{23}1/mol$	0
Constant that should define	the SI measureme	ent units	
Gravitational constant	G	$6.67430(15)\cdot10^{-11}\text{Nm}^2/\text{kg}^2$	$2.2\cdot 10^{-5}$
Other fundamental constar	nts		
Number of space-time dime	ensions	3 + 1	0 <sup>b</sup>
Fine-structure constant <sup>d</sup> or	$\alpha = \frac{e^2}{4\pi\varepsilon_0\hbar c}$	1/137.035 999 084(21)	$1.5\cdot 10^{-10}$
e.m. coupling constant	$=g_{\rm em}(m_{\rm e}^2c^2)$	= 0.007 297 352 5693(11)	$1.5\cdot 10^{-10}$
Fermi coupling constant <sup>d</sup> o	or $G_{\rm F}/(\hbar c)^3$	$1.1663787(6)\cdot 10^{-5}\mathrm{GeV}^{-2}$	$5.1 \cdot 10^{-7}$
weak coupling constant	$\alpha_{\rm w}(M_{\rm Z}) = g_{\rm w}^2/4\pi$	1/30.1(3)	$1 \cdot 10^{-2}$

 TABLE 30 Basic physical constants.

QUANTITY	Symbol	VALUE IN SI UNITS	Uncert. <sup>a</sup>
Strong coupling constant <sup>d</sup>	$\alpha_{\rm s}(M_{\rm Z}) = g_{\rm s}^2/4\pi$	0.1179(10)	$8.5 \cdot 10^{-3}$
Weak mixing angle		0.231 22(4)	$1.7\cdot 10^{-4}$
	$\sin^2 \theta_{\rm W}$ (on shell)	0.222 90(30)	$1.3\cdot 10^{-3}$
	$= 1 - (m_{\rm W}/m_{\rm Z})^2$		
		(0.97383(24)  0.2272(10))	0.00396(9)
CKM quark mixing matrix	V	$\left(\begin{array}{ccc} 0.97383(24) & 0.2272(10) \\ 0.2271(10) & 0.97296(24) \end{array}\right)$	0.04221(80)
		0.00814(64)  0.04161(78)	0.999100(34)
Jarlskog invariant	J	$3.08(18) \cdot 10^{-5}$	
		( 0.82(2) 0.55(4) 0.150(	7)
PMNS neutrino mixing m.	P	0.37(13) 0.57(11) 0.71(7	')
		$\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $	r) /
Electron mass	m <sub>e</sub>	$9.1093837015(28)\cdot 10^{-31}\mathrm{kg}$	$3.0\cdot 10^{-10}$
		$5.48579909065(16)\cdot 10^{-4}\mathrm{u}$	$2.9\cdot 10^{-11}$
		0.510 998 950 00(15) MeV	$3.0\cdot10^{-10}$
Muon mass	$m_{\mu}$	$1.883531627(42)\cdot 10^{-28}\mathrm{kg}$	$2.2\cdot 10^{-8}$
	,	105.658 3755(23) MeV	$2.2\cdot 10^{-8}$
Tau mass	$m_{ au}$	$1.776 \ 82(12) \ \mathrm{GeV}/c^2 \ 6.8 \cdot 10^{-5}$	5
El. neutrino mass	m <sub>v</sub>	$< 2 \mathrm{eV}/c^2$	
Muon neutrino mass	$m_{\nu_{\mu}}$	$< 2 \mathrm{eV}/c^2$	
Tau neutrino mass	$m_{v_{\tau}}$	$< 2 \mathrm{eV}/c^2$	
Up quark mass	u v <sub>r</sub>	$21.6(+0.49/-0.26) \text{ MeV}/c^2$	
Down quark mass	d	$4.67(+0.48/-0.17) \text{ MeV}/c^2$	
Strange quark mass	S	$93(+11/-5) \mathrm{MeV}/c^2$	
Charm quark mass	С	$1.27(2) \mathrm{GeV}/c^2$	
Bottom quark mass	Ь	$4.18(3) \mathrm{GeV}/c^2$	
Top quark mass	t	$172.9(0.4) \mathrm{GeV}/c^2$	
Photon mass	γ	$< 2 \cdot 10^{-54}  \text{kg}$	
W boson mass	$W^{\pm}$	$80.379(12) \mathrm{GeV}/c^2$	
Z boson mass	$Z^0$	91.1876(21) $\text{GeV}/c^2$	
Higgs mass	Н	$125.10(14) \mathrm{GeV}/c^2$	
Gluon mass	g <sub>18</sub>	$c.0 \mathrm{MeV}/c^2$	

TABLE 30 (Continued) Basic physical constants.

a. Uncertainty: standard deviation of measurement errors.

b. Measured from to  $10^{-19}$  m to  $10^{26}$  m.

c. Defining constant.

*d*. All coupling constants depend on the 4-momentum transfer, as explained in the section on renormalization. *Fine-structure constant* is the traditional name for the electromagnetic coupling constant  $g_{\rm em}$  in the case of a 4-momentum transfer of  $Q^2 = m_e^2 c^2$ , which is the smallest one possible. At higher momentum transfers it has larger values, e.g.,  $g_{\rm em}(Q^2 = M_W^2 c^2) \approx 1/128$ . In contrast, the strong coupling constant has lover values at higher momentum transfers; e.g.,  $\alpha_s(34 \,\text{GeV}) = 0.14(2)$ . Why do all these basic constants have the values they have? For any basic constant with a dimension, such as the quantum of action  $\hbar$ , the numerical value has only historical meaning. It is  $1.054 \cdot 10^{-34}$  Js because of the SI definition of the joule and the second. The question why the value of a dimensional constant is not larger or smaller therefore always requires one to understand the origin of some dimensionless number giving the ratio between the constant and the corresponding natural unit that is defined with c, G, k,  $N_A$  and  $\hbar$ . Details and values for the natural units are given in the dedicated section.

In other words, understanding the sizes of atoms, people, trees and stars, the duration of molecular and atomic processes, or the mass of nuclei and mountains, implies understanding the ratios between these values and the corresponding natural units. The key to understanding nature is thus the understanding of all measurement ratios, and thus of all dimensionless constants. This quest, including the understanding of the fine-structure constant  $\alpha$  itself, is completed only in the final volume of our adventure.

The basic constants yield the following useful high-precision observations.

 TABLE 31 Derived physical constants.

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QUANTITY	Symbol	VALUE IN SI UNITS	Uncert.
Vacuum permeability	$\mu_0$	$1.25663706212(19)\mu H/m$	$1.5\cdot 10^{-10}$
Vacuum permittivity	$\varepsilon_0 = 1/\mu_0 c^2$	8.854 187 8128(13) pF/m	$1.5\cdot 10^{-10}$
Vacuum impedance	$Z_0 = \sqrt{\mu_0/\varepsilon_0}$	$376.730313668(57)\Omega$	$1.5\cdot 10^{-10}$
Loschmidt's number at 273.15 K and 101 325 Pa	$N_{ m L}$	$2.686780111\cdot 10^{25}1/m^3$	0
Faraday's constant	$F = N_A e$	96 485.332 12 C/mol	0
Universal gas constant	$R = N_A k$	8.314 462 618 J/(mol K)	0
Molar volume of an ideal gas at 273.15 K and 101 325 Pa	V = RT/p	22.413 969 54l/mol	0
Rydberg constant <sup><i>a</i></sup>	$R_{\infty} = m_{\rm e} c \alpha^2 / 2h$	$10973731.568160(21)\mathrm{m}^{-1}$	$1.9\cdot 10^{-12}$
Conductance quantum	$G_0 = 2e^2/h$	77.480 917 29 μS	0
Magnetic flux quantum	$\varphi_0 = h/2e$	2.067 833 848 fWb	0
Josephson frequency ratio	2e/h	483.597 8484 THz/V	0
Von Klitzing constant	$h/e^2 = \mu_0 c/2\alpha$	$25812.80745\Omega$	0
Bohr magneton	$\mu_{\rm B} = e\hbar/2m_{\rm e}$	9.2740100783(28)yJ/T	$3.0\cdot10^{-10}$
Classical electron radius	$r_{\rm e} = e^2/4\pi\varepsilon_0 m_{\rm e}c^2$	2.817 940 3262(13) fm	$4.5\cdot10^{-10}$
Compton wavelength	$\lambda_{\rm C} = h/m_{\rm e}c$	2.426 310 238 67(73) pm	$3.0\cdot10^{-10}$
of the electron	$\lambda_{\rm c} = \hbar/m_{\rm e}c = r_{\rm e}/c$	x 0.386 159 267 96(12) pm	$3.0\cdot10^{-10}$
Bohr radius <sup><i>a</i></sup>	$a_{\infty} = r_{\rm e}/\alpha^2$	52.917 721 0903(80) pm	$1.5\cdot 10^{-10}$
Quantum of circulation	$h/2m_{\rm e}$	3.636 947 5516(11) cm <sup>2</sup> /s	$3.0\cdot10^{-10}$
Specific positron charge	$e/m_{e}$	175.882 001 076(55) GC/kg	$3.0\cdot 10^{-10}$
Cyclotron frequency of the electron	$f_{\rm c}/B = e/2\pi m_{\rm e}$	27.992 489 872(9) GHz/T	$3.0 \cdot 10^{-10}$
Electron magnetic moment	$\mu_{e}$	-9.2847647043(28)yJ/T	$3.0\cdot10^{-10}$
-	$\mu_{\rm e}/\mu_{\rm B}$	-1.001 159 652 181 28(18)	$1.7\cdot10^{-13}$
	$\mu_{\rm e}/\mu_{ m N}$	$-1838.28197188(11)\cdot 10^3$	$6.0\cdot10^{-11}$

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QUANTITY	Symbol	VALUE IN SI UNITS	Uncert.
Electron g-factor	$g_{ m e}$	-2.002 319 304 362 56(35)	$1.7\cdot 10^{-13}$
Muon-electron mass ratio	$m_{\mu}/m_{e}$	206.768 2830(46)	$2.2\cdot 10^{-8}$
Muon magnetic moment	$\mu_{\mu}$	$-4.49044830(10)\cdot10^{-26}\mathrm{J/T}$	$2.2\cdot 10^{-8}$
Muon g-factor	9μ	-2.002 331 8418(13)	$6.3\cdot 10^{-10}$
Atomic mass unit	$1 \mathrm{u} = m_{^{12}\mathrm{C}}/12$	$1.66053906660(50)\cdot 10^{-27}\mathrm{kg}$	$3.0\cdot 10^{-10}$
Proton mass	m <sub>p</sub>	$1.67262192369(51)\cdot 10^{-27}\mathrm{kg}$	$3.1\cdot 10^{-10}$
		1.007 276 466 621(53) u	$5.3\cdot 10^{-11}$
		938.272 088 16(29) MeV	$3.1\cdot10^{-10}$
Proton-electron mass ratio	$m_{\rm p}/m_{\rm e}$	1 836.152 673 43(11)	$6.0\cdot10^{-11}$
Specific proton charge	$e/m_{\rm p}$	$9.5788331560(29)\cdot 10^7\mathrm{C/kg}$	$3.1\cdot10^{-10}$
Proton Compton wavelength	$\lambda_{\rm C,p} = h/m_{\rm p}c$	1.321 409 855 39(40) fm	$3.1\cdot10^{-10}$
Nuclear magneton	$\mu_{\rm N} = e\hbar/2m_{\rm p}$	$5.0507837461(15)\cdot 10^{-27}$ J/T	$3.1\cdot10^{-10}$
Proton magnetic moment	$\mu_{ m p}$	$1.41060679736(60)\cdot 10^{-26}\mathrm{J/T}$	
	$\mu_{\rm p}/\mu_{\rm B}$	$1.52103220230(46)\cdot10^{-3}$	$3.0\cdot10^{-10}$
	$\mu_{\rm p}/\mu_{\rm N}$	2.792 847 344 63(82)	$2.9\cdot10^{-10}$
Proton gyromagnetic ratio	$\gamma_{\rm p} = 2\mu_p/h$	42.577 478 518(18) MHz/T	$4.2\cdot 10^{-10}$
Proton g factor	${\mathcal{G}}_{ m p}$	5.585 694 6893(16)	$2.9\cdot 10^{-10}$
Neutron mass	m <sub>n</sub>	$1.67492749804(95)\cdot10^{-27}\mathrm{kg}$	$5.7\cdot 10^{-10}$
		1.008 664 915 95(43) u	$4.8\cdot10^{-10}$
		939.565 420 52(54) MeV	$5.7\cdot10^{-10}$
Neutron-electron mass ratio	$m_{\rm n}/m_{\rm e}$	1 838.683 661 73(89)	$4.8\cdot10^{-10}$
Neutron-proton mass ratio	$m_{\rm n}/m_{\rm p}$	1.001 378 419 31(49)	$4.9\cdot 10^{-10}$
Neutron Compton wavelength	$\lambda_{\rm C,n} = h/m_{\rm n}c$	1.319 590 905 81(75) fm	$5.7 \cdot 10^{-10}$
Neutron magnetic moment	$\mu_{ m n}$	$-0.96623651(23)\cdot10^{-26}\mathrm{J/T}$	$2.4 \cdot 10^{-7}$
	$\mu_{ m n}/\mu_{ m B}$	$-1.04187563(25)\cdot10^{-3}$	$2.4 \cdot 10^{-7}$
	$\mu_{\rm n}/\mu_{\rm N}$	-1.913 042 73(45)	$2.4 \cdot 10^{-7}$
Stefan-Boltzmann constant	$\sigma = \pi^2 k^4 / 60\hbar^3 c^2$	56.703 744 19 nW/m <sup>2</sup> K <sup>4</sup>	0
Wien's displacement constant	$b = \lambda_{\max} T$	2.897 771 955 mmK	0
		58.789 257 57 GHz/K	0
Electron volt	eV	0.160 217 6634 aJ	0
Bits to entropy conversion cons	t. <i>k</i> ln 2	$10^{23}$ bit = 0.956 994 J/K	0
TNT energy content		3.7 to 4.0 MJ/kg	$4 \cdot 10^{-2}$

 TABLE 31 (Continued) Derived physical constants.

*a*. For infinite mass of the nucleus.

Some useful properties of our local environment are given in the following table.

QUANTITY	Symbol	Value
Tropical year 1900 <sup><i>a</i></sup>	а	31 556 925.974 7 s
Tropical year 1994	а	31 556 925.2 s
Mean sidereal day	d	23 <sup>h</sup> 56'4.090 53''
Average distance Earth-Sun <sup>b</sup>		149 597 870.691(30) km
Astronomical unit <sup>b</sup>	AU	149 597 870 691 m
Light year, based on Julian year <sup>b</sup>	al	9.460 730 472 5808 Pm
Parsec	pc	30.856 775 806 Pm = 3.261 634 al
Earth's mass	$M_{t}$	$5.973(1) \cdot 10^{24} \mathrm{kg}$
Geocentric gravitational constant	GM	$3.986004418(8)\cdot 10^{14}{m^3/s^2}$
Earth's gravitational length	$l_{\rm \odot}=2GM/c^2$	8.870 056 078(16) mm
Earth's equatorial radius <sup>c</sup>	R <sub>ðeq</sub>	6378.1366(1) km
	R <sub>ðp</sub>	6356.752(1) km
Equator–pole distance <sup>c</sup>	-	10 001.966 km (average)
Earth's flattening <sup>c</sup>	e <sub>t</sub>	1/298.25642(1)
Earth's av. density	$ ho_{\rm t}$	$5.5 \text{ Mg/m}^3$
	T <sub>t</sub>	4.54(5) Ga = 143(2) Ps
Earth's normal gravity	g	9.806 65 m/s <sup>2</sup>
Earth's standard atmospher. pressure	$p_0$	101 325 Pa
Moon's radius	$R_{(v)}$	1738 km in direction of Earth
Moon's radius	R <sub>ℂ h</sub>	1737.4 km in other two directions
Moon's mass	$M_{\mathbb{C}}$	$7.35 \cdot 10^{22} \text{ kg}$
Moon's mean distance <sup>d</sup>	$d_{\mathbb{Q}}$	384 401 km
Moon's distance at perigee <sup>d</sup>		typically 363 Mm, historical minimum 359 861 km
Moon's distance at apogee <sup>d</sup>		typically 404 Mm, historical maximum 406 720 km
Moon's angular size <sup>e</sup>		average 0.5181° = 31.08′, minimum 0.49°, maximum 0.55°
Moon's average density	$ ho_{\mathbb{C}}$	$3.3 \mathrm{Mg/m^3}$
Moon's surface gravity	9C	$1.62 \mathrm{m/s^2}$
Moon's atmospheric pressure	$P_{\mathbb{Q}}$	from $10^{-10}$ Pa (night) to $10^{-7}$ Pa (day)
lupiter's mass	$M_{2_{+}}$	$1.90 \cdot 10^{27} \text{ kg}$
lupiter's radius, equatorial	R <sub>2+</sub>	71.398 Mm
upiter's radius, polar	$R_{2+}$	67.1(1) Mm
Jupiter's average distance from Sun	$D_{2}$	778 412 020 km
Jupiter's surface gravity	<i>9</i> 4	$24.9 \mathrm{m/s^2}$
Jupiter's atmospheric pressure	$p_{2}$	from 20 kPa to 200 kPa
Sun's mass	$M_{\odot}$	$1.98843(3)\cdot10^{30}\mathrm{kg}$
	-	
	$2GM_{\odot}/c^2$	2.953 250 08(5) km

 TABLE 32
 Astronomical constants.

QUANTITY	Symbol	Value
Sun's luminosity	$L_{\odot}$	384.6 YW
Solar equatorial radius	$R_{\odot}$	695.98(7) Mm
Sun's angular size		0.53° average; minimum on fourth of July (aphelion) 1888″, maximum on fourth of January (perihelion) 1952″
Sun's average density	$ ho_{\odot}$	$1.4 \mathrm{Mg/m^3}$
Sun's average distance	AU	149 597 870.691(30) km
Sun's age	$T_{\odot}$	4.6 Ga
Solar velocity	$v_{\odot  m g}$	220(20) km/s
around centre of galaxy	0	
Solar velocity	$v_{\odot \mathrm{b}}$	370.6(5) km/s
against cosmic background		
Sun's surface gravity	$g_{\odot}$	$274 \mathrm{m/s^2}$
Sun's lower photospheric pressure	Рo	15 kPa
Distance to Milky Way's centre		8.0(5) kpc = $26.1(1.6)$ kal
Milky Way's age		13.6 Ga
Milky Way's size		<i>c</i> . 10 <sup>21</sup> m or 100 kal
Milky Way's mass		$10^{12}$ solar masses, <i>c</i> . $2 \cdot 10^{42}$ kg
Most distant galaxy cluster known	SXDF-XCLJ 0218-0510	$9.6 \cdot 10^9$ al

 TABLE 32 (Continued) Astronomical constants.

Challenge 192 s Ref. 288 *a*. Defining constant, from vernal equinox to vernal equinox; it was once used to define the second. (Remember:  $\pi$  seconds is about a nanocentury.) The value for 1990 is about 0.7 s less, corresponding to a slowdown of roughly 0.2 ms/a. (Watch out: why?) There is even an empirical formula for the change of the length of the year over time.

*b*. The truly amazing precision in the average distance Earth–Sun of only 30 m results from time averages of signals sent from Viking orbiters and Mars landers taken over a period of over twenty years. Note that the International Astronomical Union distinguishes the average distance Earth–Sun from the *astronomical unit* itself; the latter is defined as a fixed and exact length. Also the *light year* is a unit defined as an exact number by the IAU. For more details, see www.iau.org/ public/measuring.

*c*. The shape of the Earth is described most precisely with the World Geodetic System. The last edition dates from 1984. For an extensive presentation of its background and its details, see the www.wgs84.com website. The International Geodesic Union refined the data in 2000. The radii and the flattening given here are those for the 'mean tide system'. They differ from those of the 'zero tide system' and other systems by about 0.7 m. The details constitute a science in itself.

*d*. Measured centre to centre. To find the precise position of the Moon at a given date, see the www.fourmilab.ch/earthview/moon\_ap\_per.html page. For the planets, see the page www. fourmilab.ch/solar/solar.html and the other pages on the same site.

*e*. Angles are defined as follows: 1 degree =  $1^{\circ} = \pi/180$  rad, 1 (first) minute =  $1' = 1^{\circ}/60$ , 1 second (minute) = 1'' = 1'/60. The ancient units 'third minute' and 'fourth minute', each 1/60th of the preceding, are not in use any more. ('Minute' originally means 'very small', as it still does in

## A UNITS, MEASUREMENTS AND CONSTANTS

modern English.)

Challenge 193 s

Some properties of nature at large are listed in the following table. (If you want a challenge, can you determine whether any property of the universe itself is listed?)

TABLE 33 Cosmological constants.

QUANTITY	Symbol	Value
Cosmological constant	Λ	$c. 1 \cdot 10^{-52} \mathrm{m}^{-2}$
Age of the universe <sup><i>a</i></sup>	$t_0$	$4.333(53) \cdot 10^{17} \text{ s} = 13.8(0.1) \cdot 10^9 \text{ a}$
(determined from space-time, via e	xpansion, using gen	eral relativity)
Age of the universe <sup><i>a</i></sup>	$t_0$	over $3.5(4) \cdot 10^{17}$ s = $11.5(1.5) \cdot 10^9$ a
(determined from matter, via galaxi	es and stars, using q	uantum theory)
Hubble parameter <sup><i>a</i></sup>	$H_0$	$2.3(2) \cdot 10^{-18}  \text{s}^{-1} = 0.73(4) \cdot 10^{-10}  \text{a}^{-1}$
	$= h_0 \cdot 100 \mathrm{km/s}\mathrm{Mp}$	$bc = h_0 \cdot 1.0227 \cdot 10^{-10} a^{-1}$
Reduced Hubble parameter <sup>a</sup>	$h_0$	0.71(4)
Deceleration parameter <sup>a</sup>	$q_0 = -(\ddot{a}/a)_0 / H_0^2$	-0.66(10)
Universe's horizon distance <sup><i>a</i></sup>	$d_0 = 3ct_0$	$40.0(6) \cdot 10^{26} \mathrm{m} = 13.0(2) \mathrm{Gpc}$
Universe's topology		trivial up to 10 <sup>26</sup> m
Number of space dimensions		3, for distances up to $10^{26}$ m
Critical density	$\rho_{\rm c} = 3H_0^2/8\pi G$	$h_0^2 \cdot 1.87882(24) \cdot 10^{-26}\mathrm{kg/m^3}$
of the universe		$= 0.95(12) \cdot 10^{-26}  \mathrm{kg/m^3}$
(Total) density parameter <sup>a</sup>	$\Omega_0 = \rho_0 / \rho_c$	1.02(2)
Baryon density parameter <sup>a</sup>	$\Omega_{\rm B0} = \rho_{\rm B0} / \rho_{\rm c}$	0.044(4)
Cold dark matter density parameter <sup>a</sup>	$\Omega_{\rm CDM0} = \rho_{\rm CDM0} / \rho_{\rm c}$	0.23(4)
Neutrino density parameter <sup>a</sup>	$\Omega_{v0} = \rho_{v0} / \rho_{\rm c}$	0.001 to 0.05
Dark energy density parameter <sup>a</sup>	$\Omega_{\rm X0} = \rho_{\rm X0} / \rho_{\rm c}$	0.73(4)
Dark energy state parameter	$w = p_{\rm X}/\rho_{\rm X}$	-1.0(2)
Baryon mass	m <sub>b</sub>	$1.67 \cdot 10^{-27} \mathrm{kg}$
Baryon number density		$0.25(1)/m^3$
Luminous matter density		$3.8(2) \cdot 10^{-28}  \mathrm{kg/m^3}$
Stars in the universe	n <sub>s</sub>	$10^{22\pm1}$
Baryons in the universe	n <sub>b</sub>	$10^{81\pm1}$
Microwave background temperature <sup><i>l</i></sup>	' T <sub>0</sub>	2.725(1) K
Photons in the universe	$n_{\gamma}$	10 <sup>89</sup>
Photon energy density	$\rho_{\gamma}=\pi^2 k^4/15T_0^4$	$4.6 \cdot 10^{-31}  \mathrm{kg/m^3}$
Photon number density		$410.89 /\mathrm{cm}^3 \text{ or } 400 /\mathrm{cm}^3 (T_0/2.7 \mathrm{K})^3$
Density perturbation amplitude	$\sqrt{S}$	$5.6(1.5) \cdot 10^{-6}$
Gravity wave amplitude	$\sqrt{T}$	$< 0.71\sqrt{S}$
Mass fluctuations on 8 Mpc	$\sigma_8$	0.84(4)
Scalar index	n	0.93(3)
Running of scalar index	$dn/d \ln k$	-0.03(2)
Planck length	$l_{\rm Pl} = \sqrt{\hbar G/c^3}$	$1.62 \cdot 10^{-35} \mathrm{m}$

QUANTITY	Symbol	Value
Planck time	$t_{\rm Pl} = \sqrt{\hbar G/c^5}$	$5.39 \cdot 10^{-44}$ s
Planck mass	$m_{\rm Pl} = \sqrt{\hbar c/G}$	21.8 µg
Instants in history <sup><i>a</i></sup>	$t_0/t_{\rm Pl}$	$8.7(2.8) \cdot 10^{60}$
Space-time points	$N_0 = (R_0/l_{\rm Pl})^3 \cdot$	$10^{244\pm1}$
inside the horizon <sup><i>a</i></sup>	$(t_0/t_{\rm Pl})$	
Mass inside horizon	M	$10^{54\pm1}  \mathrm{kg}$

 TABLE 33 (Continued) Cosmological constants.

a. The index 0 indicates present-day values.

*b*. The radiation originated when the universe was 380 000 years old and had a temperature of about 3000 K; the fluctuations  $\Delta T_0$  which led to galaxy formation are today about  $16 \pm 4 \,\mu\text{K} = 6(2) \cdot 10^{-6} T_0$ .

# USEFUL NUMBERS

Ref. 289	π	$3.14159265358979323846264338327950288419716939937510_5$
	e	$2.71828182845904523536028747135266249775724709369995_9$
	γ	$0.57721566490153286060651209008240243104215933593992_3$
	ln 2	$0.69314718055994530941723212145817656807550013436025_5$
	ln 10	$2.30258509299404568401799145468436420760110148862877_2$
	$\sqrt{10}$	$3.16227766016837933199889354443271853371955513932521_6$



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# APPENDIX B COMPOSITE PARTICLE PROPERTIES

The following table lists the most important composite particles. he list has not changed much recently, mainly because of the vast progress hat was achieved already in the middle of the twentieth century. In principle, using the standard model of particle physics, all properties of composite matter and ra-Page 262 diation can be deduced. In particular, all properties of objects encountered in everyday life follow. (Can you explain how the size of an apple follows from the standard model?) The most important examples of composites are grouped in the following table.

Challenge 194 s

TABLE 34 Properties of selected composites.

Сомрозите	Mass <i>m</i> , quantum numbers <sup>a</sup>	LIFETIME $ au$ , MAIN DECAY MODES	Size (diam.)					
Mesons (hadrons, bosons) (selected from over 130 known types)								
Pion $\pi^0 (u\bar{u} - d\bar{d})/\sqrt{2}$	134.976 4(6) MeV/ $c^2$ $I^G(J^{PC}) = 1^-(0^{-+}), S = C$	$84(6)$ as, $2\gamma$ 98.798(32) % = $B = 0$	~ 1 fm					
Pion $\pi^+(u\bar{d})$	$139.56995(35)\mathrm{MeV}/c^2$		~ 1 fm					
	$I^{G}(J^{P}) = 1^{-}(0^{-}), S = C =$	1°						
Kaon $K_S^0$	$m_{K_s^0}$	89.27(9) ps	~ 1 fm					
Kaon $K_L^0$	$m_{K_{\rm s}^0}$ + 3.491(9) $\mu {\rm eV}/c^2$	51.7(4) ns	~ 1 fm					
Kaon $K^{\pm}$ ( $u\bar{s}, \bar{u}s$ )	493.677(16) MeV/c <sup>2</sup>	12.386(24) ns,	~ 1 fm					
		$\mu^+ \nu_\mu 63.51(18) \%$						
		$\pi^{+}\pi^{0}$ 21.16(14) %						
Kaon K <sup>0</sup> (dš) (50 % K <sub>S</sub> , 50 % K <sub>L</sub> )	$497.672(31) \mathrm{MeV}/c^2$	n.a.	~ 1 fm					
All kaons $K^{\pm}, K^0, K^0_S, K^0_L$ :	$I(J^P) = \frac{1}{2}(0^-), S = \pm 1, B =$	= C = 0						
Baryons (hadrons, fermior	ns) (selected from over 100 ]	known types)						
Proton $p$ or $N^+$ ( <i>uud</i> )	1.672 621 58(13) yg	$\tau_{\rm total} > 1.6 \cdot 10^{25}$ a,	0.89(1) fm					
	= 1.007 276 466 88(13) u	$\tau(p \to e^+ \pi^0) > 5.5 \cdot 10^{32} \mathrm{a}$	Ref. 290					
	= 938.271 998(38) MeV/c	2						
	$I(J^P) = \frac{1}{2}(\frac{1}{2}^+), S = 0$							
	gyromagnetic ratio $\mu_p/\mu_N = 2.792847337(29)$							
	electric dipole moment $d = (-4 \pm 6) \cdot 10^{-26} e$ m							

Composite	Mass <i>m</i> , quantum numbers <sup>a</sup>	LIFETIME $ au$ , MAIN DECAY MODES	Size (diam.)
	electric polarizability $\alpha_e$ = magnetic polarizability $\alpha_n$		
Neutron <sup><math>b</math></sup> $n$ or $N^0$ ( $udd$ )	1.674 927 16(13) yg = 1.008 664 915 78(55) u = $I(J^P) = \frac{1}{2}(\frac{1}{2}^+), S = 0$	887.0(2.0) s, $pe^{-}\bar{v}_{e}$ 100 % 939.565 330(38) MeV/ $c^{2}$	~ 1 fm
	gyromagnetic ratio $\mu_n/\mu_N$ electric dipole moment $d_n$ electric polarizability $\alpha =$	$h_{1} = (-3.3 \pm 4.3) \cdot 10^{-28} e m$ 0.98(23) $\cdot 10^{-3} fm^{3}$	
Omega $\Omega^-$ (sss)	1672.43(32) MeV/ <i>c</i> <sup>2</sup>	82.2(1.2) ps, $\Lambda K^-$ 67.8(7) %, $\Xi^0 \pi^-$ 23.6(7) %	~ 1 fm
	gyromagnetic ratio $\mu_{\Omega}/\mu_{N}$	$J_{J} = -1.94(22)$	
composite radiation: glueba	lls		
glueball candidate $f_0(1500)$ , status unclear		full width 120(19) MeV	~ 1 fm
	$I^G(J^{PC}) = 0^+(0^{++})$		
Atoms (selected from 114 km	own elements with over 20	000 known nuclides) Ref. 2	91
Hydrogen ( <sup>1</sup> H) [lightest]	$1.007825032(1)\mathrm{u} = 1.673$	5 yg	2 · 53 pm
Antihydrogen <sup>c</sup>	1.007 u = 1.67 yg		$2\cdot 53\mathrm{pm}$
Helium ( <sup>4</sup> He) [smallest]	$4.002603250(1)\mathrm{u} = 6.6469$	5 yg	$2\cdot 31\mathrm{pm}$
Carbon ( <sup>12</sup> C)	12 u = 19.926 482(12) yg		$2\cdot77\mathrm{pm}$
Bismuth ( <sup>209</sup> Bi <sup>*</sup> ) [shortest living and rarest]	209 u	0.1 ps Ref. 292	
Tantalum ( <sup>180m</sup> Ta) [second longest living radioactive]	180 u	> 10 <sup>15</sup> a Ref. 293	
Bismuth ( <sup>209</sup> Bi) [longest living radioactive]	209 u	1.9(2)10 <sup>19</sup> a Ref. 292	
Francium ( <sup>223</sup> Fr) [largest]	223 u	22 min	$2 \cdot 0.28  \text{nm}$
Oganesson ( <sup>289</sup> Og) [heaviest]	294 u	0.9 ms	
Molecules <sup>d</sup> (selected from o	over 10 <sup>7</sup> known types)		
Hydrogen (H <sub>2</sub> )	~ 2 u	$> 10^{25} a$	
Water ( $H_2O$ )	~ 18 u	$> 10^{25} a$	
ATP (adenosinetriphosphate)	507 u	> 10 <sup>10</sup> a	<i>c</i> . 3 nm
Human Y chromosome	$70 \cdot 10^6$ base pairs	> 10 <sup>6</sup> a	<i>c</i> . 50 mm (uncoiled)

 TABLE 34 (Continued) Properties of selected composites.

Сомрозіте	Mass <i>m</i> , quantum numbers <sup>a</sup>	LIFETIME $ au$ , MAIN DECAY MODES	S і z е ( d і а м . )
Other composites			
Blue whale nerve cell	~ 1 kg	~ 50 a	20 m
Cell (red blood)	0.1 ng	7 plus 120 days	~ 10 µm
Cell (sperm)	10 pg	not fecundated: ~ 5 d	length 60 μm, head 3 μm × 5 μm
Cell (ovule)	1 µg	fecundated: over 4000 million years	$\sim 120\mu m$
Cell (E. coli)	1 pg	4000 million years	body: 2 µm
Apple	0.1 kg	4 weeks	0.1 m
Adult human	35 kg < <i>m</i> < 350 kg	$\tau \approx 2.5 \cdot 10^9 \text{ s}  \text{Ref. 294}$ $\approx 600 \text{ million breaths}$ $\approx 2500 \text{ million heartbeats}$ < 122  a, $60 \% \text{ H}_2\text{O and 40 \% dust}$	~ 1.7 m
Heaviest living thing: colony of aspen trees	$6.6 \cdot 10^6 \text{ kg}$	> 130 a	> 4 km
Larger composites	See the table on page 260	in volume I.	

TABLE 34 (Continued) Properties of selected composites.

Page 264 Notes (see also the notes of Table 9):

*a*. The charge parity *C* is defined only for certain neutral particles, namely those that are different from their antiparticles. For neutral mesons, the charge parity is given by  $C = (-1)^{L+S}$ , where *L* is the orbital angular momentum.

*P* is the parity under space inversion  $r \rightarrow -r$ . For mesons, it is related to the orbital angular momentum *L* through  $P = (-1)^{L+1}$ .

The electric polarizability, defined on page 72 in volume III, is predicted to vanish for all elementary particles.

*G*-parity is defined only for mesons and given by  $G = (-1)^{L+S+I} = (-1)^I C$ .

*b*. Neutrons bound in nuclei have a lifetime of at least 10<sup>20</sup> years.

c. The first *anti-atoms*, made of antielectrons and antiprotons, were made in January 1996 at CERN
 Ref. 296 in Geneva. All properties of antimatter checked so far are consistent with theoretical predictions.
 d. The number of existing molecules is several orders of magnitude larger than the number of molecules that have been analysed and named.

The most important matter composites are the *atoms*. Their size, structure and interactions determine the properties and colour of everyday objects. Atom types, also called *elements* in chemistry, are most usefully set out in the so-called *periodic table*, which groups together atoms with similar properties in rows and columns. It is given in Table 35 and results from the various ways in which protons, neutrons and electrons can combine to form aggregates.

Comparable to the periodic table of the atoms, there are tables for the mesons (made of two quarks) and the baryons (made of three quarks). Neither the meson nor the baryon table is included here; they can both be found in the *Review of Particle Physics* at pdg.web.cern.ch. In fact, the baryon table still has a number of vacant spots. The missing baryons are extremely heavy and short-lived (which means expensive to make and detect), and their discovery is not expected to yield deep new insights.

TABLE 35 The periodic table of the elements, with their atomic numbers. Light blue: nonmetals, orange: alkali metals, green: alkaline earth metals, grey: transition metals, dark blue: basic metals, light orange: semimetals, yellow: halogens, brown: noble gases, red: lanthanoids, dark red: actinoids, black: no data.

Gro	oup																	
	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
	Ι	II	Illa	IVa	Va	Vla	Vlla		VIIIa		la	lla	III	IV	V	VI	VII	VIII
Pe	riod																	
1	1 <b>H</b>																	2 <b>He</b>
2	3	4											5	6	7	8	9	10
Z	Li	Be											В	С	Ν	0	F	Ne
3	11	12											13	14	15	16	17	18
2	Na	Mg											AI	Si	Ρ	S	CI	Ar
4	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
4	Κ	Са	Sc	Ti	V	Cr	Mn	Fe	Со	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
5	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54
5	Rb	Sr	Υ	Zr	Nb	Мо	Тс	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Те	Т	Хе
6	55	56		72	73	74	75	76	77	78	79	80	81	82	83	84	85	86
0	Cs	Ba	*	Hf	Та	W	Re	Os	Ir	Pt	Au	Hg	т	Pb	Bi	Ро	At	Rn
7	87	88		104	105	106	107	108	109	110	111	112	113	114	115	116	117	118
/	Fr	Ra	* *	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn	Nh	FI	Мс	Lv	Ts	Og
Lai	nthar	nids	*	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71
Lui	icitui	10103		La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Но	Er	Tm	Yb	Lu
٨	tinoio	اد	* *	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103
ΑC		12	ጥ ጥ	Ac	Th	Ра	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr

More elaborate periodic tables can be found on the chemlab.pc.maricopa.edu/periodic website. The most beautiful of them all can be found on page 61. The *atomic number* gives

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the number of protons (and electrons) found in an atom of a given element. This number determines the chemical behaviour of an element. Most – but not all – elements up to 92 are found on Earth; the others can be produced in laboratories. The highest element discovered is element 118. In a famous case of research fraud, a scientist in the 1990s tricked two whole research groups into claiming to have made and observed elements 116 and 118. Both elements were independently made and observed later on.

Ref. 297 Page 62 Nowadays, extensive physical and chemical data are available for every element. Photographs of the pure elements are shown in Figure 19. Elements in the same *group* behave similarly in chemical reactions. The *periods* define the repetition of these similarities.

The elements of group 1 are the *alkali metals* (though the exceptional hydrogen is a gas), those of group 2 are the alkaline earth metals. Also *actinoids*, *lanthanoids* are metals, as are the elements of groups 3 to 12, which are called *transition* or *heavy metals*. The elements of group 16 are called *chalkogens*, i.e., ore-formers; group 17 are the *halogens*, i.e., the salt-formers, and group 18 are the inert *noble gases*, which form (almost) no chemical compounds. The groups 13, 14 and 15 contain metals, semimetals, the only room-temperature liquid – bromine – and a few gases and non-metals; these groups have no special name. Groups 1 and 13 to 17 are central for the chemistry of life; in fact, 96% of living matter is made of C, O, N, H;\* almost 4% of P, S, Ca, K, Na, Cl; trace elements such as Mg, V, Cr, Mn, Fe, Co, Ni, Cu, Zn, Cd, Pb, Sn, Li, Mo, Se, Si, I, F, As, B form the rest. Over 30 elements are known to be essential for animal life. The full list is not yet known; candidate elements to extend this list are Al, Br, Ge and W.

Many elements exist in versions with different numbers of neutrons in their nucleus, and thus with different mass; these various *isotopes* – so called because they are found at the *same place* in the periodic table – behave identically in chemical reactions. There are over 2000 of them.

MAIN PROPERTIES,  $(NAMING)^h$  DIS-NAME Sym- Ат. AVER.  $MASS^a$ Ато-IN U (ERROR),  $MIC^{e}$ COVERY DATE AND USE BOL N. LONGEST RA-LIFETIME DIUS IN PM Actinium<sup>b</sup> 89 (227.0277(1))(188)Highly radioactive metallic rare Earth Ac (Greek aktis ray) 1899, used as alpha-21.77(2) a emitting source. 26.981 538 (8) 118c, Light metal (Latin alumen alum) 1827, Aluminium Al 13 stable 143m used in machine construction and living beings. Americium<sup>b</sup> 95 (243.0614(1))(184)Radioactive metal (Italian America from Am 7.37(2) ka Amerigo) 1945, used in smoke detectors.

Ref. 291, Ref. 298 OV

\* The 'average formula' of life is approximately  $\mathrm{C_5H_{40}O_{18}N}.$ 

 TABLE 36 The elements, with their atomic number, average mass, atomic radius and main properties.

 NAME
 SXM
 AT AVEP  $MAES^a$  ATO MAEN PROPERTIES  $(NAMEC)^h$ 

NAME	Sym-	Aт.	AVER. MASS <sup>a</sup>	Ато-	Main properties, $(naming)^h$ dis-
	BOL	N.	IN U (ERROR), LONGEST LIFETIME	, MIC <sup>e</sup> RA- DIUS IN PM	COVERY DATE AND USE
Antimony	Sb	51	121.760(1) <sup><i>f</i></sup> stable	137c, 159m, 205v	Toxic semimetal (via Arabic from Latin <i>stibium</i> , itself from Greek, Egyptian for one of its minerals) antiquity, colours rubber, used in medicines, constituent of enzymes.
Argon	Ar	18	39.948(1) <sup>f</sup> stable	(71n)	Noble gas (Greek <i>argos</i> inactive, from <i>anergos</i> without energy) 1894, third component of air, used for welding and in lasers.
Arsenic	As	33	74.92160(2) stable	120c, 185v	Poisonous semimetal (Greek <i>arsenikon</i> tamer of males) antiquity, for poisoning pigeons and doping semiconductors.
Astatine <sup>b</sup>	At	85	(209.9871(1)) 8.1(4) h	(140)	Radioactive halogen (Greek <i>astatos</i> un- stable) 1940, no use.
Barium	Ba	56	137.327(7) stable	224m	Earth-alkali metal (Greek <i>bary</i> heavy) 1808, used in vacuum tubes, paint, oil in- dustry, pyrotechnics and X-ray diagnosis.
Berkelium <sup>b</sup>	Bk	97	(247.0703(1)) 1.4(3) ka	n.a.	Made in lab, probably metallic (Berkeley, US town) 1949, no use because rare.
Beryllium	Be	4	9.012 182(3) stable	106c, 113m	Toxic Earth-alkali metal (Greek <i>beryllos</i> , a mineral) 1797, used in light alloys, in nuclear industry as moderator.
Bismuth	Bi	83	208.980 40(1) stable	170m, 215v	Diamagnetic metal (Latin via German <i>weisse Masse</i> white mass) 1753, used in magnets, alloys, fire safety, cosmetics, as catalyst, nuclear industry.
Bohrium <sup>b</sup>	Bh	107	(264.12(1)) $0.44 s^{g}$	n.a.	Made in lab, probably metallic (after Niels Bohr) 1981, found in nuclear reactions, no use.
Boron	В	5	10.811(7) <sup><i>f</i></sup> stable	83c	Semimetal, semiconductor (Latin <i>borax</i> , from Arabic and Persian for brilliant) 1808, used in glass, bleach, pyrotechnics, rocket fuel, medicine.
Bromine	Br	35	79.904(1) stable	120c, 185v	Red-brown liquid (Greek <i>bromos</i> strong odour) 1826, fumigants, photography, water purification, dyes, medicines.

TABLE 36 (Continued) The elements, with their atomic number, average mass, atomic radius and main properties.

TABLE 36 (Continued) The elements, with their atomic number, average mass, atomic radius and main properties.

1					
Nаме	Sym- bol	- Ат. N.	Aver. mass <sup>a</sup> in u (error) longest lifetime	Ato- , mic <sup>e</sup> ra- dius in pm	MAIN PROPERTIES, (NAMING) <sup>h</sup> dis- covery date and use
Cadmium	Cd	48	112.411(8) <sup>f</sup> stable	157m	Heavy metal, cuttable and screaming (Greek <i>kadmeia</i> , a zinc carbonate mineral where it was discovered) 1817, electro- plating, solder, batteries, TV phosphors dyes.
Caesium	Cs	55	132.905 4519(2) stable	273m	Alkali metal (Latin <i>caesius</i> sky blue) 1860, getter in vacuum tubes, photoelectric cells, ion propulsion, atomic clocks.
Calcium	Ca	20	40.078(4) <sup><i>f</i></sup> stable	197m	Earth-alkali metal (Latin <i>calcis</i> chalk) an- tiquity, pure in 1880, found in stones and bones, reducing agent, alloying.
Californium <sup>b</sup>	Cf	98	(251.0796(1)) 0.90(5)ka	n.a.	Made in lab, probably metallic, strong neutron emitter (Latin <i>calor</i> heat and <i>for- nicare</i> have sex, the land of hot sex :-) 1950, used as neutron source, for well log- ging.
Carbon	С	6	12.0107(8) <sup><i>f</i></sup> stable	77c	Makes up coal and diamond (Latin <i>carbo</i> coal) antiquity, used to build most life forms.
Cerium	Ce	58	140.116(1) <sup><i>f</i></sup> stable	183m	Rare Earth metal (after asteroid Ceres, Roman goddess) 1803, cigarette lighters, incandescent gas mantles, glass manu- facturing, self-cleaning ovens, carbon-arc lighting in the motion picture industry, catalyst, metallurgy.
Chlorine	Cl	17	35.453(2) <sup><i>f</i></sup> stable	102c, 175v	Green gas (Greek <i>chloros</i> yellow-green) 1774, drinking water, polymers, paper, dyes, textiles, medicines, insecticides, solvents, paints, rubber.
Chromium	Cr	24	51.9961(6) stable	128m	Transition metal (Greek <i>chromos</i> colour) 1797, hardens steel, makes steel stainless alloys, electroplating, green glass dye catalyst.
Cobalt	Co	27	58.933 195(5) stable	125m	Ferromagnetic transition metal (German <i>Kobold</i> goblin) 1694, part of vitamin $B_{12}$ , magnetic alloys, heavy-duty alloys enamel dyes, ink, animal nutrition.
Copernicium <sup>b</sup>	Cn	112	(285) 34 s <sup>g</sup>	n.a.	Made in lab, 1996, no use.

Name	Sym-		Aver. mass <sup>a</sup> in u (error),	Ато- міс <sup>е</sup>	MAIN PROPERTIES, $(NAMING)^h$ discovery date and use
	BOL	N.	IN U (ERROR), LONGEST	MIC RA-	COVERY DATE AND USE
			LIFETIME	DIUS	
				IN PM	
Copper	Cu	29	63.546(3) <sup><i>f</i></sup> stable	128m	Red metal (Latin <i>cuprum</i> from Cyprus is- land) antiquity, part of many enzymes, electrical conductors, bronze, brass and other alloys, algicides, etc.
Curium <sup>b</sup>	Cm	96	(247.0704(1)) 15.6(5) Ma	n.a.	Highly radioactive, silver-coloured (after Pierre and Marie Curie) 1944, used as ra- dioactivity source.
Darmstadtium <sup>b</sup>	Ds	110	(271) 1.6 min <sup>g</sup>	n.a.	Made in lab (after the German city) 1994, no use.
Dubnium <sup>b</sup>	Db	105	(262.1141(1)) 34(5) s	n.a.	Made in lab in small quantities, radio- active (Dubna, Russian city) 1967, no use (once known as hahnium).
Dysprosium	Dy	66	162.500(1) <sup><i>f</i></sup> stable	177m	Rare Earth metal (Greek <i>dysprositos</i> dif- ficult to obtain) 1886, used in laser ma- terials, as infrared source material, and in nuclear industry.
Einsteinium <sup>b</sup>	Es	99	(252.0830(1)) 472(2) d	n.a.	Made in lab, radioactive (after Albert Einstein) 1952, no use.
Erbium	Er	68	167.259(3) <sup><i>f</i></sup> stable	176m	Rare Earth metal (Ytterby, Swedish town) 1843, used in metallurgy and optical fibres.
Europium	Eu	63	151.964(1) <sup><i>f</i></sup> stable	204m	Rare Earth metal (named after the con- tinent) 1901, used in red screen phosphor for TV tubes.
Fermium <sup>b</sup>	Fm	100	(257.0901(1)) 100.5(2) d	n.a.	Made in lab (after Enrico Fermi) 1952, no use.
Flerovium <sup>b</sup>	Fl	114	(289)	2.7 s <sup>g</sup>	1999, no use.
Fluorine	F	9	18.998 4032(5) stable	62c, 147v	Gaseous halogen (from fluorine, a min- eral, from Greek <i>fluo</i> flow) 1886, used in polymers and toothpaste.
Francium <sup>b</sup>	Fr	87	(223.0197(1)) 22.0(1) min	(278)	Radioactive metal (from France) 1939, no use.
Gadolinium	Gd	64	157.25(3) <sup><i>f</i></sup> stable	180m	Rare-earth metal (after Johan Gadolin) 1880, used in lasers and phosphors.
Gallium	Ga	31	69.723(1) stable	125c, 141m	Almost liquid metal (Latin for both the discoverer's name and his nation, France) 1875, used in optoelectronics.

 TABLE 36 (Continued) The elements, with their atomic number, average mass, atomic radius and main properties.

 TABLE 36 (Continued) The elements, with their atomic number, average mass, atomic radius and main properties.

NAME	SVM	- Ат.	Aver. mass <sup>a</sup>	Ато-	Main properties, $(naming)^h$ dis-
	-	N.	IN U (ERROR) LONGEST LIFETIME		COVERY DATE AND USE
Germanium	Ge	32	72.64(1) stable	122c, 195v	Semiconductor (from Germania, as opposed to gallium) 1886, used in electronics.
Gold	Au	79	196.966 569(4) stable	144m	Heavy noble metal (Sanskrit <i>jval</i> to shine, Latin aurum) antiquity, electronics, jewels.
Hafnium	Hf	72	178.49(2) <sup>c</sup> stable	158m	Metal (Latin for Copenhagen) 1923, al- loys, incandescent wire.
Hassium <sup>b</sup>	Hs	108	(277) 16.5 min <sup>g</sup>	n.a.	Radioactive element (Latin form of Ger- man state Hessen) 1984, no use .
Helium	He	2	4.002 602(2) <sup><i>f</i></sup> stable	(31n)	Noble gas (Greek <i>helios</i> Sun) where it was discovered 1895, used in balloons, stars, diver's gas and cryogenics.
Holmium	Но	67	164.930 32(2) stable	177m	Metal (Stockholm, Swedish capital) 1878, alloys.
Hydrogen	Н	1	1.007 94(7) <sup>f</sup> stable	30c	Reactive gas (Greek for water-former) 1766, used in building stars and universe.
Indium	In	49	114.818(3) stable	141c, 166m	Soft metal (Greek <i>indikon</i> indigo) 1863, used in solders and photocells.
Iodine	Ι	53	126.904 47(3) stable	140c, 198v	Blue-black solid (Greek <i>iodes</i> violet) 1811, used in photography.
Iridium	Ir	77	192.217(3) stable	136m	Precious metal (Greek <i>iris</i> rainbow) 1804, electrical contact layers.
Iron	Fe	26	55.845(2) stable	127m	Metal (Indo-European <i>ayos</i> metal, Latin ferrum) antiquity, used in metallurgy.
Krypton	Kr	36	83.798(2) <sup>f</sup> stable	(88n)	Noble gas (Greek <i>kryptos</i> hidden) 1898, used in lasers.
Lanthanum	La	57	138.905 47(7) <sup><i>c</i>,<i>f</i></sup> stable	188m	Reactive rare Earth metal (Greek <i>lanthanein</i> to be hidden) 1839, used in lamps and in special glasses.
Lawrencium <sup>b</sup>	Lr	103	(262.110 97(1)) 3.6(3) h	n.a.	Appears in reactions (after Ernest Lawrence) 1961, no use.
Lead	Pb	82	207.2(1) <sup><i>c</i>, <i>f</i></sup> stable	175m	Poisonous, malleable heavy metal (Latin <i>plumbum</i> ) antiquity, used in car batteries, radioactivity shields, paints.
Lithium	Li	3	6.941(2) <sup><i>f</i></sup> stable	156m	Light alkali metal with high specific heat (Greek <i>lithos</i> stone) 1817, used in batter- ies, anti-depressants, alloys, nuclear fu-

sion and many chemicals.

Name	Sym- bol		Aver. mass <sup>a</sup> in u (error); longest lifetime	Ato- mic <sup>e</sup> ra- dius in pm	MAIN PROPERTIES, (NAMING) <sup>h</sup> DIS- COVERY DATE AND USE
Livermorium <sup>b</sup>	Lv	116	(293)	61 ms <sup>g</sup>	False discovery claim from 1999, correct claim from 2000, no use.
Lutetium	Lu	71	174.967(1) <sup>f</sup> stable	173m	Rare-earth metal (Latin <i>Lutetia</i> for Paris) 1907, used as catalyst.
Magnesium	Mg	12	24.3050(6) stable	160m	Light common alkaline Earth metal (from Magnesia, a Greek district in Thes- salia) 1755, used in alloys, pyrotechnics, chemical synthesis and medicine, found in chlorophyll.
Manganese	Mn	25	54.938 045(5) stable	126m	Brittle metal (Italian <i>manganese</i> , a mineral) 1774, used in alloys, colours amethyst and permanganate.
Meitnerium <sup>b</sup>	Mt	109	(268.1388(1)) 0.070 s <sup>g</sup>	n.a.	Appears in nuclear reactions (after Lise Meitner) 1982, no use.
Mendelevium <sup>b</sup>	Md	101	(258.0984(1)) 51.5(3) d	n.a.	Appears in nuclear reactions (after Дмитрии Иванович Менделеев Dmitriy Ivanovich Mendeleyev) 1955, no use.
Mercury	Hg	80	200.59(2) stable	157m	Liquid heavy metal (Latin god Mer- curius, Greek <i>hydrargyrum</i> liquid sil- ver) antiquity, used in switches, batteries, lamps, amalgam alloys.
Molybdenum	Мо	42	95.94(2) <sup>f</sup> stable	140m	Metal (Greek <i>molybdos</i> lead) 1788, used in alloys, as catalyst, in enzymes and lub- ricants.
Moscovium <sup>b</sup>	Mc	115	(288)	8 ms <sup>g</sup>	2004 (Moscow), no use.
Neodymium	Nd	60	144.242(3) <sup>c,f</sup> stable	182m	(Greek <i>neos</i> and <i>didymos</i> new twin) 1885, used in magnets.
Neon	Ne	10	20.1797(6) <sup>f</sup> stable	(36n)	Noble gas (Greek <i>neos</i> new) 1898, used in lamps, lasers and cryogenics.
Neptunium <sup>b</sup>	Np	93	(237.0482(1)) 2.14(1) Ma	n.a.	Radioactive metal (planet Neptune, after Uranus in the solar system) 1940, appears in nuclear reactors, used in neutron de- tection and by the military.
Nickel	Ni	28	58.6934(2) stable	125m	Metal (German <i>Nickel</i> goblin) 1751, used in coins, stainless steels, batteries, as cata- lyst.
Nihonium <sup>b</sup>	Nh	113	(284)	$0.48\mathrm{s}^g$	2003 (Nihon is Japan in Japanese), no use.

TABLE 36 (Continued) The elements, with their atomic number, average mass, atomic radius and main properties.

 TABLE 36 (Continued) The elements, with their atomic number, average mass, atomic radius and main properties.

Name	Sym-	Ат.	Aver. mass <sup>a</sup>	Ато-	Main properties, $(naming)^h$ dis-
		N.	IN U (ERROR), LONGEST LIFETIME		COVERY DATE AND USE
Niobium	Nb	41	92.906 38(2) stable	147m	Ductile metal (Greek Niobe, mythical daughter of Tantalos) 1801, used in arc welding, alloys, jewellery, superconduct- ors.
Nitrogen	Ν	7	14.0067(2) <sup><i>f</i></sup> stable	70c, 155v	Diatomic gas (Greek for nitre-former) 1772, found in air, in living organisms, Viagra, fertilizers, explosives.
Nobelium <sup>b</sup>	No	102	(259.1010(1)) 58(5) min	n.a.	(after Alfred Nobel) 1958, no use.
Oganesson <sup>b</sup>	Og	118	(294)	0.9 ms <sup>g</sup>	False discovery claim in 1999, correct claim from 2006 (after Yuri Oganessian), no use.
Osmium	Os	76	190.23(3) <sup><i>f</i></sup> stable	135m	Heavy metal (from Greek <i>osme</i> odour) 1804, used for fingerprint detection and in very hard alloys.
Oxygen	Ο	8	15.9994(3) <sup><i>f</i></sup> stable	66c, 152v	Transparent, diatomic gas (formed from Greek to mean 'acid former') 1774, used for combustion, blood regeneration, to make most rocks and stones, in countless compounds, colours auroras red.
Palladium	Pd	46	106.42(1) <sup><i>f</i></sup> stable	138m	Heavy metal (from asteroid Pallas, after the Greek goddess) 1802, used in alloys, white gold, catalysts, for hydride storage.
Phosphorus	Р	15	30.973 762(2) stable	109c, 180v	Poisonous, waxy, white solid (Greek <i>phosphoros</i> light bearer) 1669, fertilizers, glasses, porcelain, steels and alloys, living organisms, bones.
Platinum	Pt	78	195.084(9) stable	139m	Silvery-white, ductile, noble heavy metal (Spanish <i>platina</i> little silver) pre-Columbian, again in 1735, used in corrosion-resistant alloys, magnets, furnaces, catalysts, fuel cells, cathodic protection systems for large ships and pipelines; being a catalyst, a fine plat- inum wire glows red hot when placed in vapour of methyl alcohol, an effect used in hand warmers.

NAME	Sym- bol		Aver. mass <sup>a</sup> in u (error); longest lifetime	Ato- Mic <sup>e</sup> RA- Dius In PM	MAIN PROPERTIES, (NAMING) <sup>h</sup> dis- covery date and use
Plutonium	Pu	94	(244.0642(1)) 80.0(9) Ma	n.a.	Extremely toxic alpha-emitting metal (after the planet) synthesized 1940, found in nature 1971, used as nuclear explosive, and to power space equipment, such as satellites and the measurement equip- ment brought to the Moon by the Apollo missions.
Polonium	Ро	84	(208.9824(1)) 102(5) a	(140)	Alpha-emitting, volatile metal (from Po- land) 1898, used as thermoelectric power source in space satellites, as neutron source when mixed with beryllium; used in the past to eliminate static charges in factories, and on brushes for removing dust from photographic films.
Potassium	K	19	39.0983(1) stable	238m	Reactive, cuttable light metal (German <i>Pottasche</i> , Latin <i>kalium</i> from Arabic <i>quilyi</i> , a plant used to produce potash) 1807, part of many salts and rocks, essential for life, used in fertilizers, essential to chemical industry.
Praeseodymiur	n Pr	59	140.907 65(2) stable	183m	White, malleable rare Earth metal (Greek <i>praesos didymos</i> green twin) 1885, used in cigarette lighters, material for carbon arcs used by the motion picture industry for studio lighting and projection, glass and enamel dye, darkens welder's goggles.
Promethium <sup>b</sup>	Pm	61	(144.9127(1)) 17.7(4) a	181m	Radioactive rare Earth metal (from the Greek mythical figure of Prometheus) 1945, used as $\beta$ source and to excite phosphors.
Protactinium	Pa	91	(231.035 88(2)) 32.5(1) ka	n.a.	Radioactive metal (Greek <i>protos</i> first, as it decays into actinium) 1917, found in nature, no use.
Radium	Ra	88	(226.0254(1)) 1599(4) a	(223)	Highly radioactive metal (Latin <i>radius</i> ray) 1898, no use any more; once used in luminous paints and as radioactive source and in medicine.

 TABLE 36 (Continued) The elements, with their atomic number, average mass, atomic radius and main properties.

 TABLE 36 (Continued) The elements, with their atomic number, average mass, atomic radius and main properties.

Name	Sүм-	· Ат.	Aver. $mass^a$	Ато-	Main properties, $(naming)^h$ dis-
	BOL	N.	IN U (ERROR), LONGEST LIFETIME	, MIC <sup>e</sup> RA- DIUS IN PM	COVERY DATE AND USE
Radon	Rn	86	(222.0176(1)) 3.823(4) d	(130n)	Radioactive noble gas (from its old name 'radium emanation') 1900, no use (any more), found in soil, produces lung can- cer.
Rhenium	Re	75	186.207(1) <sup><i>c</i></sup> stable	138m	TRansition metal (Latin <i>rhenus</i> for Rhine river) 1925, used in filaments for mass spectrographs and ion gauges, supercon- ductors, thermocouples, flash lamps, and as catalyst.
Rhodium	Rh	45	102.905 50(2) stable	135m	White metal (Greek <i>rhodon</i> rose) 1803, used to harden platinum and palladium alloys, for electroplating, and as catalyst.
Roentgenium <sup>b</sup>	Rg	111	(272.1535(1)) 1.5 ms <sup>g</sup>	n.a.	Made in lab (after Conrad Roentgen) 1994, no use.
Rubidium	Rb	37	85.4678(3) <sup><i>f</i></sup> stable	255m	Silvery-white, reactive alkali metal (Latin <i>rubidus</i> red) 1861, used in photocells, optical glasses, solid electrolytes.
Ruthenium	Ru	44	101.107(2) <sup><i>f</i></sup> stable	134m	White metal (Latin <i>Rhuthenia</i> for Russia) 1844, used in platinum and palladium alloys, superconductors, as catalyst; the tetroxide is toxic and explosive.
Rutherfordium <sup><i>l</i></sup>	' Rf	104	(261.1088(1)) 1.3 min <sup>g</sup>	n.a.	Radioactive transactinide (after Ernest Rutherford) 1964, no use.
Samarium	Sm	62	150.36(2) <sup><i>c</i>,<i>f</i></sup> stable	180m	Silver-white rare Earth metal (from the mineral samarskite, after Wassily Samarski) 1879, used in magnets, optical glasses, as laser dopant, in phosphors, in high-power light sources.
Scandium	Sc	21	44.955 912(6) stable	164m	Silver-white metal (from Latin <i>Scansia</i> Sweden) 1879, the oxide is used in high-intensity mercury vapour lamps, a radio-active isotope is used as tracer.
Seaborgium <sup>b</sup>	Sg	106	266.1219(1) 21 s <sup>g</sup>	n.a.	Radioactive transurane (after Glenn Seaborg) 1974, no use.
Selenium	Se	34	78.96(3) <sup><i>f</i></sup> stable	120c, 190v	Red or black or grey semiconductor (Greek <i>selene</i> Moon) 1818, used in xer- ography, glass production, photographic toners, as enamel dye.

Nаме		- Ат. N.	Aver. mass <sup>a</sup> in u (error), longest lifetime	Ato- mic <sup>e</sup> ra- dius in pm	MAIN PROPERTIES, (NAMING) <sup>h</sup> dis- covery date and use
Silver	Ag	47	107.8682(2) <sup><i>f</i></sup> stable	145m	White metal with highest thermal and electrical conductivity (Latin <i>argentum</i> , Greek <i>argyros</i> ) antiquity, used in photo- graphy, alloys, to make rain.
Sodium	Na	11	22.989 769 28(2) stable	191m	Light, reactive metal (Arabic <i>souwad</i> soda, Egyptian and Arabic <i>natrium</i> ) component of many salts, soap, paper, soda, salpeter, borax, and essential for life.
Strontium	Sr	38	87.62(1) <sup><i>f</i></sup> stable	215m	Silvery, spontaneously igniting light metal (Strontian, Scottish town) 1790, used in TV tube glass, in magnets, and in optical materials.
Sulphur	S	16	32.065(5) <sup><i>f</i></sup> stable	105c, 180v	Yellow solid (Latin) antiquity, used in gunpowder, in sulphuric acid, rubber vul- canization, as fungicide in wine produc- tion, and is essential for life; some bac- teria use sulphur instead of oxygen in their chemistry.
Tantalum	Та	73	180.947 88(2) stable	147m	Heavy metal (Greek Tantalos, a mythical figure) 1802, used for alloys, surgical in- struments, capacitors, vacuum furnaces, glasses.
Technetium <sup>b</sup>	Tc	43	(97.9072(1)) 6.6(10) Ma	136m	Radioactive (Greek <i>technetos</i> artificial) 1939, used as radioactive tracer and in nuclear technology.
Tellurium	Те	52	127.60(3) <sup><i>f</i></sup> stable	139c, 206v	Brittle, garlic-smelling semiconductor (Latin <i>tellus</i> Earth) 1783, used in alloys and as glass component.
Tennessine <sup>b</sup>	Ts	117	(294)	$78\mathrm{ms}^g$	2010 (Tennessee), no use.
Terbium	Tb	65	158.925 35(2) stable	178m	Malleable rare Earth metal (Ytterby, Swedish town) 1843, used as dopant in optical material.
Thallium	Tl	81	204.3833(2) stable	172m	Soft, poisonous heavy metal (Greek <i>thallos</i> branch) 1861, used as poison and for infrared detection.

 TABLE 36 (Continued) The elements, with their atomic number, average mass, atomic radius and main properties.

TABLE 36 (Continued) The elements, with their atomic number, average mass, atomic radius and main properties.

NAME	Sym- bol		Aver. mass <sup>a</sup> in u (error), longest lifetime	Ato- mic <sup>e</sup> ra- dius in pm	Main properties, $(naming)^h$ discovery date and use
Thorium	Th	90	232.038 06(2) <sup><i>d</i>,<i>f</i></sup> 14.0(1) Ga	180m	Radioactive (Nordic god Thor, as in 'Thursday') 1828, found in nature, heats Earth, used as oxide in gas mantles for campers, in alloys, as coating, and in nuc- lear energy.
Thulium	Tm	69	168.934 21(2) stable	175m	Rare Earth metal (Thule, mythical name for Scandinavia) 1879, found in monazite, used in lasers and radiation detectors.
Tin	Sn	50	118.710(7) <sup><i>f</i></sup> stable	139c, 210v, 162m	Grey metal that, when bent, allows one to hear the 'tin cry' (Latin <i>stannum</i> ) an- tiquity, used in paint, bronze and super- conductors.
Titanium	Ti	22	47.867(1) stable	146m	Metal (Greek hero Titanos) 1791, alloys, fake diamonds.
Tungsten	W	74	183.84(1) stable	141m	Heavy, highest-melting metal (Swedish <i>tung sten</i> heavy stone, German name <i>Wolfram</i> ) 1783, lightbulbs.
Uranium	U	92	$238.028  91(3)^{d,f}$ $4.468(3) \cdot 10^9  a$	156m	Radioactive and of high density (planet Uranus, after the Greek sky god) 1789, found in pechblende and other minerals, used for nuclear energy.
Vanadium	V	23	50.9415(1) stable	135m	Metal (Vanadis, scandinavian goddess of beauty) 1830, used in steel.
Xenon	Xe	54	131.293(6) <sup>f</sup> stable	(103n) 200v	Noble gas (Greek <i>xenos</i> foreign) 1898, used in lamps and lasers.
Ytterbium	Yb	70	173.04(3) <sup><i>f</i></sup> stable	174m	Malleable heavy metal (Ytterby, Swedish town) 1878, used in superconductors.
Yttrium	Y	39	88.905 85(2) stable	180m	Malleable light metal (Ytterby, Swedish town) 1794, used in lasers.
Zinc	Zn	30	65.409(4) stable	139m	Heavy metal (German <i>Zinke</i> protuber- ance) antiquity, iron rust protection.
Zirconium	Zr	40	91.224(2) <sup><i>f</i></sup> stable	160m	Heavy metal (from the mineral zircon, after Arabic <i>zargum</i> golden colour) 1789, chemical and surgical instruments, nuclear industry.

*a*. The atomic mass unit is defined as  $1 \text{ u} = \frac{1}{12}m(^{12}\text{C})$ , making 1 u = 1.6605402(10) yg. For elements found on Earth, the *average* atomic mass for the naturally occurring isotope mixture is given, with the error in the last digit in brackets. For elements not found on Earth, the mass of

Ref. 298

the *longest living* isotope is given; as it is not an average, it is written in brackets, as is customary in this domain.

b. The element is not found on Earth because of its short lifetime.

c. The element has at least one radioactive isotope.

*d*. The element has no stable isotopes.

*e*. Strictly speaking, the *atomic radius* does not exist. Because atoms are clouds, they have no boundary. Several approximate definitions of the 'size' of atoms are possible. Usually, the radius is defined in such a way as to be useful for the estimation of distances between atoms. This distance

Ref. 299

Ref. 299 for

is different for different bond types. In the table, radii for metallic bonds are labelled m, radii for (single) covalent bonds with carbon c, and Van der Waals radii v. Noble gas radii are labelled n. Note that values found in the literature vary by about 10 %; values in brackets lack literature references.

The covalent radius can be up to 0.1 nm smaller than the metallic radius for elements on the (lower) left of the periodic table; on the (whole) right side it is essentially equal to the metallic radius. In between, the difference between the two decreases towards the right. Can you explain why? By the way, ionic radii differ considerably from atomic ones, and depend both on the ionic charge and the element itself.

All these values are for atoms in their ground state. Excited atoms can be hundreds of times larger than atoms in the ground state; however, excited atoms do not form solids or chemical compounds.

f. The isotopic composition, and thus the average atomic mass, of the element varies depending on the place where it was mined or on subsequent human treatment, and can lie outside the values given. For example, the atomic mass of commercial lithium ranges between 6.939 and 6.996 u. The masses of isotopes are known in atomic mass units to nine or more significant digits,

and usually with one or two fewer digits in kilograms. The errors in the atomic mass are thus Ref. 298 mainly due to the variations in isotopic composition.

g. The lifetime errors are asymmetric or not well known.

h. Extensive details on element names can be found on elements.vanderkrogt.net.

Challenge 195 s

Ref. 291

# APPENDIX C ALGEBRAS, SHAPES AND GROUPS

A sthematicians are fond of generalizing concepts. One of the ost generalized concepts of all is the concept of *space*. Understanding athematical definitions and generalizations means learning to think with precision. The appendix of the previous, fourth volume provided a simple introduction to the types of *spaces* that are of importance in physics; this appendix provides an introduction to the *algebras* that are of importance in physics.

## ALGEBRAS

The term *algebra* is used in mathematics with three different, but loosely related, meanings. First, it denotes a part of mathematics, as in 'I hated algebra at school'. Secondly, it denotes a set of formal rules that are obeyed by abstract objects, as in the expression 'tensor algebra'. Finally – and this is the only meaning used here – an algebra denotes a *specific* type of mathematical structure.

Intuitively, an algebra is a set of vectors with a vector multiplication defined on it. More precisely, a (unital, associative) algebra is a vector space (over a field K) that is also a (unital) ring. (The concept is due to Benjamin Peirce (b. 1809 Salem, d. 1880 Cambridge), father of Charles Sanders Peirce.) A ring is a set for which an addition and a multiplication is defined – like the integers. Thus, in an algebra, there are (often) *three* types of multiplications:

- the (main) algebraic multiplication: the product of two vectors x and y is another vector z = xy;
- the scalar multiplication: the *c*-fold multiple of a vector *x* is another vector y = cx;
- if the vector space is a inner product space, the scalar product: the scalar product of two algebra elements (vectors) x and y is a scalar  $c = x \cdot y$ ;

A precise definition of an algebra thus only needs to define properties of the (main) multiplication and to specify the number field *K*. An *algebra* is defined by the following axioms

$$x(y+z) = xy + xz$$
,  $(x + y)z = xz + yz$  distributivity of multiplication  
 $c(xy) = (cx)y = x(cy)$  bilinearity (139)

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for all vectors x, y, z and all scalars  $c \in K$ . To stress their properties, algebras are also called *linear* algebras.

For example, the set of all linear transformations of an *n*-dimensional linear space (such as the translations on a plane, in space or in time) is a linear algebra, if the composition is taken as multiplication. So is the set of observables of a quantum mechanical system.\*

An associative algebra is an algebra whose multiplication has the additional property that

$$x(yz) = (xy)z$$
 associativity. (141)

Most algebras that arise in physics are associative\*\* and unital. Therefore, in mathematical physics, a linear unital associative algebra is often simply called an algebra.

The set of multiples of the unit 1 of the algebra is called the *field of scalars* scal(A) of the algebra A. The field of scalars is also a subalgebra of A. The field of scalars and the scalars themselves behave in the same way.

We explore a few examples. The set of all polynomials in one variable (or in several variables) forms an algebra. It is commutative and infinite-dimensional. The constant polynomials form the field of scalars.

The set of  $n \times n$  matrices, with the usual operations, also forms an algebra. It is  $n^2$ dimensional. Those diagonal matrices (matrices with all off-diagonal elements equal to zero) whose diagonal elements all have the same value form the field of scalars. How is the scalar product of two matrices defined?

The set of all real-valued functions over a set also forms an algebra. Can you specify the multiplication? The constant functions form the field of scalars.

A star algebra, also written \*-algebra, is an algebra over the complex numbers for

$$T(e) = \lambda e \tag{140}$$

where  $\lambda$  is a scalar, then the vector *e* is called an *eigenvector* of *T*, and  $\lambda$  is associated *eigenvalue*. The set of all eigenvalues of a transformation T is called the *spectrum* of T. Physicists did not pay much attention to these mathematical concepts until they discovered quantum theory. Quantum theory showed that observables are transformations in Hilbert space, because any measurement interacts with a system and thus transforms it. Quantum-mechanical experiments also showed that a measurement result for an observable must be an eigenvalue of the corresponding transformation. The state of the system after the measurement is given by the eigenvector corresponding to the measured eigenvalue. Therefore every expert on motion must know what an eigenvalue is.

Challenge 197 e

Challenge 198 ny

Challenge 199 s

Challenge 196 s

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<sup>\*</sup> Linear transformations are mappings from the vector space to itself, with the property that sums and scalar multiples of vectors are transformed into the corresponding sums and scalar multiples of the transformed vectors. Can you specify the set of all linear transformations of the plane? And of three-dimensional space? And of Minkowski space?

All linear transformations transform some special vectors, called eigenvectors (from the German word eigen meaning 'self') into multiples of themselves. In other words, if T is a transformation, e a vector, and

which there is a mapping  $* : A \to A, x \mapsto x^*$ , called an *involution*, with the properties

$$(x^{*})^{*} = x$$
  

$$(x + y)^{*} = x^{*} + y^{*}$$
  

$$(cx)^{*} = \overline{c}x^{*} \text{ for all } c \in \mathbb{C}$$
  

$$(xy)^{*} = y^{*}x^{*}$$
(142)

valid for all elements x, y of the algebra A. The element  $x^*$  is called the *adjoint* of x. Star algebras are the main type of algebra used in quantum mechanics, since quantum-mechanical observables form a \*-algebra.

A C\*-*algebra* is a Banach algebra over the complex numbers with an involution \* (a function that is its own inverse) such that the norm ||x|| of an element x satisfies

$$\|x\|^2 = x^* x . (143)$$

(A Banach algebra is a complete normed algebra; an algebra is *complete* if all Cauchy sequences converge.) In short, C\*-*algebra* is a nicely behaved algebra whose elements form a continuous set and a complex vector space. The name C comes from 'continuous functions'. Indeed, the *bounded* continuous functions form such an algebra, with a properly defined norm. Can you find it?

Every C\*-algebra (pronounced 'Cee-star') contains a space of Hermitean elements (which have a real spectrum), a set of normal elements, a multiplicative group of unitary elements and a set of positive elements (with non-negative spectrum). In quantum theory, a physical system is described by a C\*-algebra, and its Hermitean elements are the observables.

We should mention one important type of algebra used in mathematics. A *division algebra* is an algebra for which the equations ax = b and ya = b are uniquely solvable in x or y for all b and all  $a \neq 0$ . Obviously, all type of continuous numbers must be division algebras. Division algebras are thus one way to generalize the concept of a number. One of the important results of modern mathematics states that (finite-dimensional) division algebras can *only* have dimension 1, like the reals, dimension 2, like the complex numbers, dimension 4, like the quaternions, or dimension 8, like the octonions. There is thus no way to generalize the concept of (continuous) 'number' to other dimensions.

And now for some fun. Imagine a ring A which contains a number field K as a subring (or 'field of scalars'). If the ring multiplication is defined in such a way that a general ring element multiplied with an element of K is the same as the scalar multiplication, then A is a vector space, and thus an algebra – *provided* that every element of K commutes with every element of A. (In other words, the subring K must be *central*.)

For example, the quaternions  $\mathbb{H}$  are a four-dimensional real division algebra, but although  $\mathbb{H}$  is a two-dimensional complex vector space, it is *not* a complex algebra, because *i* does not commute with *j* (one has ij = -ji = k). In fact, there are no finite-dimensional complex division algebras, and the only finite-dimensional real associative division algebras are  $\mathbb{R}$ ,  $\mathbb{C}$  and  $\mathbb{H}$ .

Now, if you are not afraid of getting a headache, think about this remark: every Kalgebra is also an algebra over its field of scalars. For this reason, some mathematicians

Challenge 200 s d

prefer to define an (associative) K-algebra simply as a ring which contains K as a central subfield.

In physics, it is the algebras related to symmetries which play the most important role. We study them next.

## LIE ALGEBRAS

A Lie algebra is special type of algebra (and thus of vector space). Lie algebras are the most important type of non-associative algebras. A vector space *L* over the field  $\mathbb{R}$  (or  $\mathbb{C}$ ) with an additional binary operation [, ], called *Lie multiplication* or the *commutator*, is called a real (or complex) *Lie algebra* if this operation satisfies

$$[X, Y] = -[Y, X] \quad antisymmetry$$
$$[aX + bY, Z] = a[X, Z] + b[Y, Z] \quad (left-)linearity$$
$$[X, [Y, Z]] + [Y, [Z, X]] + [Z, [X, Y]] = 0 \quad Jacobi \ identity \qquad (144)$$

Challenge 201 e

for all elements  $X, Y, Z \in L$  and for all  $a, b \in \mathbb{R}$  (or  $\mathbb{C}$ ). (Lie algebras are named after Sophus Lie.) The first two conditions together imply bilinearity. A Lie algebra is called *commutative* if [X, Y] = 0 for all elements X and Y. The *dimension* of the Lie algebra is the dimension of the vector space. A subspace N of a Lie algebra L is called an *ideal*\* if  $[L, N] \subset N$ ; any ideal is also a *subalgebra*. A *maximal ideal* M which satisfies [L, M] = 0is called the *centre* of L.

A Lie algebra is called a *linear* Lie algebra if its elements are linear transformations of another vector space V (intuitively, if they are 'matrices'). It turns out that every finite-dimensional Lie algebra is isomorphic to a linear Lie algebra. Therefore, there is no loss of generality in picturing the elements of finite-dimensional Lie algebras as matrices.

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The name 'Lie algebra' was chosen because the *generators*, i.e., the infinitesimal elements of every Lie group, form a Lie algebra. Since all important symmetries in nature form Lie groups, Lie algebras appear very frequently in physics. In mathematics, Lie algebras arise frequently because from any associative finite-dimensional algebra (in which the symbol  $\cdot$  stands for its multiplication) a Lie algebra appears when we define the *commutator* by

$$[X,Y] = X \cdot Y - Y \cdot X . \tag{145}$$

(This fact gave the commutator its name.) Lie algebras are non-associative in general; but the above definition of the commutator shows how to build one from an associative algebra.

Since Lie algebras are vector spaces, the elements  $T_i$  of a *basis* of the Lie algebra always obey a relation of the form:

$$[T_i, T_j] = \sum_k c_{ij}^k T_k .$$
 (146)

The numbers  $c_{ij}^k$  are called the *structure constants* of the Lie algebra. They depend on

Challenge 202 ny \* Can you explain the notation [*L*, *N*]? Can you define what a maximal ideal is and prove that there is only one?

the choice of basis. The structure constants determine the Lie algebra completely. For example, the algebra of the Lie group SU(2), with the three generators defined by  $T_a = \sigma^a/2i$ , where the  $\sigma^a$  are the Pauli spin matrices, has the structure constants  $C_{abc} = \varepsilon_{abc}$ .\*

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# CLASSIFICATION OF LIE ALGEBRAS

*Finite-dimensional* Lie algebras are classified as follows. Every finite-dimensional Lie algebra is the (semidirect) sum of a semisimple and a solvable Lie algebra.

A Lie algebra is called *solvable* if, well, if it is not semisimple. Solvable Lie algebras have not yet been classified completely. They are not important in physics.

A *semisimple* Lie algebra is a Lie algebra which has no non-zero solvable ideal. Other equivalent definitions are possible, depending on your taste:

- a semisimple Lie algebra does not contain non-zero Abelian ideals;
- its Killing form is non-singular, i.e., non-degenerate;
- it splits into the direct sum of non-Abelian simple ideals (this decomposition is unique);
- every finite-dimensional linear representation is completely reducible;
- the one-dimensional cohomology of *g* with values in an arbitrary finite-dimensional *g*-module is trivial.

Finite-dimensional semisimple Lie algebras have been completely classified. They decompose uniquely into a direct sum of *simple* Lie algebras. Simple Lie algebras can be complex or real.

The simple finite-dimensional *complex* Lie algebras all belong to four infinite classes and to five exceptional cases. The infinite classes are also called *classical*, and are:  $A_n$  for  $n \ge 1$ , corresponding to the Lie groups SL(n + 1) and their compact 'cousins' SU(n + 1);  $B_n$  for  $n \ge 1$ , corresponding to the Lie groups SO(2n + 1);  $C_n$  for  $n \ge 1$ , corresponding to the Lie groups Sp(2n); and  $D_n$  for  $n \ge 4$ , corresponding to the Lie groups SO(2n). Thus  $A_n$  is the algebra of all skew-Hermitean matrices;  $B_n$  and  $D_n$  are the algebras of the

$$[a,a_j] = \sum \operatorname{ad}(a)_{cj}a_c . \tag{147}$$

The definition implies that  $ad(a_i)_{jk} = c_{ij}^k$ , where  $c_{ij}^k$  are the structure constants of the Lie algebra. For a real Lie algebra, all elements of ad(a) are real for all  $a \in L$ .

Note that for any Lie algebra, a scalar product can be defined by setting

$$X \cdot Y = \operatorname{Tr}(\operatorname{ad} X \cdot \operatorname{ad} Y) . \tag{148}$$

This scalar product is symmetric and bilinear. (Can you show that it is independent of the representation?) The corresponding bilinear form is also called the *Killing form*, after the mathematician Wilhelm Killing (b. 1847 Burbach, d. 1923 Münster), the discoverer of the 'exceptional' Lie groups. The Killing form is invariant under the action of any automorphism of the Lie algebra L. In a given basis, one has

$$X \cdot Y = \operatorname{Tr}((\operatorname{ad} X) \cdot (\operatorname{ad} Y)) = c_{ll}^{i} c_{sl}^{k} x^{l} y^{s} = g_{ls} x^{l} y^{s}$$
(149)

where  $g_{ls} = c_{lk}^i c_{si}^k$  is called the *Cartan metric tensor* of L.

<sup>\*</sup> Like groups, Lie algebras can be represented by matrices, i.e., by linear operators. Representations of Lie algebras are important in physics because many continuous symmetry groups are Lie groups.

The *adjoint representation* of a Lie algebra with basis  $a_1...a_n$  is the set of matrices ad(a) defined for each element *a* by

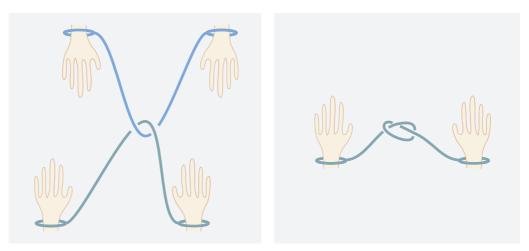


FIGURE 183 Which of the two situations can be untied without cutting?

symmetric matrices; and  $C_n$  is the algebra of the traceless matrices.

The exceptional Lie algebras are  $G_2$ ,  $F_4$ ,  $E_6$ ,  $E_7$ ,  $E_8$ . In all cases, the index gives the number of so-called *roots* of the algebra. The dimensions of these algebras are  $A_n : n(n + 2)$ ;  $B_n$  and  $C_n : n(2n + 1)$ ;  $D_n : n(2n - 1)$ ;  $G_2 : 14$ ;  $F_4 : 32$ ;  $E_6 : 78$ ;  $E_7 : 133$ ;  $E_8 : 248$ .

The simple and finite-dimensional *real* Lie algebras are more numerous; their classification follows from that of the complex Lie algebras. Moreover, corresponding to each complex Lie group, there is always one compact real one. Real Lie algebras are not so important in fundamental physics.

Of the large number of *infinite-dimensional* Lie algebras, only one is important in physics, the *Poincaré algebra*. A few other such algebras only appeared in failed attempts for unification.

# TOPOLOGY - WHAT SHAPES EXIST?

Topology is group theory. The Erlangen program

In a simplified view of topology that is sufficient for physicists, only one type of entity can possess shape: manifolds. *Manifolds* are generalized examples of pullovers: they are locally flat, can have holes and boundaries, and can often be turned inside out.

Challenge 203 s

Ref. 300

Pullovers are subtle entities. For example, can you turn your pullover inside out while your hands are tied together? (A friend may help you.) By the way, the same feat is also possible with your trousers, while your feet are tied together. Certain professors like to demonstrate this during topology lectures – of course with a carefully selected pair of underpants.

Ref. 301 Another good topological puzzle, the handcuff puzzle, is shown in Figure 183. Which of the two situations can be untied without cutting the ropes?

For a mathematician, pullovers and ropes are everyday examples of manifolds, and

the operations that are performed on them are examples of deformations. Let us look at some more precise definitions. In order to define what a manifold is, we first need to define the concept of topological space.

#### TOPOLOGICAL SPACES

En Australie, une mouche qui marche au plafond se trouve dans le même sens qu'une vache chez nous.
 Philippe Geluck, *La marque du chat*.

Ref. 302 The study of shapes requires a good definition of a set made of 'points'. To be able to talk about shape, these sets must be structured in such a way as to admit a useful concept of 'neighbourhood' or 'closeness' between the elements of the set. The search for the most general type of set which allows a useful definition of neighbourhood has led to the concept of topological space. There are two ways to define a topology: one can define the concept of *open set* and then define the concept of *neighbourhood* with their help, or the other way round. We use the second option, which is somewhat more intuitive.

A *topological space* is a finite or infinite set X of elements, called *points*, together with the neighbourhoods for each point. A *neighbourhood* N of a point x is a collection of subsets  $Y_x$  of X with the properties that

- -x is in every  $Y_x$ ;
- if N and M are neighbourhoods of x, so is  $N \cap M$ ;
- anything containing a neighbourhood of x is itself a neighbourhood of x.

The choice of the subsets  $Y_x$  is free. The subsets  $Y_x$  for all points x, chosen in a particular definition, contain a neighbourhood for each of their points; they are called *open sets*. (A neighbourhood and an open set usually differ, but all open sets are also neighbourhoods. Neighbourhoods of x can also be described as subsets of X that contain an open set that contains x.)

One also calls a topological space a 'set with a topology'. In effect, a *topology* specifies the systems of 'neighbourhoods' of every point of the set. 'Topology' is also the name of the branch of mathematics that studies topological spaces.

For example, the real numbers together with all open intervals form the *usual* topology of  $\mathbb{R}$ . Mathematicians have generalized this procedure. If one takes *all* subsets of  $\mathbb{R}$  – or any other basis set – as open sets, one speaks of the *discrete* topology. If one takes *only* the full basis set and the empty set as open sets, one speaks of the *trivial* or *indiscrete* topology.

The concept of topological space allows us to define continuity. A mapping from one topological space X to another topological space Y is *continuous* if the inverse image of every open set in Y is an open set in X. You may verify that this condition is not satisfied by a real function that makes a jump. You may also check that the term 'inverse' is necessary in the definition; otherwise a function with a jump would be continuous, as such a function may still map open sets to open sets.\*

Challenge 205 e

<sup>\*</sup> The Cauchy–Weierstass definition of continuity says that a real function f(x) is continuous at a point a if (1) f is defined on an open interval containing a, (2) f(x) tends to a limit as x tends to a, and (3) the

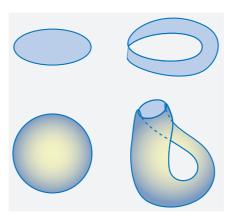


FIGURE 184 Examples of orientable and non-orientable manifolds of two dimensions: a disc, a Möbius strip, a sphere and a Klein bottle.

We thus need the concept of topological space, or of neighbourhood, if we want to express the idea that there are no jumps in nature. We also need the concept of topological space in order to be able to define limits.

Of the many special kinds of topological spaces that have been studied, one type is particularly important. A *Hausdorff space* is a topological space in which for any two points x and y there are disjoint open sets U and V such that x is in U and y is in V. A Hausdorff space is thus a space where, no matter how 'close' two points are, they can always be separated by open sets. This seems like a desirable property; indeed, non-Hausdorff spaces are rather tricky mathematical objects. (At Planck energy, it seems that vacuum appears to behave like a non-Hausdorff space; however, at Planck energy, vacuum is not really a space at all. So non-Hausdorff spaces play no role in physics.) A special case of Hausdorff space is well-known: the manifold.

#### Manifolds

In physics, the most important topological spaces are differential manifolds. Loosely speaking, a *differential manifold* – physicists simply speak of a *manifold* – is a set of points that looks like  $\mathbb{R}^n$  under the microscope – at small distances. For example, a sphere and a torus are both two-dimensional differential manifolds, since they look locally like a plane. Not all differential manifolds are that simple, as the examples of Figure 184 show.

A differential manifold is called *connected* if any two points can be joined by a path lying in the manifold. (The term has a more general meaning in topological spaces. But the notions of connectedness and pathwise connectedness coincide for differential manifolds.) We focus on connected manifolds in the following discussion. A manifold is called *simply connected* if every loop lying in the manifold can be contracted to a point. For example, a sphere is simply connected. A connected manifold which is not simply connected is called *multiply connected*. A torus is multiply connected.

Manifolds can be *non-orientable*, as the well-known Möbius strip illustrates. Non-orientable manifolds have only one surface: they do not admit a distinction between

limit is f(a). In this definition, the continuity of f is defined using the intuitive idea that the real numbers form the basic model of a set that has no gaps. Can you see the connection with the general definition given above?

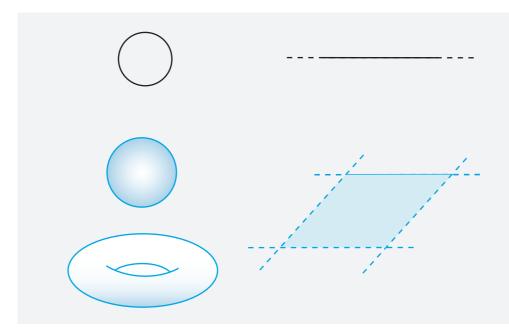


FIGURE 185 Compact (left) and non-compact (right) manifolds of various dimensions.

Challenge 207 e front and back. If you want to have fun, cut a paper Möbius strip into two along a centre line. You can also try this with paper strips with different twist values, and investigate the regularities.

In two dimensions, closed manifolds (or surfaces), i.e., surfaces that are compact and without boundary, are always of one of three types:

- The simplest type are spheres with *n* attached handles; they are called *n*-tori or surfaces
  of genus *n*. They are orientable surfaces with Euler characteristic 2 2n.
- The *projective planes* with *n* handles attached are non-orientable surfaces with Euler characteristic 1 2n.
- The Klein bottles with n attached handles are non-orientable surfaces with Euler characteristic -2n.

Therefore Euler characteristic and orientability describe compact surfaces up to homeomorphism (and if surfaces are smooth, then up to diffeomorphism). Page 367 Homeomorphisms are defined below.

The two-dimensional compact manifolds or surfaces with boundary are found by removing one or more discs from a surface in this list. A compact surface can be embedded in  $\mathbb{R}^3$  if it is orientable or if it has non-empty boundary.

In physics, the most important manifolds are space-time and Lie groups of observables. We study Lie groups below. Strangely enough, the topology of space-time is not known. For example, it is unclear whether or not it is simply connected. Obviously, the reason is that it is difficult to observe what happens at large distances form the Earth. However, a similar difficulty appears near Planck scales.

If a manifold is imagined to consist of rubber, connectedness and similar global properties are not changed when the manifold is deformed. This fact is formalized by saying

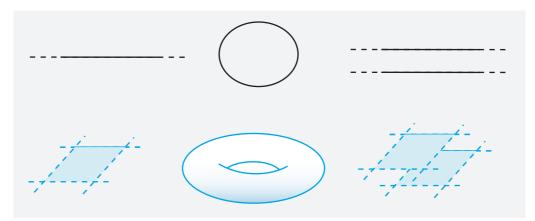
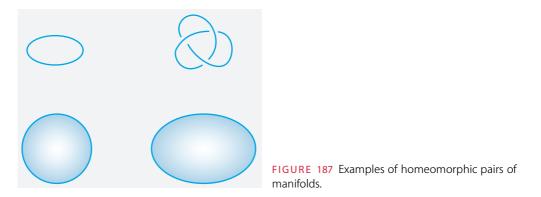


FIGURE 186 Simply connected (left), multiply connected (centre) and disconnected (right) manifolds of one (above) and two (below) dimensions.



that two manifolds are *homeomorphic* (from the Greek words for 'same' and 'shape') if between them there is a continuous, one-to-one and onto mapping with a continuous inverse. The concept of homeomorphism is somewhat more general than that of rubber deformation, as can be seen from Figure 187. If the mapping and the manifolds are differentiable, one says that the two manifolds are *diffeomorphic*.

# Holes, homotopy and homology

Only 'well-behaved' manifolds play a role in physics: namely those which are orientable and connected. In addition, the manifolds associated with observables, are always compact. The main non-trivial characteristic of connected compact orientable manifolds is that they contain 'holes' (see Figure 188). It turns out that a proper description of the holes of manifolds allows us to distinguish between all different, i.e., nonhomeomorphic, types of manifold.

There are three main tools to describe holes of manifolds and the relations among them: homotopy, homology and cohomology. These tools play an important role in the study of gauge groups, because any gauge group defines a manifold.

In other words, through homotopy and homology theory, mathematicians can clas-



FIGURE 188 The first four two-dimensional compact connected orientable manifolds: 0-, 1-, 2- and 3-tori.

*sify* manifolds. Given two manifolds, the properties of the holes in them thus determine whether they can be deformed into each other.

Physicists are now extending these results of standard topology. Deformation is a classical idea which assumes continuous space and time, as well as arbitrarily small action. In nature, however, quantum effects cannot be neglected. It is speculated that quantum effects can transform a physical manifold into one with a *different* topology: for example, a torus into a sphere. Can you find out how this can be achieved?

Challenge 208 d

Topological changes of physical manifolds happen via objects that are generalizations of manifolds. An *orbifold* is a space that is locally modelled by  $\mathbb{R}^n$  modulo a finite group. Examples are the tear-drop or the half-plane. Orbifolds were introduced by Satake Ichiro in 1956; the name was coined by William Thurston. Orbifolds are heavily studied in string theory.

#### **TYPES AND CLASSIFICATION OF GROUPS**

Vol. I, page 272

We introduced mathematical *groups* early on because groups, especially symmetry groups, play an important role in many parts of physics, from the description of solids, molecules, atoms, nuclei, elementary particles and forces up to the study of shapes, cycles and patterns in growth processes.

Group theory is also one of the most important branches of modern mathematics, and is still an active area of research. One of the aims of group theory is the *classification* of all groups. This has been achieved only for a few special types. In general, one distinguishes between finite and infinite groups. Finite groups are better understood.

Every *finite* group is isomorphic to a subgroup of the symmetric group  $S_N$ , for some number N. Examples of finite groups are the crystalline groups, used to classify crystal structures, or the groups used to classify wallpaper patterns in terms of their symmetries. The symmetry groups of Platonic and many other regular solids are also finite groups.

Finite groups are a complex family. Roughly speaking, a general (finite) group can be seen as built from some fundamental bricks, which are groups themselves. These fundamental bricks are called *simple* (finite) groups. One of the high points of twentieth-century mathematics was the classification of the finite simple groups. It was a collaborative effort that took around 30 years, roughly from 1950 to 1980. The complete list of finite simple groups consists of

Ref. 303

1) the *cyclic groups*  $Z_p$  of prime group order;

2) the *alternating groups*  $A_n$  of degree *n* at least five;

3) the *classical linear groups*, PSL(n; q), PSU(n; q), PSp(2n; q) and  $P\Omega^{\varepsilon}(n; q)$ ;

4) the exceptional or twisted groups of Lie type  ${}^{3}D_{4}(q)$ ,  $E_{6}(q)$ ,  ${}^{2}E_{6}(q)$ ,  $E_{7}(q)$ ,  $E_{8}(q)$ ,  $F_{4}(q)$ ,  ${}^{2}F_{4}(2^{n})$ ,  $G_{2}(q)$ ,  ${}^{2}G_{2}(3^{n})$  and  ${}^{2}B_{2}(2^{n})$ ;

5) the 26 sporadic groups, namely  $M_{11}$ ,  $M_{12}$ ,  $M_{22}$ ,  $M_{23}$ ,  $M_{24}$  (the Mathieu groups),  $J_1$ ,

 $J_2$ ,  $J_3$ ,  $J_4$  (the Janko groups),  $Co_1$ ,  $Co_2$ ,  $Co_3$  (the Conway groups), HS, Mc, Suz (the  $Co_1$  'babies'),  $Fi_{22}$ ,  $Fi_{23}$ ,  $Fi'_{24}$  (the Fischer groups),  $F_1 = M$  (the Monster),  $F_2$ ,  $F_3$ ,  $F_5$ , He (=  $F_7$ ) (the Monster 'babies'), Ru, Ly, and ON.

The classification was finished in the 1980s after over 10 000 pages of publications. The proof is so vast that a special series of books has been started to summarize and explain it. The first three families are infinite. The last family, that of the sporadic groups, is the most peculiar; it consists of those finite simple groups which do not fit into the other families. Some of these sporadic groups might have a role in particle physics: possibly even the largest of them all, the so-called *Monster* group. This is still a topic of research. (The Monster group has about  $8.1 \cdot 10^{53}$  elements; more precisely, its order is  $808\,017\,424\,794\,512\,875\,886\,459\,904\,961\,710\,757\,005\,754\,368\,000\,000\,000$  or  $2^{46} \cdot 3^{20} \cdot 5^9 \cdot 7^6 \cdot 11^2 \cdot 13^3 \cdot 17 \cdot 19 \cdot 23 \cdot 29 \cdot 31 \cdot 41 \cdot 47 \cdot 59 \cdot 71.)$ 

Of the *infinite* groups, only those with some finiteness condition have been studied. It is only such groups that are of interest in the description of nature. Infinite groups are divided into *discrete* groups and *continuous* groups. Discrete groups are an active area of mathematical research, having connections with number theory and topology. Continuous groups are divided into *finitely generated* and *infinitely generated* groups. Finitely generated groups can be finite-dimensional or infinite-dimensional.

The most important class of finitely generated continuous groups are the Lie groups.

# LIE GROUPS

In nature, the Lagrangians of the fundamental forces are invariant under gauge transformations and under continuous space-time transformations. These symmetry groups are examples of Lie groups, which are a special type of infinite continuous group. They are named after the great mathematician Sophus Lie (b. 1842 Nordfjordeid, d. 1899 Kristiania). His name is pronounced like 'Lee'.

A (real) *Lie group* is an infinite symmetry group, i.e., a group with infinitely many elements, which is also an analytic manifold. Roughly speaking, this means that the elements of the group can be seen as points on a smooth (hyper-) surface whose shape can be described by an analytic function, i.e., by a function so smooth that it can be expressed as a power series in the neighbourhood of every point where it is defined. The points of the Lie group can be multiplied according to the group multiplication. Furthermore, the coordinates of the product have to be analytic functions of the coordinates of the factors, and the coordinates of the inverse of an element have to be analytic functions of the coordinates of the element. In fact, this definition is unnecessarily strict: it can be proved that a Lie group is just a topological group whose underlying space is a finite-dimensional, locally Euclidean manifold.

A *complex Lie group* is a group whose manifold is complex and whose group operations are holomorphic (instead of analytical) functions in the coordinates.

In short, a Lie group is a well-behaved manifold in which points can be multiplied (and technicalities). For example, the circle  $T = \{z \in \mathbb{C} : |z| = 1\}$ , with the usual complex multiplication, is a real Lie group. It is Abelian. This group is also called S<sup>1</sup>, as it is the one-dimensional sphere, or U(1), which means 'unitary group of one dimension'. The other one-dimensional Lie groups are the multiplicative group of non-zero real numbers and its subgroup, the multiplicative group of positive real numbers.

So far, in physics, only *linear* Lie groups have played a role – that is, Lie groups which act as linear transformations on some vector space. (The cover of  $SL(2,\mathbb{R})$  or the complex compact torus are examples of non-linear Lie groups.) The important linear Lie groups for physics are the Lie subgroups of the general linear group GL(N,K), where *K* is a number field. This is defined as the set of all non-singular, i.e., invertible, N×N real, complex or quaternionic matrices. All the Lie groups discussed below are of this type.

Every *complex* invertible matrix *A* can be written in a unique way in terms of a unitary matrix *U* and a Hermitean matrix *H*:

$$A = Ue^H . (150)$$

Challenge 209 s

(*H* is given by  $H = \frac{1}{2} \ln A^{\dagger} A$ , and *U* is given by  $U = Ae^{-H}$ .) The simple Lie groups U(1) and SO(2,  $\mathbb{R}$ ) and the Lie groups based on the real and complex numbers are Abelian (see Table 37); all others are non-Abelian.

Lie groups are manifolds. Therefore, in a Lie group one can define the distance between two points, the tangent plane (or tangent space) at a point, and the notions of integration and differentiations. Because Lie groups are manifolds, Lie groups have the same kind of structure as the objects of Figures 184, 185 and 186. Lie groups can have any number of dimensions. Like for any manifold, their global structure contains important information; let us explore it.

#### Connectedness

It is not hard to see that the Lie groups SU(N) are simply connected for all N = 2, 3...; they have the topology of a 2N-dimensional sphere. The Lie group U(1), having the topology of the 1-dimensional sphere, or circle, is multiply connected.

The Lie groups SO(N) are *not* simply connected for any N = 2, 3... In general, SO(N,K) is connected, and GL(N, $\mathbb{C}$ ) is connected. All the Lie groups SL(N,K) are connected; and SL(N, $\mathbb{C}$ ) is simply connected. The Lie groups Sp(N,K) are connected; Sp(2N, $\mathbb{C}$ ) is simply connected. Generally, all semi-simple Lie groups are connected.

The Lie groups O(N,K), SO(N,M,K) and  $GL(N,\mathbb{R})$  are not connected; they contain two connected components.

Note that the Lorentz group is not connected: it consists of four separate pieces. Like the Poincaré group, it is not compact, and neither is any of its four pieces. Broadly speaking, the non-compactness of the group of space-time symmetries is a consequence of the non-compactness of space-time.

# Compactness

A Lie group is *compact* if it is closed and bounded when seen as a manifold. For a given parametrization of the group elements, the Lie group is compact if all parameter ranges are closed and finite intervals. Otherwise, the group is called *non-compact*. Both compact and non-compact groups play a role in physics. The distinction between the two cases is important, because representations of compact groups can be constructed in the same simple way as for finite groups, whereas for non-compact groups other methods have to be used. As a result, physical observables, which always belong to a representation of a symmetry group, have different properties in the two cases: if the symmetry group is

compact, observables have *discrete* spectra; otherwise they do not.

All groups of internal gauge transformations, such as U(1) and SU(*n*), form compact groups. In fact, field theory *requires* compact Lie groups for gauge transformations. The only compact Lie groups are the torus groups  $T^n$ , O(*n*), U(*n*), SO(*n*) and SU(*n*), their double cover Spin(*n*) and the Sp(*n*). In contrast, SL(*n*, $\mathbb{R}$ ), GL(*n*, $\mathbb{C}$ ) and all others are not compact.

Besides being manifolds, Lie groups are obviously also groups. It turns out that most of their group properties are revealed by the behaviour of the elements which are very close (as points on the manifold) to the identity.

Every element of a compact and connected Lie group has the form  $\exp(A)$  for some A. The elements A arising in this way form an algebra, called the *corresponding Lie algebra*. For any linear Lie group, every element of the connected subgroup can be expressed as a finite product of exponentials of elements of the corresponding Lie algebra. Mathematically, the vector space defined by the Lie algebra is tangent to the manifold defined by the Lie group, at the location of the unit element. In short, Lie algebras express the local properties of Lie groups near the identity. That is the reason for their importance in physics.

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Lie group	Descrip- tion	PROPERTIES <sup>a</sup>	LIE AL- GEBRA	Description of Lie algebra	Dimen- sion
1. Real gro	oups		real		
$\mathbb{R}^{n}$	Euclidean space with addition	Abelian, simply connected, not compact; $\pi_0 = \pi_1 = 0$	$\mathbb{R}^{n}$	Abelian, thus Lie bracket is zero; not simple	п
$\mathbb{R}^{\times}$	non-zero real numbers with multiplica- tion	Abelian, not connected, not compact; $\pi_0 = \mathbb{Z}_2$ , no $\pi_1$	R	Abelian, thus Lie bracket is zero	1
$\mathbb{R}^{>0}$	positive real numbers with multiplica- tion	Abelian, simply connected, not compact; $\pi_0 = \pi_1 = 0$	R	Abelian, thus Lie bracket is zero	1
= U(1) = T = SO(2)	complex numbers of absolute value 1, with multi- plication	Abelian, connected, not simply connected, compact; $\pi_0 = 0$ , $\pi_1 = \mathbb{Z}$	R	Abelian, thus Lie bracket is zero	1
$\mathbb{H}^{\times}$	non-zero quaternions with multi- plication	simply connected, not compact; $\pi_0 = \pi_1 = 0$	H	quaternions, with Lie bracket the commutator	4

 TABLE 37 Properties of the most important real and complex Lie groups.

Lie group	Descrip- tion	Properties <sup>a</sup>	Lie al- gebra	Description of Lie algebra	Dimen- sion
S <sup>3</sup>	quaternions of absolute value 1, with multiplica- tion, also known as Sp(1); topologically a 3-sphere	simply connected, compact; isomorphic to SU(2), Spin(3) and to double cover of SO(3); $\pi_0 = \pi_1 = 0$	Im(ℍ)	quaternions with zero real part, with Lie bracket the commutator; simple and semi-simple; isomorphic to real 3-vectors, with Lie bracket the cross product; also isomorphic to su(2) and to so(3)	3
GL( <i>n</i> , ℝ)	general linear group: invertible <i>n</i> -by- <i>n</i> real matrices	not connected, not compact; $\pi_0 = \mathbb{Z}_2$ , no $\pi_1$	M( <i>n</i> , ℝ)	<i>n</i> -by- <i>n</i> matrices, with Lie bracket the commutator	$n^2$
$\mathrm{GL}^+(n,\mathbb{R})$	<i>n</i> -by- <i>n</i> real matrices with positive determinant	simply connected, not compact; $\pi_0 = 0$ , for $n = 2$ : $\pi_1 = \mathbb{Z}$ , for $n \ge 2$ : $\pi_1 = \mathbb{Z}_2$ ; GL <sup>+</sup> (1, $\mathbb{R}$ ) isomorphic to $\mathbb{R}^{>0}$	M( <i>n</i> , ℝ)	<i>n</i> -by- <i>n</i> matrices, with Lie bracket the commutator	n <sup>2</sup>
SL( <i>n</i> , ℝ)		simply connected, not compact if $n > 1$ ; $\pi_0 = 0$ , for $n = 2$ : $\pi_1 = \mathbb{Z}$ , for $n \ge 2$ : $\pi_1 = \mathbb{Z}_2$ ; SL(1, $\mathbb{R}$ ) is a single point, SL(2, $\mathbb{R}$ ) is isomorphic to SU(1, 1) and Sp(2, $\mathbb{R}$ )	$sl(n, \mathbb{R})$ = $A_{n-1}$	<i>n</i> -by- <i>n</i> matrices with trace 0, with Lie bracket the commutator	<i>n</i> <sup>2</sup> – 1
$O(n, \mathbb{R})$ = $O(n)$	orthogonal group: real orthogonal matrices; symmetry of hypersphere	not connected, compact; $\pi_0 = \mathbb{Z}_2$ , no $\pi_1$	so(n, ℝ)	skew-symmetric <i>n</i> -by- <i>n</i> real matrices, with Lie bracket the commutator; so(3, $\mathbb{R}$ ) is isomorphic to su(2) and to $\mathbb{R}^3$ with the cross product	<i>n</i> ( <i>n</i> – 1)/2

 TABLE 37 (Continued) Properties of the most important real and complex Lie groups.

Lie group	Descrip- tion	Properties <sup>a</sup>	Lie al- gebra	Description of Lie algebra	Dimen- sion
$\overline{SO(n, \mathbb{R})} = SO(n)$		connected, compact; for $n \ge 2$ not simply connected; $\pi_0 = 0$ , for $n = 2$ : $\pi_1 = \mathbb{Z}$ , for $n \ge 2$ : $\pi_1 = \mathbb{Z}_2$	$so(n, \mathbb{R}) = B_{\frac{n-1}{2}} \text{ or } D_{\frac{n}{2}}$	skew-symmetric <i>n</i> -by- <i>n</i> real matrices, with Lie bracket the commutator; for $n = 3$ and $n \ge 5$ simple and semisimple; SO(4) is semisimple but not simple	n(n – 1)/2
Spin( <i>n</i> )	-	simply connected for $n \ge 3$ , compact; for $n = 3$ and $n \ge 5$ simple and semisimple; for $n > 1$ : $\pi_0 = 0$ , for $n > 2$ : $\pi_1 = 0$	so( <i>n</i> , ℝ)	skew-symmetric <i>n</i> -by- <i>n</i> real matrices, with Lie bracket the commutator	<i>n</i> ( <i>n</i> – 1)/2
Sp(2 <i>n</i> , ℝ)	symplectic group: real symplectic matrices	not compact; $\pi_0 = 0, \pi_1 = \mathbb{Z}$	$sp(2n, \mathbb{R})$ = $C_n$	real matrices A that satisfy $JA + A^T J = 0$ where J is the standard skew-symmetric matrix; <sup>b</sup> simple and semisimple	<i>n</i> (2 <i>n</i> + 1)
$\operatorname{Sp}(n)$ for $n \ge 3$	compact symplectic group: quaternionic $n \times n$ unitary matrices	compact, simply connected; $\pi_0 = \pi_1 = 0$	sp( <i>n</i> )	<i>n</i> -by- <i>n</i> quaternionic matrices <i>A</i> satisfying $A = -A^*$ , with Lie bracket the commutator; simple and semisimple	<i>n</i> (2 <i>n</i> + 1)
U( <i>n</i> )	unitary group: complex $n \times n$ unitary matrices	not simply connected, compact; it is <i>not</i> a complex Lie group/algebra; $\pi_0 = 0, \pi_1 = \mathbb{Z}$ ; isomorphic to $S^1$ for n = 1	u( <i>n</i> )	<i>n</i> -by- <i>n</i> complex matrices <i>A</i> satisfying $A = -A^*$ , with Lie bracket the commutator	n <sup>2</sup>
SU( <i>n</i> )	special unitary group: complex $n \times n$ unitary matrices with determinant 1	simply connected, compact; it is <i>not</i> a complex Lie group/algebra; $\pi_0 = \pi_1 = 0$	su( <i>n</i> )	<i>n</i> -by- <i>n</i> complex matrices <i>A</i> with trace 0 satisfying $A = -A^*$ , with Lie bracket the commutator; for $n \ge 2$ simple and semisimple	<i>n</i> <sup>2</sup> – 1

 TABLE 37 (Continued) Properties of the most important real and complex Lie groups.

2. Complex groups<sup>c</sup>

complex

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Lie group	Descrip- tion	Properties <sup>a</sup>	Lie al- gebra	Description of Lie algebra	Dimen- sion
$\overline{\mathbb{C}^n}$	group operation is addition	Abelian, simply connected, not compact; $\pi_0 = \pi_1 = 0$	$\mathbb{C}^n$	Abelian, thus Lie bracket is zero	п
$\mathbb{C}^{\times}$	non-zero complex numbers with multiplica- tion	Abelian, not simply connected, not compact; $\pi_0 = 0$ , $\pi_1 = \mathbb{Z}$	C	Abelian, thus Lie bracket is zero	1
GL( <i>n</i> , ℂ)	general linear group: invertible <i>n</i> -by- <i>n</i> complex matrices	simply connected, not compact; $\pi_0 = 0$ , $\pi_1 = \mathbb{Z}$ ; for $n = 1$ isomorphic to $\mathbb{C}^{\times}$	M( <i>n</i> , ℂ)	<i>n</i> -by- <i>n</i> matrices, with Lie bracket the commutator	n <sup>2</sup>
SL( <i>n</i> , ℂ)	special linear group: complex matrices with determinant 1		sl( <i>n</i> , ℂ)	<i>n</i> -by- <i>n</i> matrices with trace 0, with Lie bracket the commutator; simple, semisimple; $sl(2, \mathbb{C})$ is isomorphic to $su(2, \mathbb{C}) \otimes \mathbb{C}$	<i>n</i> <sup>2</sup> – 1
PSL(2, ℂ)	projective special linear group; isomorphic to the Möbius group, to the restricted Lorentz group $SO^+(3, 1, \mathbb{R})$ and to $SO(3, \mathbb{C})$	not compact; $\pi_0 = 0, \pi_1 = \mathbb{Z}_2$	sl(2, ℂ)	2-by-2 matrices with trace 0, with Lie bracket the commutator; $sl(2, \mathbb{C})$ is isomorphic to $su(2, \mathbb{C}) \otimes \mathbb{C}$	3
O( <i>n</i> , ℂ)	orthogonal group: complex orthogonal matrices	not connected; for $n \ge 2$ not compact; $\pi_0 = \mathbb{Z}_2$ , no $\pi_1$	so( <i>n</i> , ℂ)	skew-symmetric <i>n</i> -by- <i>n</i> complex matrices, with Lie bracket the commutator	<i>n</i> ( <i>n</i> – 1)/2

 TABLE 37 (Continued) Properties of the most important real and complex Lie groups.

Lie group	Descrip- tion	Properties <sup>a</sup>	Lie al- gebra	Description of Lie algebra	Dimen- sion
SO( <i>n</i> , ℂ)		for $n \ge 2$ not compact; not simply connected; $\pi_0 = 0$ , for $n = 2$ : $\pi_1 = \mathbb{Z}$ , for $n \ge 2$ : $\pi_1 = \mathbb{Z}_2$ ; non-Abelian for $n > 2$ , SO(2, $\mathbb{C}$ ) is Abelian and isomorphic to $\mathbb{C}^{\times}$	so( <i>n</i> , ℂ)	skew-symmetric <i>n</i> -by- <i>n</i> complex matrices, with Lie bracket the commutator; for $n = 3$ and $n \ge 5$ simple and semisimple	<i>n</i> ( <i>n</i> – 1)/2
Sp(2 <i>n</i> , ℂ)	symplectic group: complex symplectic matrices	not compact; $\pi_0 = \pi_1 = 0$	sp(2 <i>n</i> , ℂ)	complex matrices that satisfy $JA + A^T J = 0$ where <i>J</i> is the standard skew-symmetric matrix; <sup>b</sup> simple and semi-simple	<i>n</i> (2 <i>n</i> + 1)

TABLE 37 (Continued) Properties of the most important real and complex Lie groups.

*a*. The group of components  $\pi_0$  of a Lie group is given; the order of  $\pi_0$  is the number of components of the Lie group. If the group is trivial (0), the Lie group is connected. The *fundamental group*  $\pi_1$  of a connected Lie group is given. If the group  $\pi_1$  is trivial (0), the Lie group is simply connected. This table is based on that in the Wikipedia, at en.wikipedia.org/wiki/Table\_of\_Lie\_groups. *b*. The standard skew-symmetric matrix *J* of rank 2*n* is  $J_{kl} = \delta_{k,n+l} - \delta_{k+n,l}$ .

*c*. Complex Lie groups and Lie algebras can be viewed as real Lie groups and real Lie algebras of twice the dimension.

## MATHEMATICAL CURIOSITIES AND FUN CHALLENGES

Challenge 210 ny A

A theorem of topology says: you cannot comb a hairy football. Can you prove it?

Topology is fun. If you want to laugh for half an hour, fix a modified pencil, as shown in Figure 189, to a button hole and let people figure out how to get it off again.

\* \*

There are at least six ways to earn a million dollars with mathematical research. The Clay Mathematics Institute at www.claymath.org offered such a prize for major advances in seven topics:

- proving the Birch and Swinnerton-Dyer conjecture about algebraic equations;
- proving the Poincaré conjecture about topological manifolds;
- solving the Navier–Stokes equations for fluids;

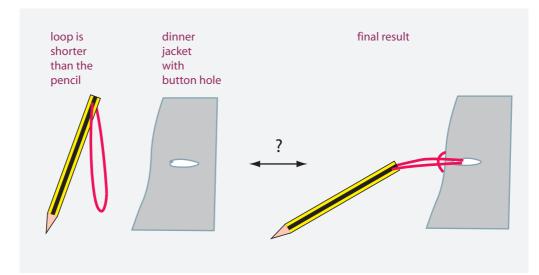


FIGURE 189 A well-known magic dexterity trick: make your friend go mad by adding a pencil to his dinner jacket.

- finding criteria distinguishing P and NP numerical problems;
- proving the Riemann hypothesis stating that the non-trivial zeros of the zeta function lie on a line;
- proving the Hodge conjectures;
- proving the connection between Yang–Mills theories and a mass gap in quantum field theory.

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The Poincaré conjecture was solved in 2002 by Grigori Perelman; on each of the other six topics, substantial progress can buy you a house.

# CHALLENGE HINTS AND SOLUTIONS

**Challenge 1**, page 10: Do not hesitate to be demanding and strict. The next edition of the text will benefit from it.

**Challenge 2**, page 18: A *virus* is an example. It has no own metabolism. By the way, the ability of some viruses to form crystals is *not* a proof that they are not living beings, in contrast to what is often said. Apart from viruses, also *prions*, *viroids* and *virusoids* are examples of non-living systems that can reproduce. Another, quite different border example between life and non-living matter is provided by the *tardigrades*. These little animals, about 1 mm in size, can loose all their water, remain in this dry – or ''dead'' – state for years, and then start living again when a drop of water is added to them.

Challenge 3, page 19: The navigation systems used by flies are an example.

**Challenge 6**, page 23: The thermal energy kT is about 4 zJ and a typical relaxation time is 0.1 ps.

Challenge 10, page 31: The argument is correct.

**Challenge 8**, page 31: This is not possible at present. If you know a way, publish it. It would help a sad single mother who has to live without financial help from the father, despite a lawsuit, as it was yet impossible to decide which of the two candidates is the right one.

**Challenge 9**, page 31: Also identical twins count as different persons and have different fates. Imprinting in the womb is different, so that their temperament will be different. The birth experience will be different; this is the most intense experience of every human, strongly determining his fears and thus his character. A person with an old father is also quite different from that with a young father. If the womb is not that of his biological mother, a further distinction of the earliest and most intensive experiences is given.

Challenge 11, page 31: Be sure to publish your results.

Challenge 12, page 32: Yes, but only very young ones. Why?

**Challenge 13**, page 32: The reason of animal symmetry is simple: without symmetry, they would not be able to move in a *straight* line.

**Challenge 14**, page 32: Life's chemicals are synthesized inside the body; the asymmetry has been inherited along the generations. The common asymmetry thus shows that all life has a common origin.

**Challenge 15**, page 32: Well, men are more similar to chimpanzees than to women. More seriously, the above data, even though often quoted, are wrong. Newer measurements by Roy Britten in 2002 have shown that the difference in genome between humans and chimpanzees is about 5% (See R. J. BRITTEN, *Divergence between samples of chimpanzee and human DNA sequences is 5%, counting indels*, Proceedings of the National Academy of Sciences **99**, pp. 13633–13635, 15th of October, 2002.) In addition, though the difference between man and woman is smaller than one whole chromosome, the large size of the X chromosome, compared with the small size of the Y chromosome, implies that men have about 3% less genetic material than women. However, all

men have an X chromosome as well. That explains that still other measurements suggest that all humans share a pool of at least 99.9 % of common genes.

**Challenge 18**, page 35: Chemical processes, including diffusion and reaction rates, are strongly temperature dependent. They affect the speed of motion of the individual and thus its chance of survival. Keeping temperature in the correct range is thus important for evolved life forms.

**Challenge 19**, page 35: The first steps are not known at all. Subsequent processes that added the complexity of cells are better understood.

**Challenge 20**, page 35: Since all the atoms we are made of originate from outer space, the answer is yes. But if one means that biological cells came to Earth from space, the answer is no, as most cells do not like vacuum. The same is true for DNA.

In fact, life and reproduction are properties of complex systems. In other words, asking whether life comes from outer space is like asking: 'Could car insurance have originated in outer space?'

Challenge 22, page 41: Haven't you tried yet? Physics is an experimental science.

**Challenge 30**, page 49: Exponential decays occur when the probability of decay is constant over time. For humans, this is not the case. Why not?

**Challenge 31**, page 52: There are no non-physical processes: anything that can be observed is a physical process. Consciousness is due to processes in the brain, thus inside matter; thus it is a quantum process. At body temperature, coherence has lifetimes much smaller than the typical thought process.

**Challenge 32**, page 53: Radioactive dating methods can be said to be based on the nuclear interactions, even though the detection is again electromagnetic.

**Challenge 33**, page 54: All detectors of light can be called relativistic, as light moves with maximal speed. Touch sensors are not relativistic following the usual sense of the word, as the speeds involved are too small. The energies are small compared to the rest energies; this is the case even if the signal energies are attributed to electrons only.

**Challenge 34**, page 54: The noise is due to the photoacoustic effect; the periodic light periodically heats the air in the jam glass at the blackened surface and thus produces sound. See M. EULER, *Kann man Licht hören?*, Physik in unserer Zeit 32, pp. 180–182, 2001.

**Challenge 35**, page 57: It implies that neither resurrection nor reincarnation nor eternal life are possible.

**Challenge 38**, page 66: The ethanol disrupts the hydrogen bonds between the water molecules so that, on average, they can get closer together. A video of the experiment is found at www. youtube.com/watch?v=LUW7a7H-KuY.

**Challenge 41**, page 67: You get an intense yellow colour due to the formation of lead iodide  $(PbI_2)$ .

**Challenge 43**, page 74: The usual way to pack oranges on a table is the densest way to pack spheres.

**Challenge 44**, page 75: Just use a paper drawing. Draw a polygon and draw it again at latter times, taking into account how the sides grow over time. You will see by yourself how the faster growing sides disappear over time.

**Challenge 46**, page 85: With a combination of the methods of Table 7, this is indeed possible. In fact, using cosmic rays to search for unknown chambers in the pyramids has been already done in the 1960s. The result was that no additional chambers exist.

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**Challenge 48**, page 89: For example, a heavy mountain will push down the Earth's crust into the mantle, makes it melt on the bottom side, and thus lowers the position of the top.

**Challenge 49**, page 89: These developments are just starting; the results are still far from the original one is trying to copy, as they have to fulfil a second condition, in addition to being a 'copy' of original feathers or of latex: the copy has to be cheaper than the original. That is often a much tougher request than the first.

Challenge 50, page 89: About 0.2 m.

**Challenge 52**, page 90: Since the height of the potential is always finite, walls can always be overcome by tunnelling.

**Challenge 53**, page 91: The lid of a box can never be at rest, as is required for a tight closure, but is always in motion, due to the quantum of action.

**Challenge 55**, page 91: The unit of thermal conductance is  $T\pi^2 k^2/3\hbar$ , where *T* is temperature and *k* is the Boltzmann constant.

**Challenge 56**, page 92: Extremely slender structures are not possible for two reasons: First, because structures built of homogeneous materials do not to achieve such ratios; secondly, the bending behaviour of plants is usually not acceptable in human-built structures.

**Challenge 57**, page 94: The concentrations and can be measured from polar ice caps, by measuring how the isotope concentration changes over depth. Both in evaporation and in condensation of water, the isotope ratio depends on the temperature. The measurements in Antarctica and in Greenland coincide, which is a good sign of their trustworthiness.

Challenge 58, page 95: In the summer, tarmac is soft.

**Challenge 61**, page 114: The one somebody else has thrown away. Energy costs about 10 cents/kWh. For new lamps, the fluorescent lamp is the best for the environment, even though it is the least friendly to the eye and the brain, due to its flickering.

**Challenge 62**, page 119: This old dream depends on the precise conditions. How flexible does the display have to be? What lifetime should it have? The newspaper like display is many years away and maybe not even possible.

**Challenge 63**, page 119: There is only speculation on the answer; the tendency of most researchers is to say no.

**Challenge 64**, page 119: The challenge here is to find a cheap way to deflect laser beams in a controlled way. Cheap lasers are already available.

**Challenge 65**, page 119: No, as it is impossible because of momentum conservation and because of the no-cloning theorem.

**Challenge 66**, page 120: There are companies trying to sell systems based on quantum cryptology; but despite the technical interest, the commercial success is questionable.

**Challenge 67**, page 120: I predicted since the year 2000 that mass-produced goods using this technology (at least 1 million pieces sold) will not be available before 2025.

Challenge 68, page 120: Maybe, but for extremely high prices.

**Challenge 69**, page 121: The set-up is affordable: it uses a laser at  $3.39 \,\mu\text{m}$ , a detector and some optics on a tripod. Sensitivity to alcohol absorption is excellent. Only future will tell.

Challenge 71, page 126: For example, you could change gravity between two mirrors.

**Challenge 72**, page 126: As usual in such statements, either group or phase velocity is cited, but not the corresponding energy velocity, which is always below *c*.

**Challenge 74**, page 129: Echoes do not work once the speed of sound is reached and do not work well when it is approached. Both the speed of light and that of sound have a finite value. Moving with a mirror still gives a mirror image. This means that the speed of light cannot be reached. If it cannot be reached, it must be the same for all observers.

**Challenge 75**, page 130: Mirrors do not usually work for matter; in addition, if they did, matter, because of its rest energy, would require much higher acceleration values.

**Challenge 78**, page 132: The classical radius of the electron, which is the size at which the field energy would make up the full electron mass, is about 137 times smaller, thus much smaller, than the Compton wavelength of the electron.

**Challenge 79**, page 134: The overhang can have any value whatsoever. There is no limit. Taking the indeterminacy relation into account introduces a limit as the last brick or card must not allow the centre of gravity, through its indeterminacy, to be over the edge of the table.

**Challenge 80**, page 134: A larger charge would lead to a field that spontaneously generates electron positron pairs, the electron would fall into the nucleus and reduce its charge by one unit.

**Challenge 82**, page 134: The Hall effect results from the deviation of electrons in a metal due to an applied magnetic field. Therefore it depends on their speed. One gets values around 1 mm. Inside atoms, one can use Bohr's atomic model as approximation.

**Challenge 83**, page 134: The steps are due to the particle nature of electricity and all other moving entities.

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**Challenge 84**, page 135: If we could apply the Banach–Tarski paradox to vacuum, it seems that we could split, without any problem, one ball of vacuum into *two* balls of vacuum, each with the same volume as the original. In other words, one ball with vacuum energy E could not be distinguished from two balls of vacuum energy 2E.

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We used the Banach–Tarski paradox in this way to show that chocolate (or any other matter) possesses an intrinsic length. But it is *not* clear that we can now deduce that the vacuum has an intrinsic length. Indeed, the paradox cannot be applied to vacuum for *two* reasons. First, there indeed is a maximum energy and minimum length in nature. Secondly, there is no place in nature without vacuum energy; so there is no place were we could put the second ball. We thus do not know why the Banach–Tarski paradox for vacuum cannot be applied, and thus cannot use it to deduce the existence of a minimum length in vacuum.

It is better to argue in the following way for a minimum length in vacuum. If there were no intrinsic length cut-off, the vacuum energy would be infinite. Experiments however, show that it is finite.

**Challenge 85**, page 135: Mud is a suspension of sand; sand is not transparent, even if made of clear quartz, because of the scattering of light at the irregular surface of its grains. A suspension cannot be transparent if the index of refraction of the liquid and the suspended particles is different. It is never transparent if the particles, as in most sand types, are themselves not transparent.

**Challenge 86**, page 135: The first answer is probably no, as composed systems cannot be smaller than their own compton wavelength; only elementary systems can. However, the universe is not a system, as it has no environment. As such, its length is not a precisely defined concept, as an environment is needed to measure and to define it. (In addition, gravity must be taken into account in those domains.) Thus the answer is: in those domains, the question makes no sense.

Challenge 87, page 135: Methods to move on perfect ice from mechanics:

- if the ice is perfectly flat, rest is possible only in one point otherwise you oscillate around that point, as shown in challenge 26;
- do nothing, just wait that the higher centrifugal acceleration at body height pulls you away;
- to rotate yourself, just rotate your arm above your head;
- throw a shoe or any other object away;
- breathe in vertically, breathing out (or talking) horizontally (or vice versa);
- wait to be moved by the centrifugal acceleration due to the rotation of the Earth (and its oblateness);

- jump vertically repeatedly: the Coriolis acceleration will lead to horizontal motion;
- wait to be moved by the Sun or the Moon, like the tides are;
- 'swim' in the air using hands and feet;
- wait to be hit by a bird, a flying wasp, inclined rain, wind, lava, earthquake, plate tectonics, or any other macroscopic object (all objects pushing count only as one solution);
- wait to be moved by the change in gravity due to convection in Earth's mantle;
- wait to be moved by the gravitation of some comet passing by;
- counts only for kids: spit, sneeze, cough, fart, pee; or move your ears and use them as wings.

Note that gluing your tongue is not possible on perfect ice.

**Challenge 88**, page 136: Methods to move on perfect ice using thermodynamics and electrodynamics:

- use the radio/TV stations nearby to push you around;
- use your portable phone and a mirror;
- switch on a pocket lamp, letting the light push you;
- wait to be pushed around by Brownian motion in air;
- heat up one side of your body: black body radiation will push you;
- heat up one side of your body, e.g. by muscle work: the changing airflow or the evaporation will push you;
- wait for one part of the body to be cooler than the other and for the corresponding black body radiation effects;
- wait for the magnetic field of the Earth to pull on some ferromagnetic or paramagnetic metal piece in your clothing or in your body;
- wait to be pushed by the light pressure, i.e. by the photons, from the Sun or from the stars, maybe using a pocket mirror to increase the efficiency;
- rub some polymer object to charge it electrically and then move it in circles, thus creating a
  magnetic field that interacts with the one of the Earth.

Note that perfect frictionless surfaces do not melt.

Challenge 89, page 136: Methods to move on perfect ice using general relativity:

- move an arm to emit gravitational radiation;
- deviate the cosmic background radiation with a pocket mirror;
- wait to be pushed by gravitational radiation from star collapses;
- wait for the universe to contract.

**Challenge 90**, page 136: Methods to move on perfect ice using quantum effects:

- wait for your wave function to spread out and collapse at the end of the ice surface;
- wait for the pieces of metal in the clothing to attract to the metal in the surrounding through the Casimir effect;
- wait to be pushed around by radioactive decays in your body.

**Challenge 91**, page 136: Methods to move on perfect ice using materials science, geophysics and astrophysics:

- be pushed by the radio waves emitted by thunderstorms and absorbed in painful human joints;
- wait to be pushed around by cosmic rays;
- wait to be pushed around by the solar wind;
- wait to be pushed around by solar neutrinos;

- wait to be pushed by the transformation of the Sun into a red giant;
- wait to be hit by a meteorite.

**Challenge 92**, page 136: A method to move on perfect ice using self-organization, chaos theory, and biophysics:

 wait that the currents in the brain interact with the magnetic field of the Earth by controlling your thoughts.

Challenge 93, page 136: Methods to move on perfect ice using quantum gravity:

- accelerate your pocket mirror with your hand;
- deviate the Unruh radiation of the Earth with a pocket mirror;
- wait for proton decay to push you through the recoil.

**Challenge 95**, page 143: This is a trick question: if you can say why, you can directly move to the last volume of this adventure and check your answer. The gravitational potential changes the phase of a wave function, like any other potential does; but the reason *why* this is the case will only become clear in the last volume of this series.

Challenge 100, page 145: No. Bound states of massless particles are always unstable.

**Challenge 101**, page 147: This is easy only if the black hole size is inserted into the entropy bound by Bekenstein. A simple deduction of the black hole entropy that includes the factor 1/4 is not yet at hand; more on this in the last volume.

**Challenge 102**, page 147: An entropy limit implies an information limit; only a given information can be present in a given region of nature. This results in a memory limit.

**Challenge 103**, page 147: In natural units, the exact expression for entropy is S = 0.25A. If each Planck area carried one bit (degree of freedom), the entropy would be  $S = \ln W = \ln(2^A) = A \ln 2 = 0.693A$ . This close to the exact value.

**Challenge 107**, page 153: The universe has about  $10^{22}$  stars; the Sun has a luminosity of about  $10^{26}$  W; the total luminosity of the visible matter in the universe is thus about  $10^{48}$  W. A gamma-ray burster emits up to  $3 \cdot 10^{47}$  W.

**Challenge 113**, page 155: They are carried away by the gravitational radiation.

**Challenge 119**, page 159: No system is known in nature which emits or absorbs only one graviton at a time. This is another point speaking against the existence of gravitons.

**Challenge 123**, page 168: Two stacked foils show the same effect as one foil of the same total thickness. Thus the surface plays no role.

**Challenge 125**, page 173: The electron is held back by the positive charge of the nucleus, if the number of protons in the nucleus is sufficient, as is the case for those nuclei we are made of.

**Challenge 127**, page 181: The half-time  $t_{1/2}$  is related to the life-time  $\tau$  by  $t_{1/2} = \tau \ln 2$ .

**Challenge 128**, page 182: The number is small compared with the number of cells. However, it is possible that the decays are related to human ageing.

Challenge 130, page 185: By counting decays and counting atoms to sufficient precision.

**Challenge 132**, page 186: The radioactivity necessary to keep the Earth warm is low; lava is only slightly more radioactive than usual soil.

**Challenge 133**, page 198: There is no way to conserve both energy and momentum in such a decay.

**Challenge 134**, page 198: The combination of high intensity X-rays and UV rays led to this effect.

**Challenge 138**, page 210: The nuclei of nitrogen and carbon have a high electric charge which strongly repels the protons.

Challenge 140, page 219: See the paper by C.J. Hogan mentioned in Ref. 270.

**Challenge 141**, page 222: Touching something requires getting near it; getting near means a small time and position indeterminacy; this implies a small wavelength of the probe that is used for touching; this implies a large energy.

**Challenge 144**, page 229: The processes are electromagnetic in nature, thus electric charges give the frequency with which they occur.

**Challenge 145**, page 238: Designing a nuclear weapon is not difficult. University students can do it, and even have done so a few times. The first students who did so were two physics graduates in 1964, as told on www.guardian.co.uk/world/2003/jun/24/usa.science. It is not hard to conceive a design and even to build it. By far the hardest problem is getting or making the nuclear material. That requires either an extensive criminal activity or a vast technical effort, with numerous large factories, extensive development, and coordination of many technological activities. Most importantly, such a project requires a large financial investment, which poor countries cannot afford without great sacrifices for all the population. The problems are thus not technical, but financial.

**Challenge 149**, page 269: In 2008, an estimated 98% of all physicists agreed. Time will tell whether they are right.

**Challenge 151**, page 281: A mass of 100 kg and a speed of 8 m/s require  $43 \text{ m}^2$  of wing surface. **Challenge 154**, page 288: The issue is a red herring. The world has three dimensions.

**Challenge 155**, page 291: The largest rotation angle  $\Delta \varphi$  that can be achieved in one stroke *C* is found by maximizing the integral

$$\Delta \varphi = -\int_C \frac{a^2}{a^2 + b^2} \mathrm{d}\theta \tag{151}$$

Since the path C in shape space is closed, we can use Stokes' theorem to transform the line integral to a surface integral over the surface S enclosed by C in shape space:

$$\Delta \varphi = \int_{S} \frac{2ab^2}{(a^2 + b^2)^2} \mathrm{d}a \,\mathrm{d}\theta \,. \tag{152}$$

The maximum angle is found by noting that  $\theta$  can vary at most between 0 and  $\pi$ , and that *a* can vary at most between 0 and  $\infty$ . This yields

$$\Delta \varphi_{\max} = \int_{\theta=0}^{\pi} \int_{a=0}^{\infty} \frac{2ab^2}{(a^2 + b^2)^2} da \, d\theta = \pi \,. \tag{153}$$

**Challenge 157**, page 295: A cloud is kept afloat and compact by convection currents. Clouds without convection can often be seen in the summer: they diffuse and disappear. The details of the internal and external air currents depend on the cloud type and are a research field on its own.

Challenge 162, page 301: Lattices are not isotropic, lattices are not Lorentz invariant.

**Challenge 164**, page 304: The infinite sum is not defined for numbers; however, it is defined for a knotted string.

**Challenge 165**, page 305: The research race for the solution is ongoing, but the goal is still far. **Challenge 166**, page 306: This is a simple but hard question. Find out!

**Challenge 169**, page 309: Large raindrops are pancakes with a massive border bulge. When the size increases, e.g. when a large drop falls through vapour, the drop splits, as the central membrane is then torn apart.

**Challenge 170**, page 309: It is a drawing; if it is interpreted as an image of a three-dimensional object, it either does not exist, or is not closed, or is an optical illusion of a torus.

**Challenge 171**, page 309: See T. FINK & Y. MAO, *The 85 Ways to Tie a Tie*, Broadway Books, 2000.

**Challenge 172**, page 309: See T. CLARKE, *Laces high*, Nature Science Update 5th of December, 2002, or www.nature.com/nsu/021202/021202-4.html.

**Challenge 175**, page 311: In fact, nobody has even tried to do so yet. It may also be that the problem makes no sense.

**Challenge 177**, page 317: Most macroscopic matter properties fall in this class, such as the change of water density with temperature.

**Challenge 179**, page 323: Before the speculation can be fully tested, the relation between particles and black holes has to be clarified first.

**Challenge 180**, page 324: Never expect a correct solution for personal choices. Do what you yourself think and feel is correct.

**Challenge 185**, page 331: Planck limits can be exceeded for extensive observables for which many particle systems can exceed single particle limits, such as mass, momentum, energy or electrical resistance.

**Challenge 187**, page 333: Do not forget the relativistic time dilation.

**Challenge 188**, page 333: The formula with n - 1 is a better fit. Why?

**Challenge 192**, page 340: The slowdown goes *quadratically* with time, because every new slow-down adds to the old one!

**Challenge 193**, page 341: No, only properties of parts of the universe are listed. The universe Vol. VI, page 112 itself has no properties, as shown in the last volume.

**Challenge 194**, page 343: The gauge coupling constants, via the Planck length, determine the size of atoms, the strength of chemical bonds and thus the size of all things.

**Challenge 195**, page 358: Covalent bonds tend to produce full shells; this is a smaller change on the right side of the periodic table.

**Challenge 196**, page 360: The solution is the set of all two by two matrices, as each two by two matrix specifies a linear transformation, if one defines a transformed point as the product of the point and this matrix. (Only multiplication with a fixed matrix can give a linear transformation.) Can you recognize from a matrix whether it is a rotation, a reflection, a dilation, a shear, or a stretch along two axes? What are the remaining possibilities?

**Challenge 199**, page 360: The (simplest) product of two functions is taken by point-by-point multiplication.

**Challenge 200**, page 361: The norm ||f|| of a real function f is defined as the supremum of its absolute value:

$$\|f\| = \sup_{x \in \mathbb{R}} |f(x)| .$$
(154)

In simple terms: the maximum value taken by the absolute of the function is its norm. It is also called 'sup'-norm. Since it contains a supremum, this norm is only defined on the subspace of *bounded* continuous functions on a space X, or, if X is compact, on the space of all continuous functions (because a continuous function on a compact space must be bounded).

**Challenge 203**, page 364: Take out your head, then pull one side of your pullover over the corresponding arm, continue pulling it over the over arm; then pull the other side, under the first, to the other arm as well. Put your head back in. Your pullover (or your trousers) will be inside out.

**Challenge 204**, page 364: Both can be untied.

**Challenge 208**, page 369: The transformation from one manifold to another with different topology can be done with a tiny change, at a so-called *singular point*. Since nature shows a minimum action, such a tiny change cannot be avoided.

**Challenge 209**, page 371: The product  $M^{\dagger}M$  is Hermitean, and has positive eigenvalues. Thus H is uniquely defined and Hermitean. U is unitary because  $U^{\dagger}U$  is the unit matrix.





Gedanken sind nicht stets parat. Man schreibt auch, wenn man keine hat.\* Wilhelm Busch, *Aphorismen und Reime*.

- 1 The use of radioactivity for breeding of new sorts of wheat, rice, cotton, roses, pineapple and many more is described by B. S. AHLOOWALIA & M. MALUSZYNSKI, *Induced mutations a new paradigm in plant breeding*, Euphytica 11, pp. 167–173, 2004. Cited on page 22.
- 2 See JOHN T. BONNER, *Why Size Matters: From Bacteria to Blue Whales*, Princeton University Press, 2011. Cited on page 22.
- **3** See the book by PETER LÄUGER, *Electrogenic Ion Pumps*, Sinauer, 1991. Cited on page 22.
- **4** The motorized screw used by viruses was described by A.A. SIMPSON & al., *Structure of the bacteriophage phi29 DNA packaging motor*, Nature **408**, pp. 745–750, 2000. Cited on page 23.
- 5 S. M. BLOCK, *Real engines of creation*, Nature 386, pp. 217–219, 1997. Cited on page 23.
- 6 Early results and ideas on molecular motors are summarised by B. GOSS LEVI, *Measured steps advance the understanding of molecular motors*, Physics Today pp. 17–19, April 1995. Newer results are described in R. D. ASTUMIAN, *Making molecules into motors*, Scientific American pp. 57–64, July 2001. Cited on pages 23 and 24.
- R. BARTUSSEK & P. HÄNGGI, Brownsche Motoren, Physikalische Blätter 51, pp. 506-507, 1995. See also R. ALT-HADDOU & W. HERZOG, Force and motion generation of myosin motors: muscle contraction, Journal of Electromyography and kinesiology 12, pp. 435-445, 2002. Cited on page 25.
- 8 N. HIROKAWA, S. NIWA & Y. TANAKA, Molecular motors in neurons: transport mechanisms and roles in brain function, development, and disease, Neuron 68, pp. 610–638, 2010. Cited on page 26.
- **9** J. WEBER & A. E. SENIOR, *ATP synthesis driven by proton transport in F1Fo-ATP synthase*, FEBS letters 545, pp. 61–70, 2003. Cited on page 27.
- 10 This truly fascinating research result, worth a Nobel Prize, is summarized in N. HIROKAWA, Y. TANAKA & Y. OKADA, Left-right determination: involvement of molecular motor KIF3, cilia, and nodal flow, Cold Spring Harbor Perspectives in Biology 1, p. a000802, 2009, also available at www.cshperspectives.org. The website also links to numerous captivating films of the involved microscopic processes, found at beta. cshperspectives.cshlp.org. Cited on page 29.
- 11 R. J. CANO & M. K. BORUCKI, *Revival and identification of bacterial spores in 25- to 40million-year-old Dominican amber*, Science 26, pp. 1060–1064, 1995. Cited on page 32.

<sup>\* &#</sup>x27;Thoughts are not always available. Many write even without them.'

- 12 The first papers on bacteria from salt deposits were V. R. OTT & H. J. DOMBRWOSKI, Mikrofossilien in den Mineralquellen zu Bad Nauheim, Notizblatt des Hessischen Landesamtes für Bodenforschung 87, pp. 415–416, 1959, H. J. DOMBROWSKI, Bacteria from Paleozoic salt deposits, Annals of the New York Academy of Sciences 108, pp. 453–460, 1963. A recent confirmation is R. H. VREELAND, W. D. ROSENZWEIG & D. W. POWERS, Isolation of a 250 million-year-old halotolerant bacterium from a primary salt crystal, Nature 407, pp. 897–899, 2000. Cited on page 32.
- 13 This is explained in D. GRAUR & T. PUPKO, The permian bacterium that isn't, Molecular Biology and Evolution 18, pp. 1143–1146, 2001, and also in M. B. HEBSGAARD, M. J. PHILLIPS & E. WILLERSLEV, Geologically ancient DNA: fact or artefact?, Trends in Microbiology 13, pp. 212–220, 2005. Cited on page 32.
- **14** GABRIELE WALKER, Snowball Earth The Story of the Great Global Catastrophe That Spawned Life as We Know It, Crown Publishing, 2003. No citations.
- 15 J. D. RUMMEL, J. H. ALLTON & D. MORRISON, A microbe on the moon? Surveyor III and lessons learned for future sample return missions, preprint at www.lpi.usra.edu/meetings/ sssr2011/pdf/5023.pdf. Cited on page 32.
- 16 The table and the evolutionary tree are taken from J. O. MCINERNEY, M. MULLARKEY, M. E. WERNECKE & R. POWELL, *Bacteria and archaea: molecular techniques reveal astonishing diversity*, Biodiversity 3, pp. 3–10, 2002. The evolutionary tree might still change a little in the coming years. Cited on page 33.
- 17 The newest estimate is by R. SENDER, S. FUCHS & R. MILO, Revised estimates for the number of human and bacteria cells in the body, PLOS Biology 14, p. e1002533, 2016, free preprint at biorxiv.org/content/early/2016/01/06/036103. The first professional estimate was by E. BIANCONI, A. PIOVESAN, F. FACCHIN, A. BERAUDI, R. CASADEI, F. FRABETTI, L. VITALE, M. C. PELLERI, S. TASSANI, F. PIVA, S. PEREZ-AMODIO, P. STRIPPOLI & S. CANAIDER, An estimation of the number of cells in the human body, Annals of Human Biology 40, pp. 463–471, 2013, also available for free online. A typical older and more optimistic estimate is E. K. COSTELLO, C. L. LAUBER, M. HAMADY, N. FIERER, J. I. GORDON & R. KNIGHT, Bacterial community variation in human body habitats across space and time, Science Express 5 November 2009. Cited on page 34.
- 18 E. PUTTONEN, C. BRIESE, G. MANDLBURGER, M. WIESER, M. PFENNIGBAUER, A. ZLINSKY & N. PFEIFER, Quantification of overnight movement of birch (Betula pendula) branches and foliage with short interval terrestrial laser scanning, Frontiers in Plant Science 7, 2016, free download at journal.frontiersin.org. A video of the tree motion is also available there. Cited on page 38.
- **19** This is taken from the delightful children text HANS J. PRESS, *Spiel das Wissen schafft*, Ravensburger Buchverlag 1964, 2004. Cited on page 39.
- 20 The discovery of a specific taste for fat was published by F. LAUGERETTE, P. PASSILLY-DEGRACE, B. PATRIS, I. NIOT, M. FEBBRAIO, J. P. MONTMAYEUR & P. BESNARD, CD36 involvement in orosensory detection of dietary lipids, spontaneous fat preference, and digestive secretions, Journal of Clinical Investigation 115, pp. 3177–3184, 2005. Cited on page 41.
- **21** There is no standard procedure to learn to enjoy life to the maximum. A good foundation can be found in those books which teach the ability to those which have lost it.

The best experts are those who help others to overcome traumas. PETER A. LEVINE & ANN FREDERICK, Waking the Tiger – Healing Trauma – The Innate Capacity to Transform Overwhelming Experiences, North Atlantic Books, 1997. GEOFF GRAHAM, How to

Become the Parent You Never Had - a Treatment for Extremes of Fear, Anger and Guilt, Real Options Press, 1986. A good complement to these texts is the approach presented by BERT HELLINGER, Zweierlei Glück, Carl Auer Verlag, 1997. Some of his books are also available in English. The author presents a simple and efficient technique for reducing entanglement with one's family past. Another good book is PHIL STUTZ & BARRY MICHELS, The Tools – Transform Your Problems into Courage, Confidence, and Creativity, Random House, 2012.

The next step, namely full mastery in the enjoyment of life, can be found in any book written by somebody who has achieved mastery in any one topic. The topic itself is not important, only the passion is. A few examples:

A. DE LA GARANDERIE, Le dialogue pédagogique avec l'élève, Centurion, 1984, A. DE LA GARANDERIE, Pour une pédagogie de l'intelligence, Centurion, 1990, A. DE LA GARANDERIE, Réussir ça s'apprend, Bayard, 1994. De la Garanderie explains how the results of teaching and learning depend in particular on the importance of evocation, imagination and motivation.

PLATO, Phaedrus, Athens, 380 BCE.

FRANÇOISE DOLTO, *La cause des enfants*, Laffont, 1985, and her other books. Dolto (b. 1908 Paris, d. 1988 Paris), a child psychiatrist, is one of the world experts on the growth of the child; her main theme was that growth is only possible by giving the highest possible responsibility to every child during its development.

In the domain of art, many had the passion to achieve full pleasure. A good piece of music, a beautiful painting, an expressive statue or a good film can show it. On a smaller scale, the art to typeset beautiful books, so different from what many computer programs do by default, the best introduction are the works by Jan Tschichold (b. 1902 Leipzig, d. 1974 Locarno), the undisputed master of the field. Among the many books he designed are the beautiful Penguin books of the late 1940s; he also was a type designer, e.g. of the *Sabon* typeface. A beautiful summary of his views is the short but condensed text JAN TSCHICHOLD, *Ausgewählte Aufsätze über Fragen der Gestalt des Buches und der Typographie*, Birkhäuser Verlag, Basel, 1993. An extensive and beautiful textbook on the topic is HANS PETER WILLBERG & FRIEDRICH FORSSMAN, *Lesetypographie*, Verlag Hermann Schmidt, Mainz, 1997. See also ROBERT BRINGHURST, *The Elements of Typographic Style*, Hartley & Marks, 2004.

Many scientists passionately enjoyed their occupation. Any biography of Charles Darwin will purvey his fascination for biology, of Friedrich Bessel for astronomy, of Albert Einstein for physics and of Linus Pauling for chemistry. Cited on page 42.

- **22** The group of John Wearden in Manchester has shown by experiments with humans that the accuracy of a few per cent is possible for any action with a duration between a tenth of a second and a minute. See J. MCCRONE, *When a second lasts forever*, New Scientist pp. 53–56, 1 November 1997. Cited on page 43.
- 23 The chemical clocks in our body are described in JOHN D. PALMER, *The Living Clock*, Oxford University Press, 2002, or in A. AHLGREN & F. HALBERG, *Cycles of Nature: An Introduction to Biological Rhythms*, National Science Teachers Association, 1990. See also the www.msi.umn.edu/~halberg/introd website. Cited on page 43.
- 24 D.J MORRÉ & al., *Biochemical basis for the biological clock*, Biochemistry 41, pp. 11941–11945, 2002. Cited on page 43.
- 25 An introduction to the sense of time as result of clocks in the brain is found in R. B. IVRY & R. SPENCER, *The neural representation of time*, Current Opinion in Neurobiology 14, pp. 225–232, 2004. The interval timer is explain in simple words in K. WRIGHT, *Times in our lives*, Scientific American pp. 40–47, September 2002. The MRI research used is

S. M. RAO, A. R. MAYER & D. L. HARRINGTON, *The evolution of brain activation during temporal processing*, Nature Neuroscience 4, pp. 317–323, 2001. Cited on page 45.

- **26** See, for example, JAN HILGEVOORD, *Time in quantum mechanics*, American Journal of Physics 70, pp. 301–306, 2002. Cited on page 45.
- **27** E. J. ZIMMERMAN, *The macroscopic nature of space-time*, American Journal of Physics 30, pp. 97–105, 1962. Cited on page 46.
- **28** See P.D. PEŞIĆ, *The smallest clock*, European Journal of Physics 14, pp. 90–92, 1993. Cited on page 46.
- **29** The possibilities for precision timing using single-ion clocks are shown in W.H. OSKAY & al., *Single-atom clock with high accuracy*, Physical Review Letters **97**, p. 020801, 2006. Cited on page 47.
- **30** A pretty example of a quantum mechanical system showing exponential behaviour at all times is given by H. NAKAZATO, M. NAMIKI & S. PASCAZIO, *Exponential behaviour of a quantum system in a macroscopic medium*, Physical Review Letters 73, pp. 1063–1066, 1994. Cited on page 49.
- 31 See the delightful book about the topic by PAOLO FACCHI & SAVERIO PASCAZIO, La regola d'oro di Fermi, Bibliopolis, 1999. An experiment observing deviations at short times is S.R. WILKINSON, C.F. BHARUCHA, M.C. FISCHER, K.W. MADISON, P.R. MORROW, Q. NIU, B. SUNDARAM & M.G. RAIZEN, Nature 387, p. 575, 1997. Cited on page 49.
- **32** See, for example, R. EFRON, *The duration of the present*, Annals of the New York Academy of Sciences 138, pp. 713–729, 1967. Cited on page 49.
- 33 W. M. ITANO, D. J. HEINZEN, J. J. BOLLINGER & D. J. WINELAND, Quantum Zeno effect, Physical Review A 41, pp. 2295–2300, 1990. M. C. FISCHER, B. GUTIÉRREZ-MEDINA & M. G. RAIZEN, Observation of the Quantum Zeno and Anti-Zeno effects in an unstable system, Physical Review Letters 87, p. 040402, 2001, also www-arxiv.org/abs/ quant-ph/0104035. Cited on page 51.
- 34 See P. FACCHI, Z. HRADIL, G. KRENN, S. PASCAZIO & J. ŘEHÁČEK Quantum Zeno tomography, Physical Review A 66, p. 012110, 2002. Cited on page 51.
- **35** See P. FACCHI, H. NAKAZATO & S. PASCAZIO From the quantum Zeno to the inverse quantum Zeno effect, Physical Review Letters 86, pp. 2699–2702, 2001. Cited on page 51.
- **36** H. KOBAYASHI & S. KOHSHIMA, Unique morphology of the human eye, Nature 387, pp. 767–768, 1997. No citations.
- **37** JAMES W. PRESCOTT, *Body pleasure and the origins of violence*, The Futurist Bethseda, 1975, also available at www.violence.de/prescott/bullettin/article.html. Cited on page 54.
- **38** FRANCES ASHCROFT, *The Spark of Life: Electricity in the Human Body*, Allen Lane, 2012. Cited on page 54.
- **39** FELIX TRETTER & MARGOT ALBUS, Einführung in die Psychopharmakotherapie Grundlagen, Praxis, Anwendungen, Thieme, 2004. Cited on page 56.
- **40** See the talk on these experiments by Helen Fisher on www.ted.org and the information on helenfisher.com. Cited on page 57.
- 41 See for example P. PYYKKÖ, Relativity, gold, closed-shell interactions, and CsAu.NH3, Angewandte Chemie, International Edition 41, pp. 3573–3578, 2002, or L. J. NORRBY, Why is mercury liquid? Or, why do relativistic effects not get into chemistry textbooks?, Journal of Chemical Education 68, pp. 110–113, 1991. Cited on page 59.

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- **43** For good figures of atomic orbitals, take any modern chemistry text. Or go to csi.chemie. tu-darmstadt.de/ak/immel/. Cited on page 61.
- **44** For experimentally determined pictures of the orbitals of dangling bonds, see for example F. GIESSIBL & al., *Subatomic features on the silicon (111)-(7x7) surface observed by atomic force microscopy*, Science **289**, pp. 422–425, 2000. Cited on page 61.
- 45 L. GAGLIARDI & B. O. ROOS, Quantum chemical calculations show that the uranium molecule U<sub>2</sub> has a quintuple bond, Nature 433, pp. 848–851, 2005. B. O. ROOS, A. C. BORIN & L. GAGLIARDI, Reaching the maximum multiplicity of the covalent chemical bond, Angewandte Chemie, International Edition 46, pp. 1469–1472, 2007. Cited on page 63.
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- **50** T. GU, M. LI, C. MCCAMMON & K. K. M. LEE, *Redox-induced lower mantle density contrast and effect on mantle structure and primitive oxygen*, Nature Geoscience 9, pp. 723–727, 2016. Cited on page 72.
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#### Acknowledgements

Many people who have kept their gift of curiosity alive have helped to make this project come true. Most of all, Peter Rudolph and Saverio Pascazio have been – present or not – a constant reference for this project. Fernand Mayné, Ata Masafumi, Roberto Crespi, Serge Pahaut, Luca Bombelli, Herman Elswijk, Marcel Krijn, Marc de Jong, Martin van der Mark, Kim Jalink, my parents Peter and Isabella Schiller, Mike van Wijk, Renate Georgi, Paul Tegelaar, Barbara and Edgar Augel, M. Jamil, Ron Murdock, Carol Pritchard, Richard Hoffman, Stephan Schiller, Franz Aichinger and, most of all, my wife Britta have all provided valuable advice and encouragement.

Many people have helped with the project and the collection of material. Most useful was the help of Mikael Johansson, Bruno Barberi Gnecco, Lothar Beyer, the numerous improvements by Bert Sierra, the detailed suggestions by Claudio Farinati, the many improvements by Eric Sheldon, the detailed suggestions by Andrew Young, the continuous help and advice of Jonatan Kelu, the corrections of Elmar Bartel, and in particular the extensive, passionate and conscientious help of Adrian Kubala.

Important material was provided by Bert Peeters, Anna Wierzbicka, William Beaty, Jim Carr, John Merrit, John Baez, Frank DiFilippo, Jonathan Scott, Jon Thaler, Luca Bombelli, Douglas Singleton, George McQuarry, Tilman Hausherr, Brian Oberquell, Peer Zalm, Martin van der Mark, Vladimir Surdin, Julia Simon, Antonio Fermani, Don Page, Stephen Haley, Peter Mayr, Allan Hayes, Norbert Dragon, Igor Ivanov, Doug Renselle, Wim de Muynck, Steve Carlip, Tom Bruce, Ryan Budney, Gary Ruben, Chris Hillman, Olivier Glassey, Jochen Greiner, squark, Martin Hardcastle, Mark Biggar, Pavel Kuzin, Douglas Brebner, Luciano Lombardi, Franco Bagnoli, Lukas Fabian Moser, Dejan Corovic, Paul Vannoni, John Haber, Saverio Pascazio, Klaus Finkenzeller, Leo Volin, Jeff Aronson, Roggie Boone, Lawrence Tuppen, Quentin David Jones, Arnaldo Uguzzoni, Frans van Nieuwpoort, Alan Mahoney, Britta Schiller, Petr Danecek, Ingo Thies, Vitaliy Solomatin, Carl Offner, Nuno Proença, Elena Colazingari, Paula Henderson, Daniel Darre, Wolfgang Rankl, John Heumann, Joseph Kiss, Martha Weiss, Antonio González, Antonio Martos, André Slabber, Ferdinand Bautista, Zoltán Gácsi, Pat Furrie, Michael Reppisch, Enrico Pasi, Thomas Köppe, Martin Rivas, Herman Beeksma, Tom Helmond, John Brandes, Vlad Tarko, Nadia Murillo, Ciprian Dobra, Romano Perini, Harald van Lintel, Andrea Conti, François Belfort, Dirk Van de Moortel, Heinrich Neumaier, Jarosław Królikowski, John Dahlman, Fathi Namouni, Paul Townsend, Sergei Emelin, Freeman Dyson, S.R. Madhu Rao, David Parks, Jürgen Janek, Daniel Huber, Alfons Buchmann, William Purves, Pietro Redondi, Douglas Singleton, Emil Akhmedov Damoon Saghian, Zach Joseph Espiritu, Miles Mutka, plus a number of people who wanted to remain unnamed.

The software tools were refined with extensive help on fonts and typesetting by Michael Zedler and Achim Blumensath and with the repeated and valuable support of Donald Arseneau; help came also from Ulrike Fischer, Piet van Oostrum, Gerben Wierda, Klaus Böhncke, Craig Upright, Herbert Voss, Andrew Trevorrow, Danie Els, Heiko Oberdiek, Sebastian Rahtz, Don Story, Vincent Darley, Johan Linde, Joseph Hertzlinger, Rick Zaccone, John Warkentin, Ulrich Diez, Uwe Siart, Will Robertson, Joseph Wright, Enrico Gregorio, Rolf Niepraschk, Alexander Grahn and Paul Townsend.

The typesetting and book design is due to the professional consulting of Ulrich Dirr. The typography was much improved with the help of Johannes Küster and his Minion Math font. The design of the book and its website also owe much to the suggestions and support of my wife Britta.

I also thank the lawmakers and the taxpayers in Germany, who, in contrast to most other countries in the world, allow residents to use the local university libraries.

From 2007 to 2011, the electronic edition and distribution of the Motion Mountain text was generously supported by the Klaus Tschira Foundation.

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Christoph Schiller, PhD Université Libre de Bruxelles, is a physicist and physics popularizer. He wrote this book for his children and for all students, teachers and readers interested in physics, the science of motion.

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